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Measurements of polarization and spin correlation and observation of entanglement in top quark pairs using lepton+jets events from proton-proton collisions at $\sqrt{s} = 13$ TeV

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Abstract

Measurements of the polarization and spin correlation in top quark pairs ($t\bar{t}$) are presented using events with a single electron or muon and jets in the final state. The measurements are based on proton-proton collision data from the LHC at $\sqrt{s} = 13$ TeV collected by the CMS experiment, corresponding to an integrated luminosity of 138 fb^{-1} . All coefficients of the polarization vectors and the spin correlation matrix are extracted simultaneously by performing a binned likelihood fit to the data. The measurement is performed inclusively and in bins of additional observables, such as the mass of the $t\bar{t}$ system and the top quark scattering angle in the $t\bar{t}$ rest frame. The measured polarization and spin correlation are in agreement with the standard model. From the measured spin correlation, conclusions on the $t\bar{t}$ spin entanglement are drawn by applying the Peres–Horodecki criterion. The standard model predicts entangled spins for $t\bar{t}$ states at the production threshold and at high masses of the $t\bar{t}$ system. Entanglement is observed for the first time in events at high $t\bar{t}$ mass, where a large fraction of the $t\bar{t}$ decays are space-like separated, with an expected and observed significance of above 5 standard deviations.

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1 Introduction

The top quark is the most massive known fundamental particle with a lifetime of the order of 10^{-25} s. This is shorter than the quantum chromodynamics (QCD) hadronization time scale $1/\Lambda_{\text{QCD}} \approx 10^{-24}$ s, and the spin decorrelation time scale $m_t/\Lambda_{\text{QCD}}^2 \approx 10^{-21}$ s, where m_t is the top quark mass [1, 2]. Consequently, the top quark usually decays before hadronization, thus preserving its spin information in the angular distribution of the decay products. This makes top quark and antiquark ($t\bar{t}$) pairs excellent candidates for studying polarization and spin correlation.

We present measurements of the polarization and spin correlation in $t\bar{t}$ pairs using proton-proton collisions at a center-of-mass energy of 13 TeV at the CERN LHC. The measurements are performed using data collected by the CMS detector between 2016 and 2018, corresponding to an integrated luminosity of 138 fb^{-1} . Once produced, a top quark decays via the weak interaction into a W boson and a b quark. The W boson further decays into either two quarks, which subsequently hadronize into jets, or a charged lepton and a neutrino. In this analysis, we focus on the final state with two b jets, two jets from one W boson, and an electron or muon paired with a neutrino from the other W boson. This decay channel is referred to as the e/μ +jets channel. Events with tau leptons are treated as $t\bar{t}$ background and not included in the e/μ +jets category.

At the LHC $t\bar{t}$ pairs are produced through gluon-gluon (gg) fusion and quark-antiquark ($q\bar{q}$) annihilation. The top quarks and antiquarks are unpolarized at leading order (LO). However, their spins are expected to be strongly correlated [3]. The complete spin correlation is encoded in a 3×3 matrix that depends on the $t\bar{t}$ production mechanism, the invariant mass of the $t\bar{t}$ system $m(t\bar{t})$, and the scattering angle of the top quark. Evidence for $t\bar{t}$ spin correlation was first reported by the D0 experiment at the Tevatron in Refs. [4, 5]. The ATLAS and CMS experiments have performed a number of top quark polarization and spin correlation measurements using various observables and data sets [6–15].

The top quark polarization and spin correlation measurement is interesting in its own right as a test of the standard model (SM) [16, 17], but it also provides new opportunities for testing quantum mechanics (QM) at high energies using the decay products of unstable particles as probes. This is not possible in experiments with stable particles, such as electrons and photons. An important prediction of QM is quantum entanglement, which has been studied in connection with particle physics at high energies only in recent years [18–21]. The ATLAS and CMS experiments reported the observation of entanglement in the $t\bar{t}$ system at the production threshold [14, 15] using events where both W bosons from the $t\bar{t}$ pair decay into leptons. In this paper we include measurements of entanglement at the production threshold and at high $m(t\bar{t})$ for $t\bar{t}$ events in the e/μ +jets channel. In [22] it was argued that since collider experiments do not measure spins of the produced particles directly, but rather infer the spin directions statistically from the distribution of their decay products, a local hidden variable theory can always be found that explains the observation. Following [23] we assume that the $t\bar{t}$ system is described by QM and we characterize the state as separable or entangled.

This paper is organized in the following way. First, we outline the measurement strategy in Section 2. We briefly describe the CMS detector in Section 3 and then discuss the signal and background modeling used for this analysis in Section 4. The event selection and the $t\bar{t}$ reconstruction are described in Sections 5 and 6, respectively, followed by a discussion of the background estimation in Section 7 and the extraction of the polarization and spin correlation coefficients in Section 8. Systematic uncertainties are detailed in Section 9. Finally, the results are presented in Section 10 and the paper is summarized in Section 11. Tabulated results are

provided in the HEPData record for this analysis [24].

2 Measurement strategy

We perform a measurement of the $t\bar{t}$ polarization and spin correlation in the helicity basis $\{n, r, k\}$ following Ref. [25]. This basis is defined by boosting the top quarks and their decay products from the laboratory frame into the $t\bar{t}$ rest frame. Afterward, based on the unit vectors in the top quark direction $\hat{k}$ and the beam in the positive z -direction $\hat{b}$, the axes of the new coordinate system are given by

$$\hat{n} = \frac{\hat{b} \times \hat{k}}{\sin(\theta)}, \quad \hat{r} = \frac{\hat{b} - \cos(\theta)\hat{k}}{\sin(\theta)}, \quad \hat{k}, \quad (1)$$

where θ is the scattering angle of the top quark, i.e., $\cos(\theta) = \hat{b} \cdot \hat{k}$. The Bose–Einstein symmetry of the gg initial state [25] requires a redefinition of the n and r axes (which are odd under Bose–Einstein symmetry) to allow nonzero values of the polarization and spin correlation coefficients involving an odd number of these axes. This is done by multiplying the n and r directions by the sign of $\cos(\theta)$, which is also odd under Bose–Einstein symmetry, such that all axes are even under Bose–Einstein symmetry:

$$\{n, r, k\} \rightarrow \{\text{sgn}(\cos(\theta))n, \text{sgn}(\cos(\theta))r, k\}. \quad (2)$$

Finally, the top quark and antiquark are boosted individually into their rest frames together with their corresponding decay products.

In this basis, the unit vector

$$\Omega(\bar{\Omega}) = (\sin(\theta_{p(\bar{p})})\cos(\phi_{p(\bar{p})}), \sin(\theta_{p(\bar{p})})\sin(\phi_{p(\bar{p})}), \cos(\theta_{p(\bar{p})})) \quad (3)$$

describes the direction of a decay product $p(\bar{p})$ of the top (anti)quark, where $\phi_{p(\bar{p})}$ is the azimuthal and $\theta_{p(\bar{p})}$ the polar angle of the decay product. The differential cross section as a function of the four variables $\phi_{p(\bar{p})}$ and $\theta_{p(\bar{p})}$ has the form

$$\begin{aligned} \Sigma_{\text{tot}}(\phi_{p(\bar{p})}, \theta_{p(\bar{p})}) &= \frac{d^4\sigma}{d\phi_p d\cos(\theta_p) d\phi_{\bar{p}} d\cos(\theta_{\bar{p}})} \\ &= \sigma_{\text{norm}}(1 + \kappa \mathbf{P} \cdot \Omega + \bar{\kappa} \bar{\mathbf{P}} \cdot \bar{\Omega} - \kappa \bar{\kappa} \Omega \cdot (C\bar{\Omega})), \end{aligned} \quad (4)$$

with two 3-dimensional polarization vectors $\mathbf{P}$ and $\bar{\mathbf{P}}$, and one 3×3 spin correlation matrix C . This means that Σ_{tot} depends linearly on 15 coefficients collectively referred to as $Q_m = \{P_n, P_r, P_k, \bar{P}_n, \dots, C_{nn}, C_{nr}, \dots, C_{kk}\}$. In this analysis, we perform a measurement of all 15 coefficients, which we subsequently refer to as the full matrix measurement. There is one additional coefficient σ_{norm} that describes the overall normalization. The spin analyzing power κ represents how much information from the top quark spin is transferred to its decay products. We use the down-type quarks and the charged leptons in the W boson decays. The magnitude of κ for these decay products have the maximum value of unity at LO. Including QCD corrections, the magnitude of κ for down-type quarks is reduced to 0.966 [26]. However, we perform the measurements using the LO values and leave the application of different κ values for reinterpretations. For simplicity, we flip the sign of κ for $\bar{t}$ decays following the convention of Ref. [3], instead of inverting the axes of the coordinate system as in Refs. [15, 25].

The top quark, being a spin-1/2 particle, can be described as a two-state quantum system known as a qubit. The minimal example of an entangled state consists of two qubits, e.g.,

a $t\bar{t}$ pair, where the entanglement can be characterized by their spin correlation. The Peres–Horodecki criterion [27, 28] can be used to determine if a quantum state is separable. If the state is not separable, it is considered entangled. In general, a quantum state is described by a density matrix ρ , in this case a spin density matrix whose coefficients are probed by Eq. (4). A quantum state is said to be separable if ρ can be factorized into individual states belonging to separate subspaces, i.e., $\rho = \sum_n q_n \rho_n^a \otimes \rho_n^b$, where ρ_n^a, ρ_n^b are density matrices describing the quantum states of the subsystems a and b and the q_n are the corresponding probabilities. If ρ is a separable physical state, the state $\rho^{T_2} = \sum_n q_n \rho_n^a \otimes (\rho_n^b)^T$ resulting from taking the transpose for only subsystem b should also be a physical state. It was demonstrated [27, 28] that a sufficient condition for entanglement is that ρ^{T_2} has at least one negative eigenvalue, meaning it is not a physical state. This translates to a sufficient condition for entanglement based on the diagonal elements of the spin correlation matrix [18, 29]:

$$\Delta_E = C_{nn} + |C_{rr} + C_{kk}| > 1. \quad (5)$$

Based on the measured values of the spin correlation matrix we apply this criterion to evaluate the entanglement of the $t\bar{t}$ system in different regions of phase space.

