MICROSTRUCTURE-BASED 3D FE MODELING FOR MICRO CUTTING FERRITIC-PEARLITIC CARBON STEELS

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ABSTRACT
The mechanics of the cutting process on the microscopic level differ fundamentally from the conventional macro cutting. For example, the tool edge radius influences the cutting mechanism in micro machining significantly with regard to the effective rake angle, the minimum chip thickness, the dominance of ploughing, and the related elasto-plastic deformation of the workpiece material. These phenomena, known as size effects, have a profound impact on the cutting force, process stability, and resulting surface finish in micro cutting. Therefore, microstructural effects in microscale cutting require quite different assumptions to be made concerning underlying material behaviour during micro cutting and have led to the need for new modeling approaches to account for such effects.

This paper presents a three-dimensional finite element approach to incorporate microstructure into micro cutting simulation based on the concept of a representative volume element (RVE) and constitutive material modeling as well as using the Lagrangian formulation proposed in the implicit FE code Deform 3D™. Micro drilling and micro milling tests using solid carbide tools with different diameters (d = 50 µm – 1 mm) were performed on ferrite-pearlite two-phase steel AISI 1045 for the verification of the developed 3D multiphase FE computation model regarding chip formation, feed force, and torque. The developed 3D multiphase FE model was successfully used to predict size effects in micro cutting.

NOMENCLATURE
A initial yield stress
B hardening modulus
C strain rate sensitivity coefficient
FE finite element
F_x cutting force in x direction
F_y cutting force in y direction
F_z cutting force in z direction
JC Johnson-Cook law
SEM Scanning Electron Microscope
T temperature
a_c width of cut
a_p depth of cut
d diameter
f total cutting feed
f_c cutting feed per cutting edge
k_f related feed force
m thermal softening exponent
n strain hardening exponent
r_e cutting edge radius
\tau_{rel} related torque
V_{C} cutting speed
V_{f} feed velocity
\sigma effective stress
\varepsilon plastic strain
\dot{\varepsilon} strain rate
\mu Coulomb friction coefficient
1 INTRODUCTION

Due to the advantages of micro technological solutions, such as small dimensions, low weight, energy efficiency, simultaneous functions integration and new applications, the product miniaturization is worldwide considered as key technology for the 21st century. Therefore, micro machining is a central topic in product development in different fields of application as electronics, telecommunications, sensor technologies, optics, medical engineering, watch manufacturing, biotechnology and environmental engineering [1-3].

Although conventional machining and micro machining show many similarities, the cutting parameters of conventional machining, like cutting speed, feed, depth of cut and width of cut, cannot be offhand downscaled into the micro range due to size effects [4-9]. When the uncut chip thickness is on the same order as the material grain size, the workpiece material cannot any more be assumed as homogeneous and isotropic. Furthermore, the tool edge radius influences the cutting mechanism in micro machining significantly with regard to the effective rake angle and the ploughing effect [10-12].

In the past seven decades, conventional macro cutting mechanics have been amply investigated and various analytical, mechanistic, empirical and numerical models were developed to understand the thermo-mechanical interactions between workpiece material, tool and chip during the cutting process [13-22]. Most developed cutting models which are based on assumptions such as relative sharp tool edge radius and homogenous materials cannot be simply applied to micro cutting operations due to the above mentioned size effects. Especially, micro cutting of multiphase materials results in significantly varying cutting mechanisms and associated process response [23-26].

A popular tool in helping to explain the effects of microstructure during micro cutting is the use of finite element (FE) simulations. Due to the very complicated cutting process at the microscale and the higher modeling effort, most developed FE models for micro cutting heterogeneous materials are still limited at present to the two dimensional orthogonal cut and only give a qualitative prediction of simple plane strain cutting processes [27-30].

Based on the concept of a representative volume element (RVE) and constitutive material modeling, a 3D multiphase FE computational model is presented in this paper to simulate explicitly micro cutting ferritic-pearlitic carbon steels. The paper has three parts. First, a material characterization including the analysis of the microstructure and constitutive equations for each phase ferrite, pearlite and composite ferritic-pearlitic carbon steel C45 (AISI 1045) is discussed. Then, the development of the two phase 3D FE material model for steel C45 is described. Finally, the validation of the developed multiphase FE model using micro drilling and micro milling is performed.

2 MATERIAL CHARACTERIZATION

2.1 Microstructure

The materials used in this investigation are ferritic-pearlitic carbon steels C05, C45, and C75 with different carbon contents ranging from 0.05% to 0.75% but otherwise similar composition of other alloying elements. The materials were hot drawn, shaved, ground, normalized and supplied as steel bars with a diameter of 10 mm. The microstructure of carbon steels consists of ferrite and pearlite, where the volume fractions depend primarily on the carbon content. Pearlite is a lamellar structure consisting of two phases, namely ferrite and cementite. For this purpose, steel C05 was assumed to be purely ferritic and steel C75 to be purely pearlitic. Quasi-static flow curves and one representative optical micrograph of each steel are shown in Fig. 1. In steel C05, ferrite, as white areas, is the dominating phase with a sparse distribution of pearlite, especially at grain corners. In steels C45 and C75 with higher carbon contents, pearlite is the dominating structure and ferrite is seen as white pockets between pearlite colonies (steel C45) and as grain boundary ferrite (steel C75). The carbon steels show a fairly similar hardening behaviour, while the difference in yield stress is large, see Fig. 1.

![Figure 1. Flow curves and microstructure of the investigated carbon steels.](image)

In this work, the steel’s microstructure is characterized with respect to the volume fractions of the two structural constituents, ferrite and pearlite and the grain size of ferrite. The interlamellar spacing and the aspect ratio of pearlite are assumed to be the same for the investigated steels. The volume fractions of ferrite and pearlite of the steels were evaluated from micrographs and compared with the calculated values from the iron-carbon phase diagram. The determined volume fraction of pearlite in steels C05, C45, and C75 are 1%, 60%, and 99%, respectively, see Table 1. The average grain sizes of ferrite were measured using the intercept method and presented in Table 1. The smaller ferrite grain size measured in steel C45 is expected
since pearlite has grown in the material thereby decreasing the ferrite grains.

Table 1. Microstructural data.

<table>
<thead>
<tr>
<th>Steel</th>
<th>Carbon, w%</th>
<th>Pearlite, %</th>
<th>Ferrite, %</th>
<th>Ferrite grain size, μm</th>
</tr>
</thead>
<tbody>
<tr>
<td>C05</td>
<td>0.05</td>
<td>1</td>
<td>99</td>
<td>30</td>
</tr>
<tr>
<td>C45</td>
<td>0.45</td>
<td>60</td>
<td>40</td>
<td>15</td>
</tr>
<tr>
<td>C75</td>
<td>0.75</td>
<td>99</td>
<td>1</td>
<td>-</td>
</tr>
</tbody>
</table>

2.2 Constitutive material modeling

To determine the mechanical flow behaviour of the carbon steels, uniaxial compression tests were performed on cylindrical specimens (Ø 4x4 mm) of each steel at different strain rates. The compression tests with lower strain rates (\( \varepsilon < 1 \text{ 1/s} \)) were carried out using a numerically controlled hydraulic testing machine. The high strain rate tests with \( \varepsilon > 1000 \text{ 1/s} \), were performed on a modified Split Hopkinson Pressure Bar [31].

The constitutive Johnson-Cook (JC) law was applied for the material modeling. The JC model is a strain rate and temperature dependent visco-plastic material model [32], which describes the thermo-mechanical material flow behavior (strain hardening, strain rate sensitivity, and thermal softening) over the entire strain rate and temperature range. The JC model uses the following equation for the equivalent flow stress:

\[
\sigma = (A + B \varepsilon^n) \left(1 + C \ln \left(\frac{\varepsilon}{\varepsilon_0}\right) \right) \left[1 - \left(\frac{T - T_r}{T_m - T_r}\right)^m\right] \quad (1)
\]

Where \( \sigma \), \( \varepsilon \), \( \varepsilon_0 \), and \( T \) represent the equivalent flow stress, the equivalent plastic strain, the plastic strain rate and the absolute temperature, respectively. The JC parameters \( n \) (strain hardening exponent), \( C \) (strain rate sensitivity coefficient), and \( m \) (thermal softening exponent) describe the thermo-mechanical material behavior. The remaining JC material parameters are \( A \) (the initial yield stress), \( B \) (the hardening modulus), \( \varepsilon_0 \) (reference strain rate), \( T_r \) (room temperature), and \( T_m \) (melting temperature).