As an alternative to the full matrix measurement, we measure angular variables directly sensitive to Δ_E . The trace of the spin correlation matrix $\text{Tr}(C)$ can be probed using the opening angle χ between the two decay products in the helicity basis, $\cos(\chi) = \mathbf{\Omega} \cdot \bar{\mathbf{\Omega}}$. This observable is sensitive to the entanglement in the spin-singlet state [18] expected from gg fusion events at the $t\bar{t}$ production threshold. The distribution of χ is given by

$$\frac{d\sigma}{d\cos(\chi)} = \sigma_{\text{norm}}(1 + D\kappa\bar{\kappa}\cos(\chi)), \text{ where } D = -\frac{1}{3}\text{Tr}(C). \quad (6)$$

For gg fusion events at low $m(t\bar{t})$, both C_{rr} and C_{kk} are positive [3], which simplifies the entanglement criterion to

$$\Delta_E = -3D = \text{Tr}(C) > 1. \quad (7)$$

The entanglement in a spin-triplet state, predicted in both $q\bar{q}$ annihilation and gg fusion events with high $m(t\bar{t})$ and low $|\cos(\theta)|$, can be probed using a criterion based on [3, 30]

$$\tilde{D} = \frac{1}{3}(C_{nn} - C_{rr} - C_{kk}). \quad (8)$$

The signs of C_{rr} and C_{kk} become negative at transverse momentum of the top quark $p_T(t) \sim m_t$ [3], so the entanglement criterion based on $\tilde{D}$ in the high- $m(t\bar{t})$ region is:

$$\Delta_E = 3\tilde{D} > 1. \quad (9)$$

The extraction of $\tilde{D}$ is performed using $\tilde{\chi} = -\Omega_n\bar{\Omega}_n + \Omega_r\bar{\Omega}_r + \Omega_k\bar{\Omega}_k$, analogous to χ but with an inverted sign of the n -component of one of the decay products.

3 The CMS detector

The central feature of the CMS apparatus is a superconducting solenoid of 6 m internal diameter, providing a magnetic field of 3.8 T. Within the solenoid volume are a silicon pixel and strip tracker, a lead tungstate crystal electromagnetic calorimeter (ECAL), and a brass and scintillator hadron calorimeter (HCAL), each composed of a barrel and two endcap sections. Forward

calorimeters extend the pseudorapidity (η) coverage provided by the barrel and endcap detectors. Muons are measured in gas-ionization detectors embedded in the steel flux-return yoke outside the solenoid.

Events of interest are selected using a two-tiered trigger system. The first level (L1), composed of custom hardware processors, uses information from the calorimeters and muon detectors to select events at a rate of around 100 kHz within a fixed latency of about $4\ \mu\text{s}$ [31]. The second level, known as the high-level trigger, consists of a farm of processors running a version of the full event reconstruction software optimized for fast processing, and reduces the event rate to around 1 kHz before data storage [32]. For this measurement events are selected using single electron and muon triggers for isolated leptons with minimum p_T requirements, depending on the year, of 24 and 27 GeV for muons and 27 and 32 GeV for electrons.

The primary vertex is taken to be the vertex corresponding to the hardest scattering in the event, evaluated using tracking information alone, as described in Section 9.4.1 of Ref. [33]. The particle-flow (PF) algorithm [34] aims to reconstruct and identify each individual particle in an event, with an optimized combination of information from various elements of the CMS detector. The energy of photons is obtained from the ECAL measurement. The energy of electrons is determined from a combination of the electron momentum at the primary interaction vertex as determined by the tracker, the energy of the corresponding ECAL cluster, and the energy sum of all bremsstrahlung photons spatially compatible with originating from the electron track. The energy of muons is obtained from the curvature of the corresponding track. The energy of charged hadrons is determined from a combination of their momentum measured in the tracker and the matching ECAL and HCAL energy deposits, corrected for the response function of the calorimeters to hadronic showers. Finally, the energy of neutral hadrons is obtained from the corresponding corrected ECAL and HCAL energies. A more detailed description of the CMS detector, together with a definition of the coordinate system used and the relevant kinematic variables, can be found in Ref. [35].

4 Signal and background modeling

The matrix element (ME) event generator POWHEG v2 [36–38] is used to simulate $t\bar{t}$ events with next-to-LO (NLO) QCD accuracy. It is subsequently combined with the parton shower (PS) simulation from PYTHIA 8.230 [39], using the underlying event tune CP5 [40]. In addition, a sample of $t\bar{t}$ production at next-to-NLO (NNLO) QCD is generated with POWHEG MINNLO [41] in combination with the CP5 PYTHIA tune. This is used to estimate uncertainties in the contribution from higher-order QCD. Similarly, for the estimation of electroweak corrections, we use the HATHOR 2.1-B3 package [42]. The measured coefficients are compared to the predictions obtained using POWHEG+HERWIG 7.1 [43] with tune CH3 [44] and MADGRAPH5_aMC@NLO 2.6.1 [45] combining ME calculations at NLO QCD including up to two additional partons with the PYTHIA PS using the FFX algorithm [46]. In all $t\bar{t}$ simulations, the decays of the top quarks including the spin correlation are evaluated at LO precision.

The $t\bar{t}$ simulations are normalized to the inclusive cross section value of $832^{+40}_{-46}\ \text{pb}$ [47] which is calculated with NNLO precision including soft-gluon resummation at the level of next-to-next-to-leading-logarithm. The renormalization scale μ_r and factorization scale μ_f are taken to be equal to the average transverse mass of the top quark and antiquark, $m_T = 0.5(\sqrt{m_t^2 + p_T(t)^2} + \sqrt{m_{\bar{t}}^2 + p_T(\bar{t})^2})$, where p_T is the transverse momentum of the top quark evaluated in the $t\bar{t}$ rest frame, and $m_t = 172.5\ \text{GeV}$ [48] is used in all simulations, unless stated otherwise. The main background processes in this analysis are single top quark production, Drell–Yan (DY) and

W boson production in association with jets, and events composed uniquely of jets produced through the strong interaction, referred to as QCD multijet events. Single top quark production via t channel and top quark production in association with a W boson are generated using POWHEG+PYTHIA, while the production via s channel is generated at NLO QCD using MADGRAPH5_aMC@NLO+PYTHIA. The simulation of background from DY+jets and W+jets production is performed at LO QCD using MADGRAPH5_aMC@NLO+PYTHIA with the MLM PS matching [49, 50] of up to four partons. The QCD multijet processes are simulated at LO using PYTHIA. The cross sections are taken from NNLO calculations for W+jets and DY+jets events [51] and NLO calculations for single top quark events [52, 53]. The default parameterization of the parton distribution functions (PDFs) used in all simulations is the NNLO version of NNPDF 3.1 [54].

The detector response is modeled using GEANT4 [55]. Additional proton-proton interactions within the same or nearby bunch crossings (pileup) are overlaid on each simulated event. Simulated events are assigned event weights based on the number of pileup interactions to match the pileup distribution in data. The same reconstruction algorithms that are applied to the data are used for simulated events.

5 Physics object reconstruction

The measurements presented in this analysis depend on the reconstruction and identification of electrons, muons, jets, and the missing transverse momentum $\vec{p}_T^{\text{miss}}$ associated with neutrinos.

Electrons [56] and muons [57] are selected if they are isolated and compatible with originating from the primary vertex. Moreover, they must have $p_T > 30 \text{ GeV}$ and $|\eta| < 2.4$. In the 2018 data set, the minimum p_T of electrons was raised to 34 GeV because of the increased trigger thresholds. Leptons are required to satisfy several quality criteria including isolation and compatibility with the primary vertex. The electron and muon reconstruction and selection efficiencies are measured in the data using the “tag-and-probe” technique [58]. Depending on p_T and η , the overall reconstruction and selection efficiency is 50–80% for electrons and 75–85% for muons.

Jets are clustered from PF candidates using the anti- k_T jet algorithm with a distance parameter of 0.4 implemented in the FASTJET package [59, 60]. Charged PF candidates originating from a pileup interaction vertex are excluded. The total energy of the jets is corrected for energy depositions from pileup. In addition, p_T - and η -dependent corrections are applied to account for detector response effects [61]. If an isolated lepton with $p_T > 15 \text{ GeV}$ within $\Delta R = \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2} = 0.4$ around a jet exists, the jet is assumed to represent the isolated lepton and is discarded to prevent counting the lepton momentum twice. The jets are considered for analysis if they fulfill the kinematic requirements $p_T > 30 \text{ GeV}$ and $|\eta| < 2.4$.

For the identification of b jets, the DeepJet algorithm [62, 63] is used. It is based on an artificial neural network (NN) that provides a discriminant to distinguish between b and other flavored jets. Jets are categorized based on three thresholds of the discriminant and a jet belongs to the category with the highest threshold that is smaller than that jet’s discriminant value. The tight, medium, and loose thresholds have, depending on the jet p_T and η , efficiencies of about 50–70, 70–82, and 85–92%, respectively, and rejection probabilities of about 97, 85, and 55% for c jets and about 99.5, 98, and 90% for non-heavy-flavor jets.

The missing transverse momentum vector $\vec{p}_T^{\text{miss}}$ is computed as the negative vector sum of the transverse momenta of all the PF candidates in an event, and its magnitude is denoted as

p_T^{miss} [64]. The $\vec{p}_T^{\text{miss}}$ is modified to account for corrections to the energy scale of the reconstructed jets in the event.

The data was recorded in the years 2016–2018. For each year individual sets of simulations and correction factors are used according to the actual data-taking conditions and detector configurations. Because of significant changes in the detector configuration affecting the tracking efficiency, two separate sets of simulations and scale factors are used for 2016 data. Therefore, four different data-taking periods are analyzed.

6 Event reconstruction

The reconstruction of the $t\bar{t}$ system is performed using an artificial NN. The goal is the correct identification of detector-level objects as decay products of the leptonically (t_ℓ) and hadronically (t_h) decaying top quarks in e/μ +jets events. In the simulation, a quark or lepton at the generator level can be spatially matched to the corresponding detector-level object. Of the possible candidates, we select the highest p_T object within $\Delta R = 0.2$. If a one-to-one assignment to a corresponding detector-level object is possible for all of the particles in the generator-level $t\bar{t}$ system, the event is labeled “reconstructable”, while all other e/μ +jets events are called “nonreconstructable”.

The input layer of the NN is a vector encoding kinematical information about the detector-level objects and b tagging category for jets. The first four elements of the vector hold the four-momentum of the electron or muon ($p_x(\ell)$, $p_y(\ell)$, $p_z(\ell)$, $E(\ell)$), followed by (p_x^{miss} , p_y^{miss}). Finally, for up to eight jets the four-momentum and their b tagging category (p_x , p_y , p_z , E , b cat.) are stored. The NN is trained to assume the following order of the jets: the b jet in the decay of t_ℓ , the b jet in the decay of t_h , the down-type, and the up-type quark in the W boson decay. The remaining jets are added in descending order of their p_T . If there are fewer than eight jets, the rest of the input vector is filled with zeros. The b tagging information also helps to identify c jets from W boson decays, since 40–50% of the c jets are loosely b tagged. The input layer is followed by seven fully connected layers, each with 220 nodes and the hyperbolic tangent as the activation function. The output layer consists of a single node whose value is transformed by a sigmoid function into the range $[0, 1]$. In total, the network has about 300 000 parameters.

The NN is trained using about 20M simulated e/μ +jets events. Events with one selected electron or muon, no additional isolated electron or muon with $p_T > 15$ GeV, and at least four jets are used. The NN is trained using a batch size of 128 events and the ADAM algorithm [65] for the minimization of the logistic loss function. For each event in a batch, the network is provided with all possible permutations for the four jets from the $t\bar{t}$ decay using up to eight jets per event, i.e., for 4 (5, 6, 7, 8) jets the training includes 24 (120, 360, 840, 1680) input vectors. Correct permutations are trained to have a response of one, while all other permutations should result in zero. The training sample includes “nonreconstructable” events, i.e., those with no correct permutation. During the training, the logistic loss function is monitored with a validation sample. The losses for the training and validation samples are compatible and no indication of overtraining is observed. During the inference, for each event, all possible permutations of assigning detector-level jets to the corresponding $t\bar{t}$ decay products are successively provided as input to the NN and the permutation resulting in the highest NN score S_{NN} is used.

For the selected permutation, the neutrino four-momentum p_ν is calculated using the W boson mass constraint $(p_\nu + p_\ell)^2 = m_W^2$, where $\vec{p}_T^{\text{miss}}$ is taken as the p_T of the neutrino. This constraint results in a quadratic equation for the longitudinal component of the neutrino momentum $p_z(\nu)$. In the 39.1% of events where this equation yields no real solution, the x and

y components of $\vec{p}_T^{\text{miss}}$ are scaled separately to find a single solution under the condition of a minimum modification of p_T^{miss} , i.e., in the transverse plane we choose the point with the smallest distance from $\vec{p}_T^{\text{miss}}$ for which a solution exists. This modified $\vec{p}_T^{\text{miss}}$ together with the calculated solution for $p_z(\nu)$ form the neutrino momentum. If there are two solutions of the quadratic equation, the invariant mass $m(t_\ell)^2 = (p_\nu + p_\ell + p_{b_\ell})^2$ is calculated for both p_ν and the solution with $m(t_\ell)$ closer to m_t is selected. This procedure identifies the correct solution in 69.9% of the events. To enhance the fraction of correctly reconstructed events and reduce the background contribution, event selection requirements on the reconstructed particle masses $|m(t_\ell) - 172.5 \text{ GeV}| < 50 \text{ GeV}$, $|m(t_h) - 172.5 \text{ GeV}| < 50 \text{ GeV}$, and $|m(W_h) - 80.4 \text{ GeV}| < 30 \text{ GeV}$ are imposed.

The distributions of S_{NN} are shown in Fig. 1 for events in categories where either both (2b) or exactly one (1b) of the jets identified as b jets from the $t\bar{t}$ decay are medium b tagged. In these distributions, it can be seen that the data and the prediction are in agreement within the uncertainty bands. We reject all events with $S_{\text{NN}} < 0.1$ due to the low fraction of correctly reconstructed events and the large contribution of background processes.

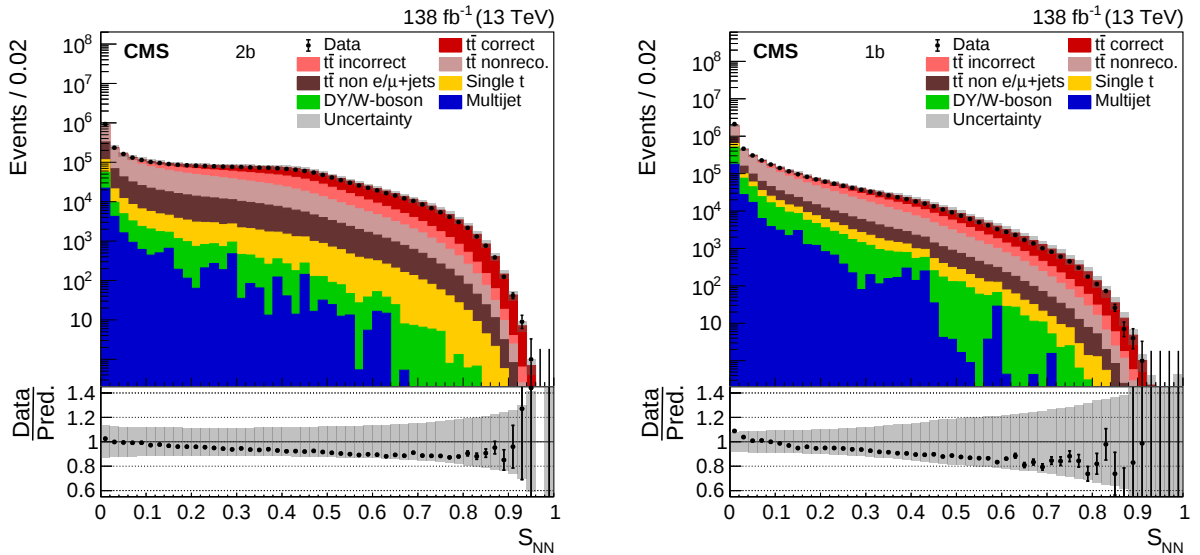


Figure 1: Distribution of S_{NN} in the 2b (left) and 1b (right) categories. The data (points) are compared to the prediction (stacked histograms). The $t\bar{t}$ contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/μ +jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction, while the vertical bars on the points show the statistical uncertainty of the data. The ratios of data to the predicted yields are provided in the lower panels.

The 2b and 1b categories are further split based on the value of S_{NN} . In the 1b (2b) category events belong to the S_{high} category if $S_{\text{NN}} > 0.30$ (0.36), while the remaining events are placed in the S_{low} category. These requirements define the signal categories for the analysis and were systematically optimized to minimize the uncertainties in the expected spin polarization and correlation coefficients.

In the simulation, the fraction of reconstructable e/μ +jets events is 73% for 2b S_{high} , 47% for 2b S_{low} , 64% for 1b S_{high} , and 38% for 1b S_{low} . The fractions of correctly reconstructed events with respect to all signal and background events in the various categories are 46% for 2b S_{high} , 21% for 2b S_{low} , 37% for 1b S_{high} , and 15% for 1b S_{low} . Figure 2 shows these fractions as functions of $m(t\bar{t})$ together with the fraction of correctly reconstructed events with respect to all

reconstructable events.

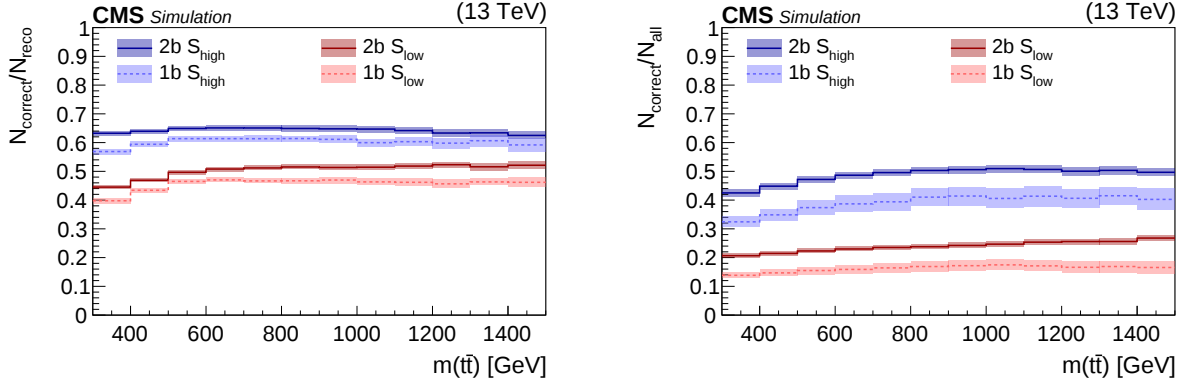


Figure 2: Reconstruction efficiency of the NN (left) and the fraction of correctly reconstructed events (right) as a function of $m(t\bar{t})$ estimated from the simulation. The values are shown separately for the 1b and 2b categories with the S_{low} and S_{high} selections. The event counts N_{correct} and N_{reco} refer to the number of correctly reconstructed and “reconstructable” $t\bar{t}$ events, respectively. All reconstructed events regardless of the process are labeled N_{all} . The uncertainty bands include all systematic uncertainties as detailed in Section 9.

7 Background estimation

The main background contributions of non- $t\bar{t}$ events are expected from QCD multijet, DY, W boson, and single top quark production.

The shapes of the QCD multijet (multijet), and DY and W boson (EW) background distributions are estimated using a combined template of these backgrounds that is obtained from a b-jet depleted control region (CR). The simulation of these backgrounds suffers from large statistical uncertainties due to their high cross sections but low fraction of events that pass the selection. They contribute fractions of about 6.6% (1b S_{low}), 2.4% (1b S_{high}), 1.1% (2b S_{low}), and 0.2% (2b S_{high}), i.e., the contribution in the 2b categories is negligible. The shape of the background distribution is estimated by performing the NN reconstruction for events without any jet fulfilling the medium b tagging requirement. No selections on S_{NN} are applied, but the mass ranges of t_ℓ , t_h , and the W_h boson are required as introduced in Section 6. These selection requirements define the CR. The expected contributions of $t\bar{t}$ and single top quark events are subtracted from the data in the CR. The simulated kinematic distributions obtained in the CR are generally in agreement with the simulated distributions in the signal categories, as shown for the 1b signal category in Fig. 3.

As systematic uncertainties in the background template shapes, we evaluate shape differences between the CR and the signal categories. The definition of the CR is inclusive in S_{NN} . This choice has the advantage of maximizing the number of events in the CR while minimizing the contribution from $t\bar{t}$ events. We obtain alternative shapes from additional control regions, where the S_{low} or S_{high} requirement of the corresponding signal category is also imposed. While it is expected that these distributions are more similar to the real background, they suffer from a small sample of events and large $t\bar{t}$ contributions. Therefore, they are only used to evaluate the uncertainty in the background templates.