The JC equation parameters \( A \), \( B \), \( n \), and \( C \) were determined with help of the determined flow curves at room temperature of the correspondent steel and listed in Table 2. The thermal softening exponent \( m \) was identified by means of quasi-static compression tests at different temperatures (20°C - 800°C), see Table 2. The reference parameters \( \varepsilon_0 = 0.002 \text{ s}^{-1} \), \( T_r = 20^\circ \text{C} \), \( T_m = 1500^\circ \text{C} \) are specified.

Table 2. The parameter values of the JC equation for the carbon steels.

<table>
<thead>
<tr>
<th>Steel</th>
<th>( A ), MPa</th>
<th>( B ), MPa</th>
<th>( n )</th>
<th>( C )</th>
<th>( m )</th>
</tr>
</thead>
<tbody>
<tr>
<td>C05</td>
<td>175</td>
<td>571</td>
<td>0.35</td>
<td>0.034</td>
<td>1.86</td>
</tr>
<tr>
<td>C45</td>
<td>546</td>
<td>487</td>
<td>0.25</td>
<td>0.015</td>
<td>1.22</td>
</tr>
<tr>
<td>C75</td>
<td>750</td>
<td>593</td>
<td>0.33</td>
<td>0.011</td>
<td>1.10</td>
</tr>
</tbody>
</table>

Figure 2 shows a comparison between calculated flow stresses following Eq. 1 (continuous curves) and measured flow stresses from the compression tests (markers) at different strain rates and at a constant strain of \( \varepsilon = 0.1 \). It is obvious that the JC material model describes the flow behaviour of the investigated carbon steels relatively well in the entire range of strain rates. In addition to the constitutive JC model, the linear rule-of-mixtures (ROM) is used to predict the mechanical behaviour of the two-phase steel C45. The flow stress data calculated by the linear rule-of-mixtures (dashed line, Fig. 2) show a quite good agreement with the experiment and the JC model. Consequently, the flow stress increases approximately linearly with the pearlite volume fraction. The flow curves of the two-phase carbon steel scale in a nice manner that JC equation parameters \( (A_c, B_c, n_c, C_c, \text{and } m_c) \) can be determined for all carbon steels by means of the pearlite volume fraction \( f_p \) (or carbon percentage) and JC parameters of Ferrite (\( A_F, B_F, C_F, \text{and } m_F \)) and Pearlite (\( A_P, B_P, n_p, C_P, \text{and } m_P \)), as shown Fig. 2. The micromechanical modeling based on the microstructure and constitutive material data is then possible, in order to predict the deformation behaviour. In the two-phase FE material modeling, the steels C05 and C75 were used to describe the thermo-mechanical behaviour of the phases ferrite and pearlite, respectively.

3 TWO-PHASE FE MATERIAL MODEL FOR STEEL C45

3.1 Modeling approach

Based on the concept of a representative volume element (RVE), introduced by Hill [33], a new 3D two-phase FE material model was developed for the ferritic-pearlitic carbon steel C45. The RVE concept considers only a small material part that has the same average behaviour as a larger model. In the formulation of the FE material model, the microstructural data (phase volume fraction, ferrite grain size) and the
and pearlite behave in the same way in the two-phase material C45, as they do as single phases in C05 and C75 respectively. Fig. 4 shows a comparison between the experimental and computed flow curves under different loads. It is obvious that the developed multiphase 3D FE material model reproduces the mechanical behaviour of the real material C45 fairly well and can adequately be used for the simulation of micro cutting, provided that the RVE’s volume is greater or equal to 10\(^3\) mm\(^3\).

4 MICROSTRUCTURE-BASED 3D FE COMPUTATION MODEL FOR MICRO CUTTING

4.1 Multiphase FE modeling approach

In this research work, a 3D thermo mechanically coupled two-phase finite element model of the micro cutting processes has been developed by using the commercial implicit FE code Deform-3DTM. The representation of tool and workpiece in the 3D FE simulation requires the input of geometrical, thermal and mechanical data. Since the geometry of the tool strongly influences the micro cutting process, the design of the selected micro tools has to be accurate. Only then, the FE model is able to predict real process behaviour during cutting. The micro tools geometries are designed by CAD, whereas the detailed geometric parameters of the tool are made available by the tool manufacture.