In the CR, there is an excess of about 20% in data. This excess is within the uncertainty in the simulated event yield. However, to take into account a possible underestimation of $t\bar{t}$

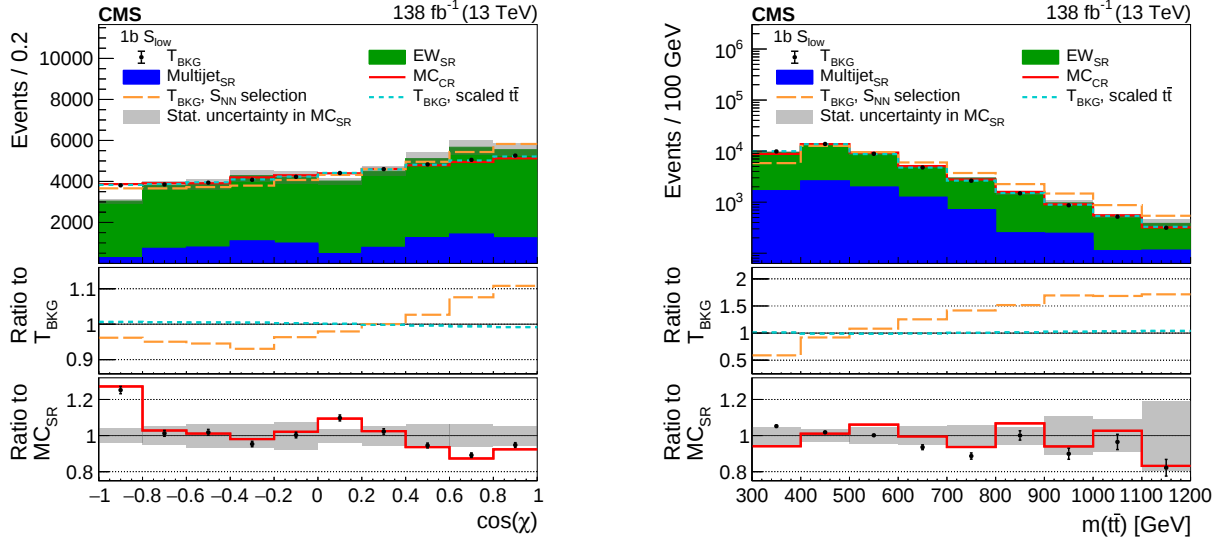


Figure 3: Comparison of the $\cos(\chi)$ (left) and $m(t\bar{t})$ (right) distributions of the simulated background in the control region (MC_{CR}) shown as the red line, and in the $1b S_{low}$ signal region (MC_{SR}) shown as the stacked histograms of the multijet and EW components. The estimated background template (T_{BKG}) shown as black markers corresponds to the data distribution in the CR after subtracting the predicted $t\bar{t}$ and single top quark contributions. Variations of the T_{BKG} are obtained applying the additional S_{NN} selection for the $1b S_{low}$ category (orange line) and by taking into account the mismatch of the normalization in the CR when subtracting the $t\bar{t}$ and single top quark contributions (blue line). All distributions are normalized to the event yields predicted by the MC_{SR} . The gray uncertainty band shows the statistical uncertainties in the MC_{SR} . The middle panels show the relative effects of the T_{BKG} variations. The lower panels show the ratio of the MC_{CR} and the T_{BKG} to the MC_{SR} .

production in the CR, an additional systematic uncertainty in the shape is obtained by scaling the amount of subtracted $t\bar{t}$ and single top quark events by the ratio of the total observed and simulated event yields in the CR, shown as the dashed light blue lines in Fig. 3.

The predicted ratio of the multijet and EW event yield (multijet+EW) in each signal category to the corresponding CR is applied to normalize the background templates. This normalization factor has a large statistical uncertainty due to the limited number of simulated events in the signal categories. In addition, the observed differences between the predicted and observed event yields in the CR are considered as a systematic uncertainty in the normalization of the background. As a result, the normalization uncertainties can be as large as 50%, depending on the category.

The obtained background predictions with their shape and normalization uncertainties are included in the fits of spin polarization and correlation coefficients, as described in Section 8. The normalization uncertainties are treated as uncorrelated among all categories, because of their large statistical component from the simulation. The shape uncertainties are considered as uncorrelated among the categories to account for differences in their selection. In addition, the uncertainties are assumed uncorrelated among the data-taking periods, because of the differences in the b tagging performances and selections. It has been verified that the results of the analysis are not sensitive to these assumptions.

The contribution of single top quark production is about 4.0% ($1b S_{low}$), 2.2% ($1b S_{high}$), 2.4% ($2b S_{low}$), and 1.4% ($2b S_{high}$). Templates according to their SM expectation are taken from the simulation. We evaluate the relevant uncertainties in these templates (as described in Section 9):

ME and PS scales, jet resolution and energy scales, and b tagging and lepton efficiencies. The ME scale uncertainties are treated independently from the corresponding variations of the $t\bar{t}$ simulation.

In Figs. 4–9, the distributions of several observables in all signal categories are shown with the multijet+EW background estimation taken from the CR. The uncertainty bands include statistical uncertainties and all systematic uncertainties detailed in Section 9, and are in general dominated by uncertainties in the jet energy scale, the b tagging efficiencies, PS modeling, and ME scales, with the latter contributing the largest uncertainty in the overall normalization.

8 Extraction of polarization and spin correlation coefficients

Following the formalism introduced in Eq. (4), the differential cross section Σ_{tot} can be written as a linear combination of functions Σ_m , which depend on the angles $\phi_{p(\bar{p})}$ and $\theta_{p(\bar{p})}$ of the decay products of the top quark and antiquark:

$$\Sigma_{\text{tot}} = \Sigma_0 + \sum_{m=1}^{15} Q_m \Sigma_m. \quad (10)$$

The spin analyzing powers κ and the cross section σ_{norm} are absorbed in the definitions of the functions Σ_m .

The values of the coefficients Q_m can be extracted by fitting Σ_{tot} with Eq. (10). This approach is used at the generator level to obtain the Q_m^{MC} —the polarization and spin correlation of the partonic top quarks as predicted by each of the $t\bar{t}$ simulations and their uncertainty variations. These fits are performed in bins of the additional observables $m(t\bar{t})$ vs. $|\cos(\theta)|$ and $p_T(t)$ vs. $|\cos(\theta)|$. A binning in $m(t\bar{t})$ of $\{300, 400, 600, 800, 13000\}$ GeV with the first $m(t\bar{t})$ bin including a few underflow events, and in $p_T(t)$ of $\{0, 100, 200, 300, 6500\}$ GeV is used. In both cases the bins are further divided into $|\cos(\theta)|$ bins with the boundaries $\{0, 0.4, 0.7, 1\}$. As a result we obtain the average values of the Q_m^{MC} in each of these bins. The knowledge of the Q_m^{MC} facilitates the analytical calculation of $\Sigma_{\text{tot}}^{\text{MC}}$ as a function of $\phi_{p(\bar{p})}$ and $\theta_{p(\bar{p})}$ in each bin of the additional observables.

For the measurement of the Q_m , we are interested in templates T_m that can be fit to the data and describe only the effect of the corresponding coefficient. At the generator level, these templates are $L\Sigma_m$, where L is the integrated luminosity. Accordingly, the T_m are the corresponding distributions of events at the detector level in the signal categories. The binnings at the generator and the detector levels are the same. The T_m include all $t\bar{t}$ events selected at the detector level, meaning that they describe polarization and spin correlation effects of e/μ +jets and $t\bar{t}$ background events, also referred as $t\bar{t}$ non e/μ +jets. To avoid the full simulation of $t\bar{t}$ samples for each Q_m we use a reweighting technique to evaluate the T_m . For this, each event is assigned a weight equal to $\Sigma_m/\Sigma_{\text{tot}}^{\text{MC}}$, which are evaluated for each event based on the generator-level values of $\theta_{p(\bar{p})}$, $\phi_{p(\bar{p})}$, and the bin determined by the additional observables $m(t\bar{t})$ vs. $|\cos(\theta)|$ or $p_T(t)$ vs. $|\cos(\theta)|$. In this bin we know the average value of the Q_m^{MC} , as determined from the fits of the Σ_m at the generator level. The generator-level Σ_m and the T_m for the 2b S_{high} category at the detector level are shown in Fig. 10. Here, the x axis shows the bin number of the unrolled 4-dimensional distribution of $\phi_{\bar{p}}$, $\cos(\theta_{\bar{p}})$, ϕ_p , and $\cos(\theta_p)$, listed from the outermost to the innermost variable, where $\cos(\theta_{p(\bar{p})})$ uses two bins: $\{-1, 0, 1\}$, and $\phi_{p(\bar{p})}$ is divided into four bins: $\{-\pi, -\pi/2, 0, \pi/2, \pi\}$, resulting in a total number of 64 bins.

In general, the Q_m are not constant within a bin. At the generator level, the functions Σ_m do not depend on the kinematic properties of the top quarks, so they factorize and the average

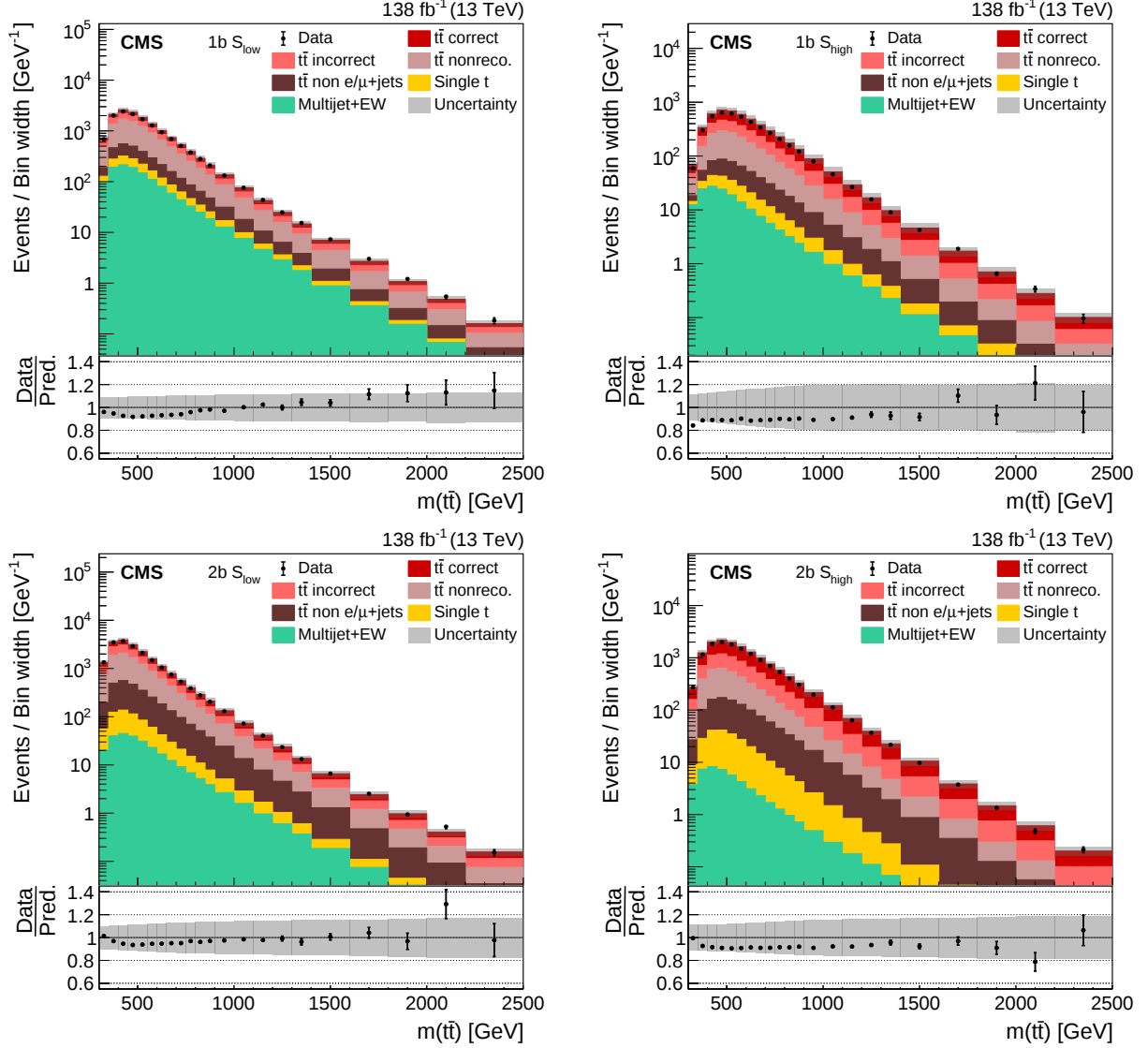


Figure 4: Distribution of $m(t\bar{t})$ in all four categories. The data (points) are compared to the prediction (stacked histograms). The $t\bar{t}$ and single top quark contributions are taken from the simulation, while the multijet+EW background is obtained from the CR. The $t\bar{t}$ contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/μ+jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty of the data. Ratios to the predicted yields are provided in the lower panels.

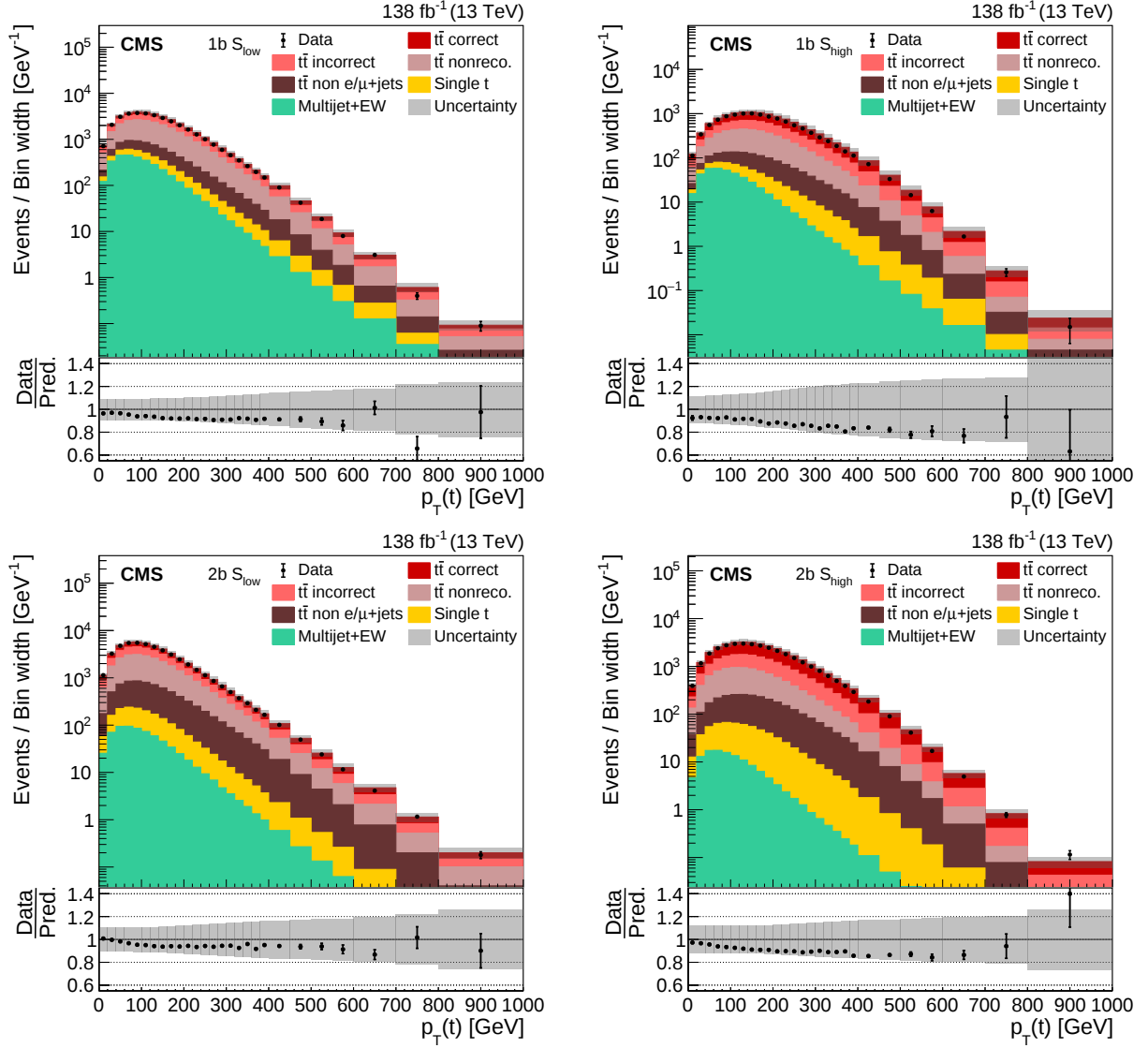


Figure 5: Distribution of $p_T(t)$ in all four categories. The data (points) are compared to the prediction (stacked histograms). The $t\bar{t}$ and single top quark contributions are taken from the simulation, while the multijet+EW background is obtained from the CR. The $t\bar{t}$ contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/μ +jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty of the data. Ratios to the predicted yields are provided in the lower panels.

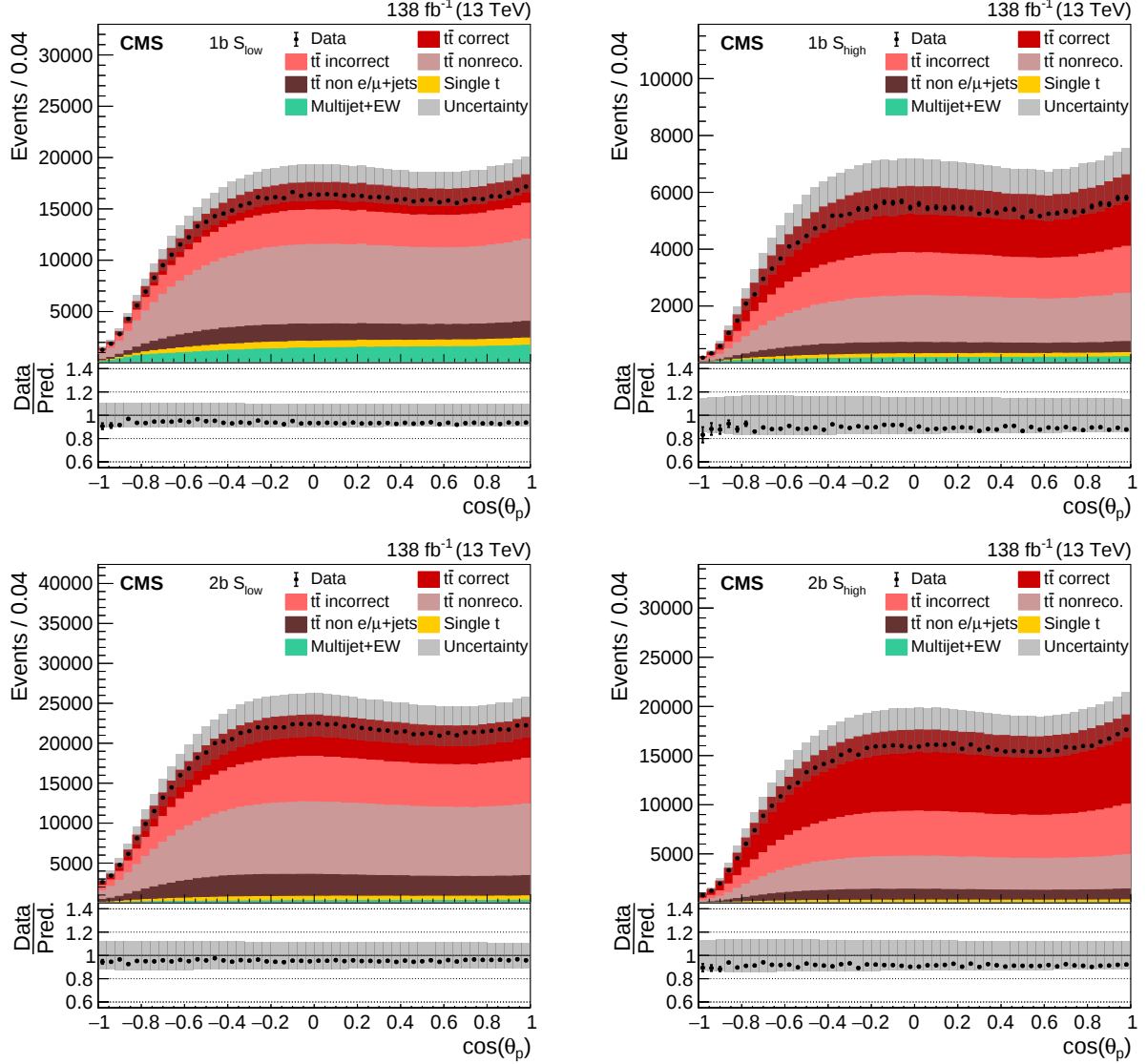


Figure 6: Distribution of $\cos(\theta_p)$ in all four categories. The data (points) are compared to the prediction (stacked histograms). The $t\bar{t}$ and single top quark contributions are taken from the simulation, while the multijet+EW background is obtained from the CR. The $t\bar{t}$ contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/μ +jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty of the data. Ratios to the predicted yields are provided in the lower panels.