The generated CAD models for the micro tools are then compared with the real micro tools. For more efficient computing, the volume of the modelled workpiece was selected as small as possible. The CAD models have been transferred in Deform 3D and meshed using 3D tetrahedron elements. After the meshing of workpiece, the two-phase microstructure was generated using the developed multiphase material model (see section above). Exemplarily, the generated 3D two-phase FE models for micro drilling and micro milling with d = 1 mm are shown in Fig. 5.
4.2 Boundary conditions

The movement of the micro tools (rigid body with mesh) is specified by its translation and angular velocities in z-direction, while the workpiece (deformable) is constrained on the bottom and the round surfaces in the x, y, and z directions. Friction at the objects interfaces, tool-workpiece and chip-workpiece is governed by the Coulomb friction model ($\mu = 0.2$). For the thermal boundary conditions, conduction and convection of the generated heat are applied. The gap conductance and the thermal convection coefficient between two contacting surfaces are assumed to be $10^7$ W/m²K and 20 W/m²K, respectively. The workpiece and tool temperatures are initially set to room temperature (20°C). In order to adapt the energy balance in the modeled workpiece to the experiment, the nodes temperature at the bottom and the round surfaces are kept constant at a value of 20°C. The implicit 3D simulation of the micro cutting process requires an enormous amount of CPU time. Therefore, parallel computing (2 x 3.2 GHz) are necessary to solve such a complicated problem.

5 MICRO CUTTING VALIDATION TESTS

5.1 Micro cutting setup

In order to validate the developed 3D multi-phase FE computation model, experimental and computational micro drilling and milling tests were carried out on the investigated steel C45 using different tool diameters (full carbide tools: $d = 100 \, \mu\text{m}$ - 1 mm). The micro cutting tests were conducted without the application of coolant on the ultra-precision CNC machining centre KERN Evolution (Fig. 6, position accuracy of ± 0.5 µm, maximum spindle speed of 160,000 rpm). The cutting speed $v_c = 35 \, \text{m/min}$, the feed $f = 0.012 \cdot d$ and the drilling depth of 2•$d$ are the cutting parameters for the micro drilling tests and $v_c = 60, 80, 100 \, \text{m/min}$, the feed per cutting edge $f_c = 0.01 \cdot d$, the depth of cut $a_p = 0.4 \cdot d$ and the width of cut $a_e = 0.1 \cdot d$ for micro milling.

The cutting force and torque were measured using a Kistler dynamometer 9256B (working range of ± 250 N, response threshold of 2 mN) and a highly sensitive torque sensor Kistler 9329A (working range of ± 1 Nm, response threshold of 30 µNm).

Figure 5. 3D two-phase FE models for micro drilling and micro milling.

Figure 6. Ultra-precision micro machine tool.

In order to investigate the influence of the microstructure in micro drilling, two types of simulation were performed, one with isotropic and homogeneous material behavior and the second with the mixture material model discussed above. Furthermore, drill CAD models with sharp as well as rounded cutting edge were employed in the FE simulation to demonstrate the influence of the cutting edge rounding. Three size effects identified in micro drilling tests were predicted successfully with the developed two-phase 3D FE model.

5.2 Prediction of the size effect of the microstructure

The validation of the mixture FE model for micro drilling using a drill diameter of $d = 1$ mm is represented in Fig. 7. The predicted values of the feed force and torque with the developed mixture model are in good agreement with the measured results (average deviation about 7% and 3% respectively). On the contrary, the deviation by the isotropic model, which takes no influence of the microstructure, is about 20%, see Fig. 7 (b). A realistic prediction of the chip form was also obtained with the developed 3D multiphase FE model, as illustrated in Fig. 7 (c). Scanning electron microscope (SEM) pictures show micro holes on the deformed chip, see Fig. 7 (c). These holes could be attributed to the size of uncut chip thickness which was on the same order as the harder pearlite grains. This size effect could be reproduced by means of the multiphase FE model, as represented in Fig. 7 (d). In the micro drilling simulation with 1 mm drill, the computed values of the strain rate are in the...
range of 0 to 30,000 1/s and the maximum temperature calculated is about 150 °C.

![Figure 7. FE model validation - chip form in micro drilling C45 with d = 1 mm (r_b = 1 µm).](image)

**5.3 Prediction of size effect of drill micro geometry**

To compare the obtained micro drilling results of this work with earlier macro drilling tests (d = 1 - 3 mm and the same twist geometry) in the normalized steel C45 [23], the related feed force and torque to the cross section of the uncut chip (d•f/2) are plotted versus drill diameters between 50 µm and 3 mm in Fig. 8.