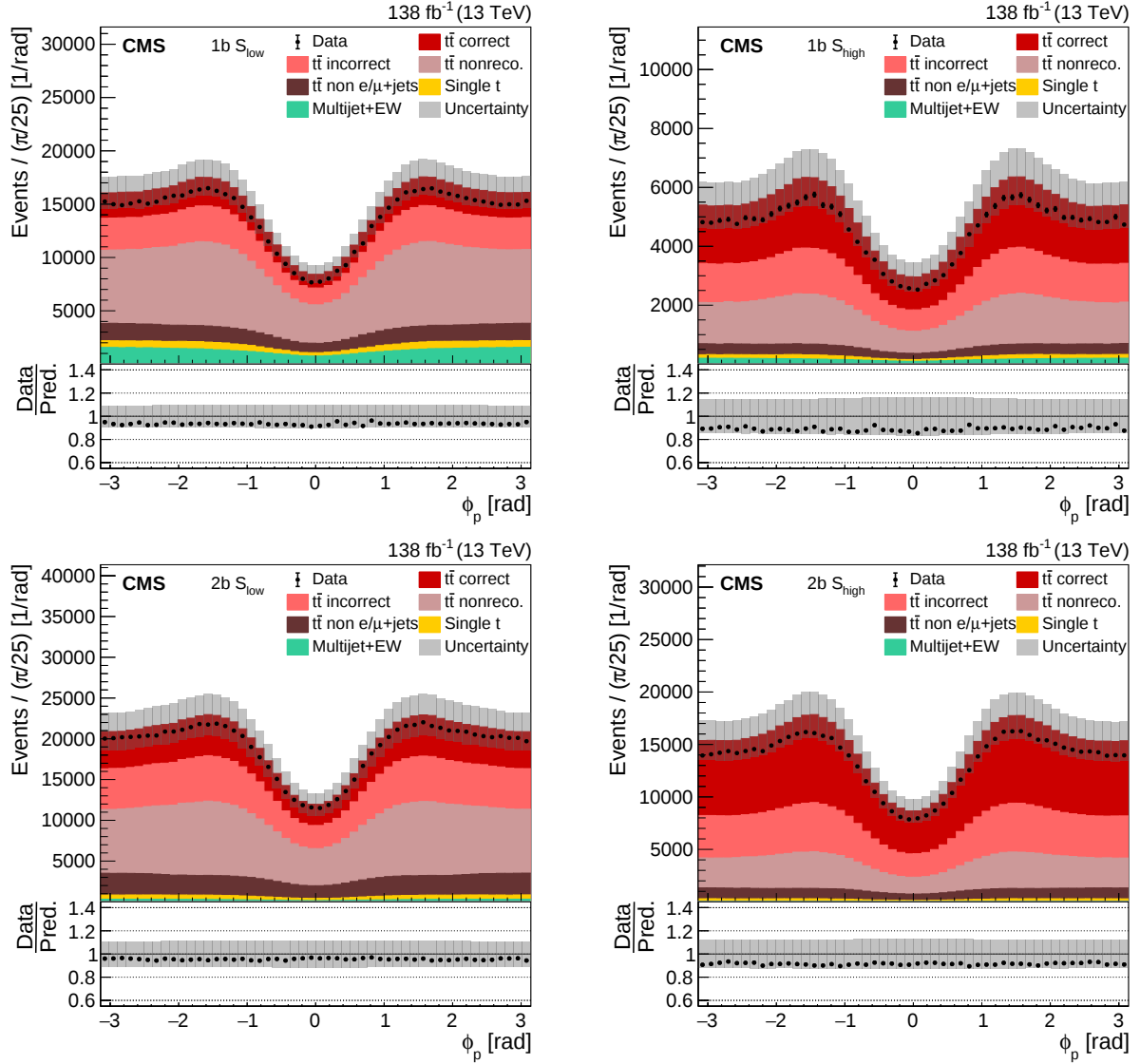


Figure 7: Distribution of ϕ_p in all four categories. The data (points) are compared to the prediction (stacked histograms). The $t\bar{t}$ and single top quark contributions are taken from the simulation, while the multijet+EW background is obtained from the CR. The $t\bar{t}$ contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/ μ +jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty of the data. Ratios to the predicted yields are provided in the lower panels.

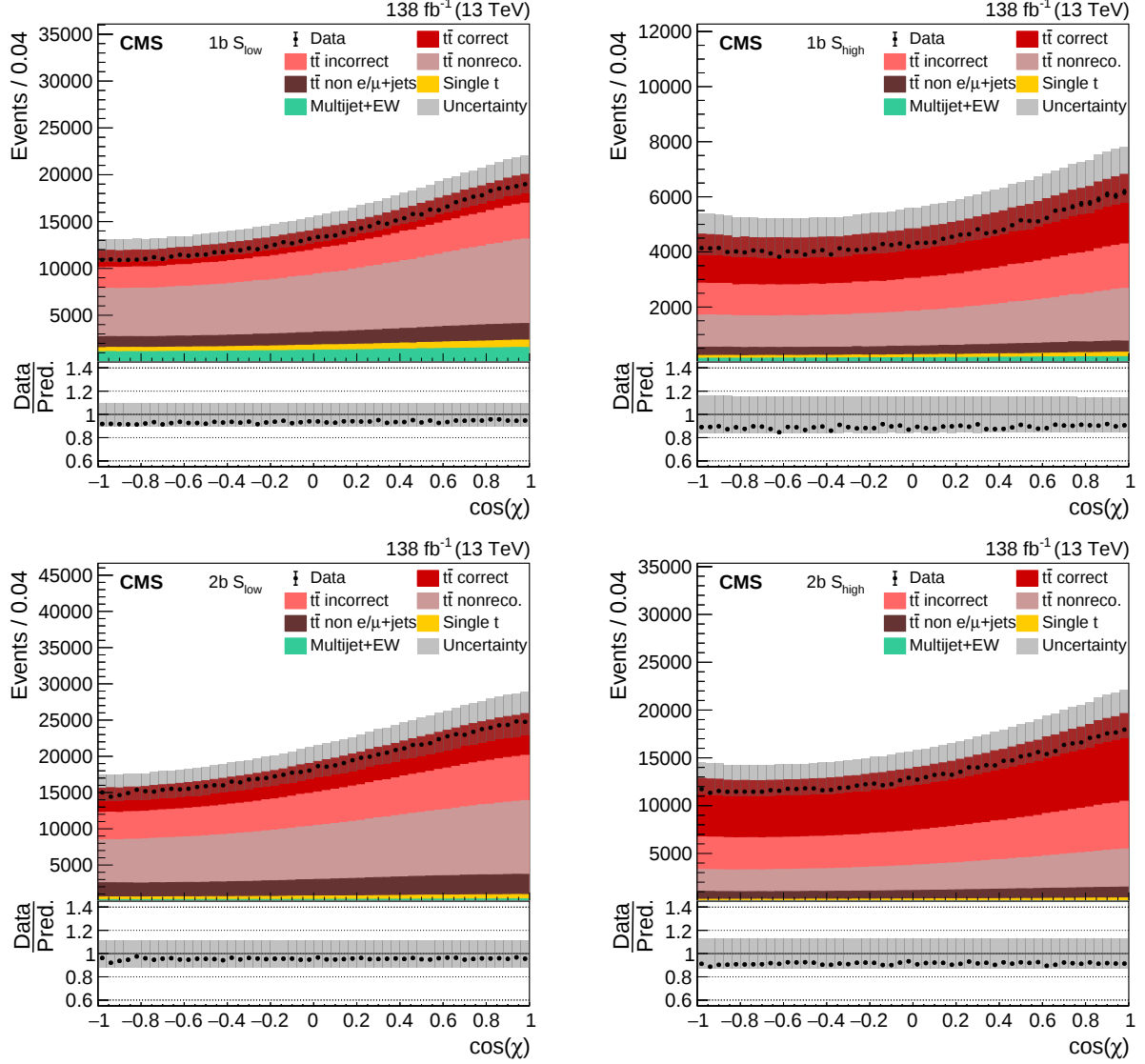


Figure 8: Distribution of $\cos(\chi)$ in all four categories. The data (points) are compared to the prediction (stacked histograms). The tt and single top quark contributions are taken from the simulation, while the multijet+EW background is obtained from the CR. The tt contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/μ +jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty of the data. Ratios to the predicted yields are provided in the lower panels.

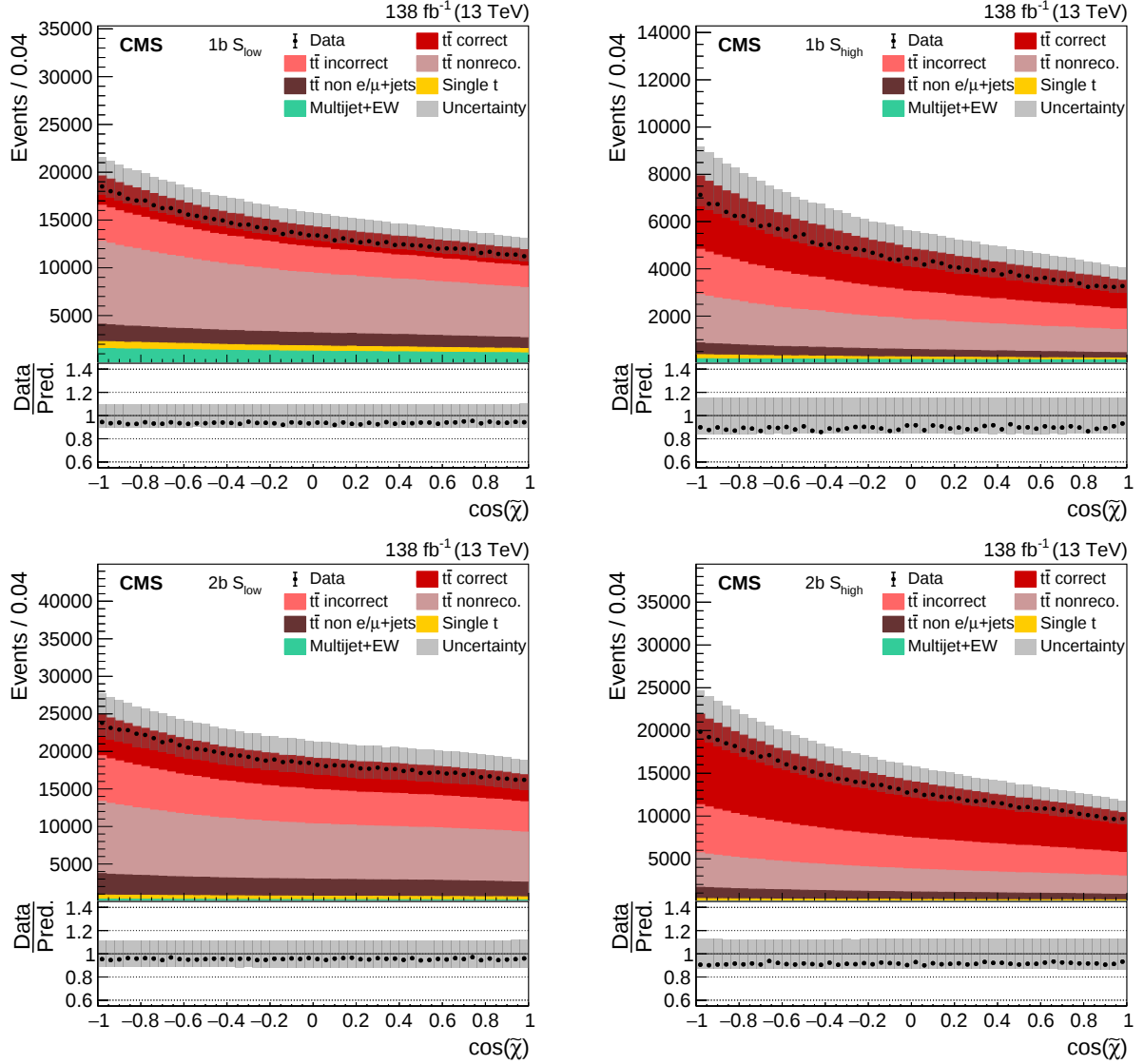


Figure 9: Distribution of $\cos(\tilde{\chi})$ in all four categories. The data (points) are compared to the prediction (stacked histograms). The $t\bar{t}$ and single top quark contributions are taken from the simulation, while the multijet+EW background is obtained from the CR. The $t\bar{t}$ contribution is split into the correctly and incorrectly reconstructed, “nonreconstructable”, and non e/ μ +jets events. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty of the data. Ratios to the predicted yields are provided in the lower panels.

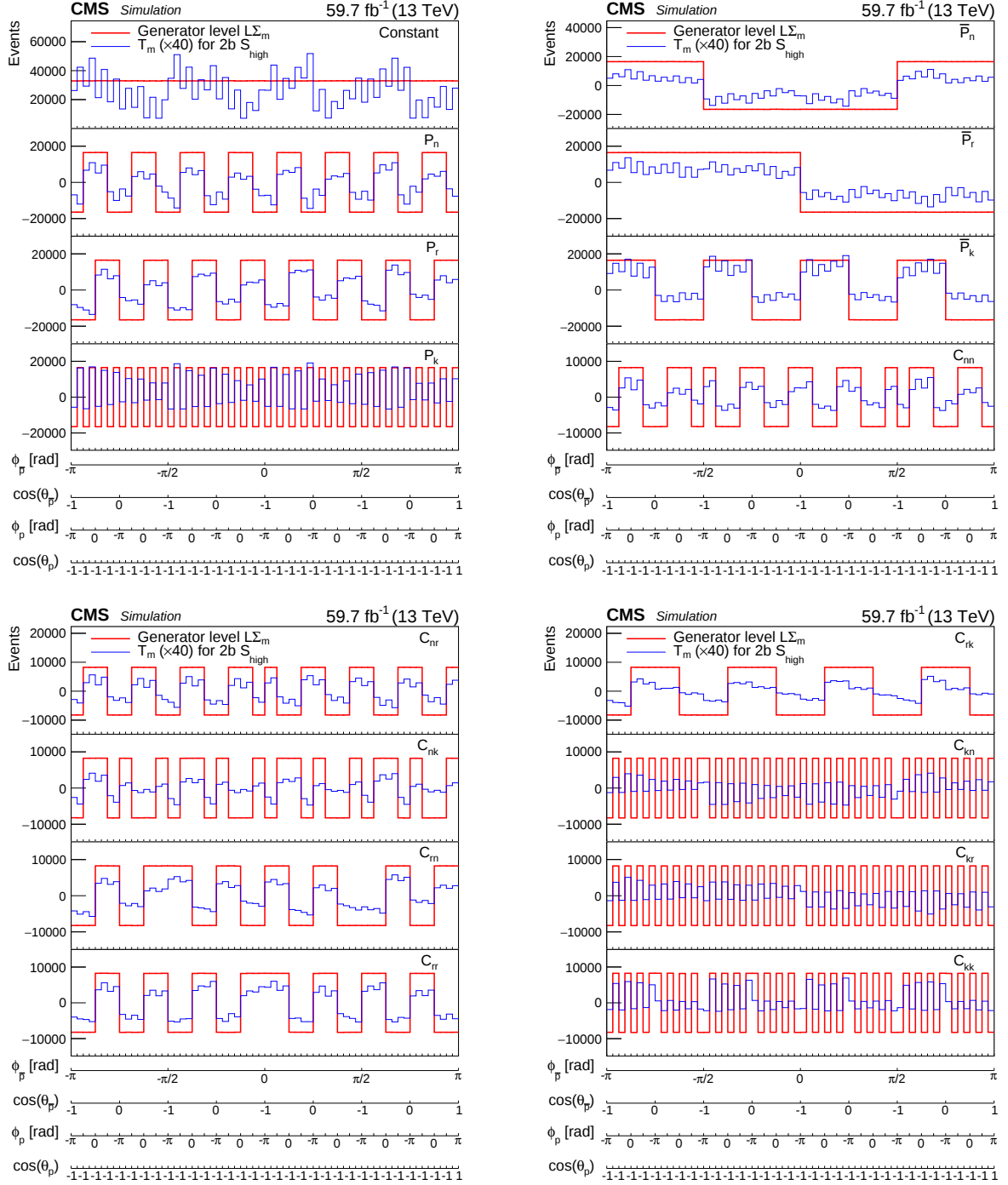


Figure 10: Examples of unrolled 4-dimensional distributions $L\Sigma_m$ and T_m as functions of $\phi_{\bar{p}}(\bar{p})$ and $\theta_{\bar{p}}(\bar{p})$ for the individual coefficients of the polarization vectors and the spin correlation matrix for events with $400 < m(t\bar{t}) < 600 \text{ GeV}$ and $|\cos(\theta)| < 0.4$. The $L\Sigma_m$ (red lines) are the distributions at the generator level in the full phase space, and the T_m (blue lines) are the distributions in the $2b S_{\text{high}}$ category for the 2018 data. For the purpose of illustration, the events are required to be reconstructed and generated in the same $m(t\bar{t})$ vs. $|\cos(\theta)|$ bin. The detector-level distributions are enhanced by a factor of 40 to improve their visibility.

values of the Q_m are fitted in each bin. However, at the detector level, the T_m do change as a function of the top quark and antiquark kinematic properties due to selection requirements and detector effects. Therefore, it is important to perform the measurements in sufficiently small bins such that either the Q_m or the T_m are approximately constant within each bin. If the T_m vary significantly within a fitted bin, the measured Q_m could be biased if the values of the coefficients change within a bin in a different way than in the SM simulation. The binnings in $m(\text{t}\bar{\text{t}})$ vs. $|\cos(\theta)|$ and $p_T(\text{t})$ vs. $|\cos(\theta)|$ were selected to minimize the bias due to nonconstant T_m templates within the bins. The way the templates are constructed ensures that a template fit to the SM prediction extracts the correct Q_m , i.e., the bias is minimized for SM-like data.

The same reweighting procedure is used for the D and $\tilde{D}$ measurements, but decomposing the distribution of $\cos(\chi)$ and $\cos(\tilde{\chi})$ into constant and linear terms as given by Eq. (6). In these cases we use 10 equally sized bins in $\cos(\chi)$, and $\cos(\tilde{\chi})$ for all measurements. A finer binning in $m(\text{t}\bar{\text{t}})$ of $\{300, 400, 500, 600, 700, 800, 900, 1000, 13000\}$ GeV and $p_T(\text{t})$ of $\{0, 50, 100, 150, 200, 250, 300, 400, 6500\}$ GeV is selected for the D and $\tilde{D}$ measurements.

We perform a maximum likelihood fit combining the information of the four selections (2b S_{high} , 2b S_{low} , 1b S_{high} , 1b S_{low}) in the four data-taking periods, for a total of 16 categories. The statistical model describes the total number of events in each bin

$$N_{ij'n'}(a_n, \{Q_{mn}\}, \{v_k\}) = S_{ij'n'}(a_n, \{Q_{mn}\}, \{v_k\}) + B_{ij'n'}(\{v_k\}), \quad (11)$$

with i denoting the category and j' referring to a bin in the 1-dimensional concatenated detector-level distribution of $\phi_{\text{p}(\bar{\text{p}})}$ and $\theta_{\text{p}(\bar{\text{p}})}$. The index n' (n) refers to a bin of the $m(\text{t}\bar{\text{t}})$ vs. $|\cos(\theta)|$ or $p_T(\text{t})$ vs. $|\cos(\theta)|$ distribution at the detector (generator) level. The normalization parameters a_n and the Q_{mn} (or D_n , $\tilde{D}_n$) are defined separately for each bin n and are free parameters in the fit. The $S_{ij'n'}$ and $B_{ij'n'}$ are the $\text{t}\bar{\text{t}}$ and background contributions, respectively, and both can depend on the nuisance parameters $\{v_k\}$ modeling the variation of the expected event yields due to systematic uncertainties. The $\text{t}\bar{\text{t}}$ contribution takes the form

$$S_{ij'n'}(a_n, \{Q_{mn}\}, \{v_k\}) = \sum_n a_n \left(T_{i0nj'n'}(\{v_k\}) + \sum_{m=1}^{15} Q_{mn} T_{imnj'n'}(\{v_k\}) \right), \quad (12)$$

where $T_{imnj'n'}$ are the detector-level distributions (templates) obtained by reweighting the $\text{t}\bar{\text{t}}$ simulation to the individual components proportional to the Q_{mn} and the templates $T_{i0nj'n'}$ correspond to the constant terms. Finally, the function

$$\begin{aligned} -2 \log \left(L(a_n, \{Q_{mn}\}, \{v_k\}) \right) = & -2 \sum_{ij'n'} \left[d_{ij'n'} \log \left(N_{ij'n'}(a_n, \{Q_{mn}\}, \{v_k\}) \right) \right. \\ & \left. - N_{ij'n'}(a_n, \{Q_{mn}\}, \{v_k\}) \right] - 2 \log \left(G(\{v_k\}) \right) \end{aligned} \quad (13)$$

is minimized with respect to the value of the parameters a_n , Q_{mn} , and v_k . Here, $d_{ij'n'}$ are the observed event yields and $G(\{v_k\})$ describes the Gaussian constraints of the v_k . Goodness of fit tests indicate good agreement between the data and the fitted model with p -values [66] of 0.80–0.95 for all fits. We tested that the Gaussian approximation can be used to describe the distributions of the uncertainties in the measured parameters. This allows us to use Gaussian error propagation when evaluating quantities derived from the measured parameters.

In Figs. 11–12, the pre- and post-fit distributions are shown for the full matrix measurement in the 2b S_{high} category. The pre-fit model uses the POWHEG+PYTHIA predictions. In addition, a model without any polarization and spin correlation is shown as a blue line to demonstrate

those effects. The 2b S_{high} category is shown here as an example since it is the category with the largest effects from polarization and spin correlation. The agreement between the data and the model is very similar in the other categories.

The same strategy is used to extract D_n ($\tilde{D}_n$) directly. In this case, j' represents a bin of $\cos(\chi)$ ($\cos(\tilde{\chi})$). The pre- and post-fit distributions in the 2b S_{high} category of the D and $\tilde{D}$ measurements in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ are presented in Figs. 13–16, respectively. The post-fit model describes the data well and no significant deviations are observed in any of the $m(t\bar{t})$ vs. $|\cos(\theta)|$ or $p_T(t)$ vs. $|\cos(\theta)|$ bins.

A possible bias in the measured Q_{mn} (D_n , $\tilde{D}_n$) was estimated by performing fits on simulations with variations of the coefficients of up to ± 0.3 , which exceeds the maximum observed difference between the expected and measured values. We found that any bias turns out to be negligible compared to the other uncertainties in the measurements. We also performed the fit using the POWHEG+HERWIG and MADGRAPH5_aMC@NLO+PYTHIA simulations as pseudo-data and found that we can extract the correct values of the coefficients.