![Figure 8. FE model validation - feed force and torque (r_b = 0.2 µm for d = 100 µm, r_b = 1 µm for d = 1 mm).](image)

A higher increase of the related feed force was observed by down scaling of the drill diameter in the micro range, see Fig. 8. This size effect on the related feed force can be attributed to the exponential growth of the ratio of chisel edge length to drill diameter. The technical qualified increase of the part of the chisel edge of micro drills is to ensure the rigidity and stability of the tool, leading to a significant influence on the micro drilling process reactions. The related torque behaves proportionately to the drill diameter in the micro range like in the case of the conventional macro drilling. The predicted results with the mixture FE drilling model for d = 100 µm are in good agreement with the measured results (average deviation less than 10%, see Fig. 8). On the contrary, the deviation by the isotropic model is up to 30%. In this respect, the developed two-phase FE model for micro drilling can realistically predict the size effect of chisel edge length on the related feed force.

**5.4 Prediction of size effect ploughing in micro drilling**

SEM photographs of deformed chips in micro drilling tests on C45 with drill diameter d = 100 µm indicate a ploughing dominant cutting, as illustrated in Fig. 9 c) and d). For the prediction of this ploughing effect, when micro drilling with drill diameter d = 100 µm, FE computations with the mixture FE model were performed using sharp and rounded cutting edges (r_b = 0 µm and r_b = 0.2 µm). These simulations were made in two successive steps: First, plunging the drill into the workpiece for one half of the feed without drill rotation and second, starting the drilling process.

Figures 9 a) and b) show the computed chip form after one half revolution of the drill when drilling with sharp and rounded cutting edge, respectively. Contrary to the simulation with sharp cutting edge, the deformed chip in front of the rounded main cutting edge became thinner and thinner until it disappeared. During simulation, the used FE program Deform 3D™ deletes elements with very small thickness. This computed effect demonstrates ploughing caused by the small ratio between the uncut chip thickness and cutting edge radius in micro cutting. In the same manner, ploughing effect could also be predicted with the isotropic FE model.

![Figure 9. FE model validation - ploughing in micro drilling C45 with d = 100 µm (v_c = 35 m/min, f = 1.2 µm).](image)
5.5 Micro milling validation tests

The validation of the developed two-phase FE model for micro down milling C45 with different cutting speeds (60, 80 and 100 mm/min) and using a mill diameter of d = 1 mm is shown in Fig. 10. The predicted cutting force components $F_x$ and $F_y$ (maximal values) with the microstructure-based FE model are in good agreement with the measured forces (average deviation about 10%), see Fig. 10 a). The relatively higher deviation of the calculated cutting force component $F_z$ from the measured is due to the rigid body assumption of the micro mill without consideration of wear in the milling simulation. Furthermore, the geometry accuracy of micro mills used is insufficient leading to relatively higher values of the measured force components compared with the computation results.

The decrease of the cutting force with the cutting speed could moreover be reproduced in the simulation of micro milling C45, as illustrated in Fig. 10 a). This decline of the cutting force with the cutting speed is the result of the thermal material softening during cutting. Figures 10 b) and 10 c) show a comparison between the computed and measured chip form exemplarily for micro milling with a cutting speed of 100 m/min. Obviously, a realistic chip formation in micro milling was also predicted by means of the multiphase FE model.

The validation of the FE model is exemplarily for micro milling with a cutting speed of 100 m/min. Figure 10 shows a comparison between the computed and measured chip form.

![Cutting forces](image)

**Figure 10. FE model validation - Cutting force and Chip form in micro down milling C45 with d = 1 mm.**

6 CONCLUSIONS

In the present research work, a microstructure-based 3D FE computation model is developed and successfully validated for micro cutting ferritic-pearlitic carbon steels. Some of the significant findings from this investigation can be summarized as follows:

- The microstructure morphology of carbon steel C45 and its phases ferrite and pearlite is evaluated experimentally
- By means of Split-Hopkinson-Pressure-Bar tests, a constitutive material law has been proposed to describe the thermo-mechanical material behavior at high strain rates
- Two-phase FE material model for steel C45 is developed and successfully validated under different loads
- A microstructure-based 3D FE computation model for micro cutting is worked out and validated for micro drilling and micro milling
- Three size effects identified in micro drilling test were predicted successfully with the developed multi-phase FE model.

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