9 Systematic uncertainties

Several theoretical and experimental systematic uncertainties affect the predicted event yields and are taken into account for the extraction of the Q_{mn} (D_n , $\tilde{D}_n$). Their templates are obtained from alternative or reweighted simulations corresponding to variations in a specific uncertainty source, usually by one standard deviation. We take into account the following theoretical uncertainties:

- The effect of higher-order contributions to the ME calculation is estimated by varying the renormalization μ_r and factorization μ_f scales up and down by a factor of two. Distributions for these variations are obtained using event weights in the POWHEG+PYTHIA simulation. The variations of μ_r and μ_f are parameterized in the fit by two independent nuisance parameters. The ME scales of $t\bar{t}$ and single top quark production are treated separately.
- The difference in the $p_T(t)$ spectrum between the POWHEG+PYTHIA NLO and the NNLO calculations, obtained with POWHEG MINNLO+PYTHIA exceeds what is expected based on the μ_r and μ_f variations. Therefore, an additional uncertainty is introduced, whose +1 standard deviation variation corresponds to the reweighting of the NLO to the NNLO simulation using a NN-based method [67, 68]. The NN-based approach is used to reduce the statistical fluctuations in this uncertainty.
- First order virtual electroweak corrections are calculated with HATHOR and applied to LO $t\bar{t}$ events obtained with MADGRAPH5_aMC@NLO+PYTHIA. The ratio to the LO simulation without electroweak corrections is determined as a function of $m(t\bar{t})$ and $|\cos(\theta)|$. These ratios are used as event weights to correct the POWHEG simulation. The differences between the electroweak corrected and the default POWHEG simulation are taken into account as uncertainty.
- The 100 Hessian variations of the NNPDF3.1 set plus the variation of strong coupling α_s are taken into account as PDF uncertainties. For each of these variations a nuisance parameter is added. The distributions are obtained using the corresponding event weights. The PDF variations are correlated for $t\bar{t}$ and single top quark production.
- The uncertainties in the initial- and final-state parton showers are estimated by vary-

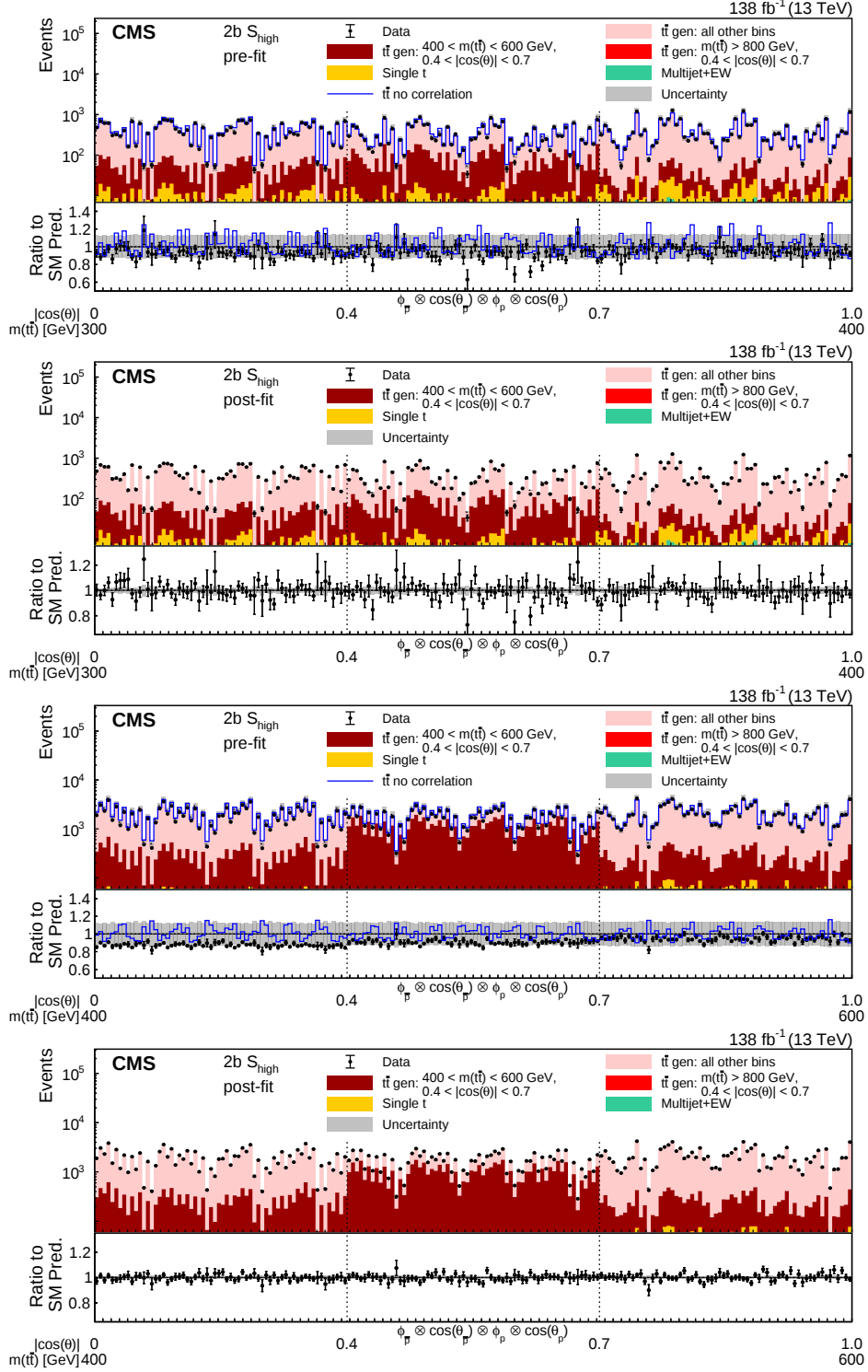


Figure 11: Pre- and post-fit distributions comparing the data (points) to the POWHEG+PYTHIA simulation (stacked histograms) for the full matrix measurement in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ in the $2b S_{\text{high}}$ category. The x axis shows the bins of the unrolled 4-dimensional distribution of $\phi_{\bar{p}}, \cos(\theta_{\bar{p}}), \phi_p,$ and $\cos(\theta_p)$, listed from the outermost to the innermost variable in each of the $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins. The boundaries of the $|\cos(\theta)|$ and $m(t\bar{t})$ bins are labeled and indicated by dashed and solid lines, respectively. For the illustration of resolution effects, $t\bar{t}$ events generated in two selected $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins are shown in different shades of red. All other $t\bar{t}$ contributions are shown in pink. A model without any polarization and spin correlation is shown as a blue line. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty. Ratios to the predicted yields are provided in the lower panels.

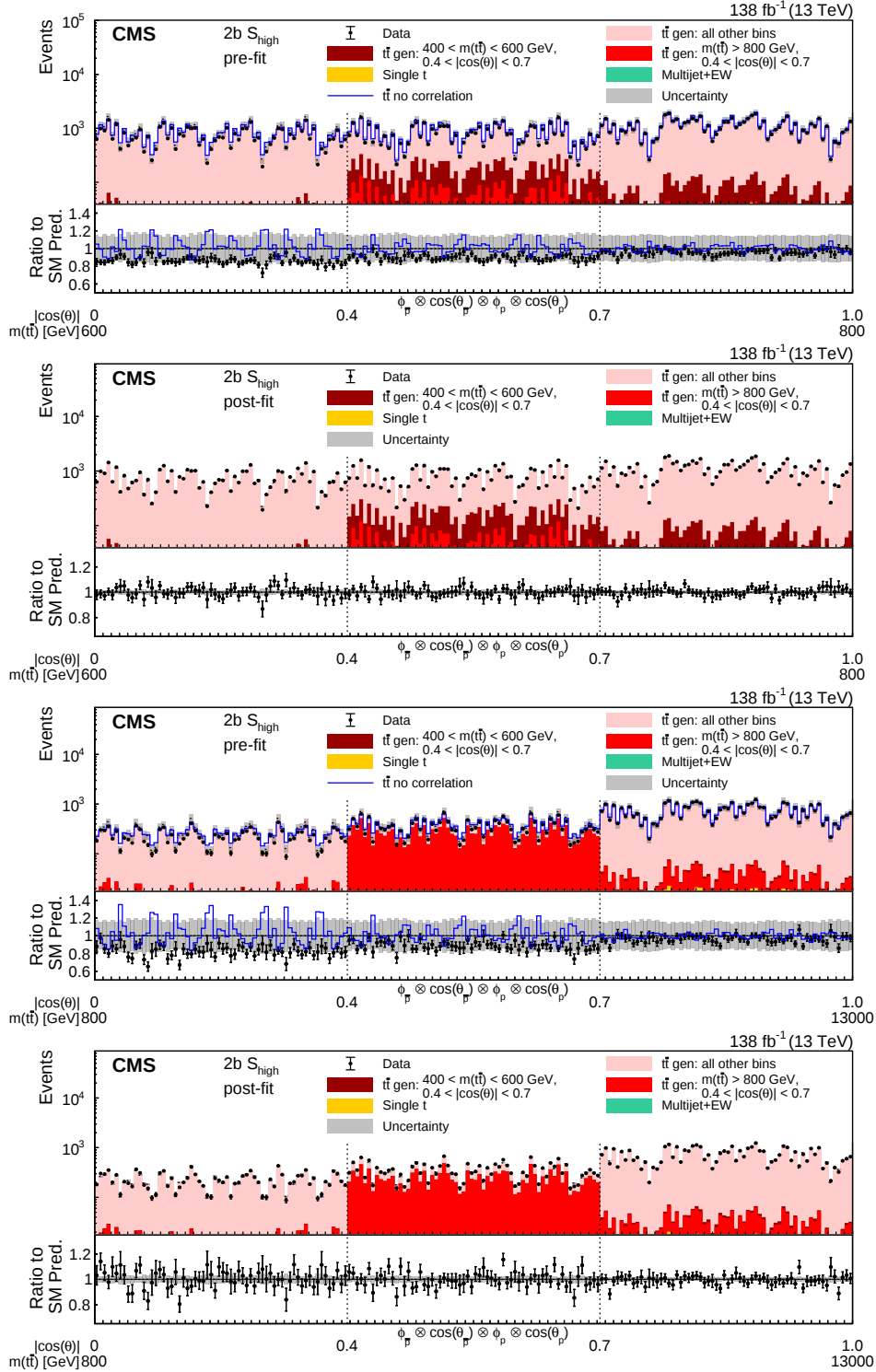


Figure 12: Pre- and post-fit distributions comparing the data (points) to the POWHEG+PYTHIA simulation (stacked histograms) for the full matrix measurement in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ in the $2b S_{\text{high}}$ category. The x axis shows the bins of the unrolled 4-dimensional distribution of $\phi_{\bar{p}}, \cos(\theta_{\bar{p}}), \phi_p$, and $\cos(\theta_p)$, listed from the outermost to the innermost variable in each of the $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins. The boundaries of the $|\cos(\theta)|$ and $m(t\bar{t})$ bins are labeled and indicated by dashed and solid lines, respectively. For the illustration of resolution effects, $t\bar{t}$ events generated in two selected $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins are shown in different shades of red. All other $t\bar{t}$ contributions are shown in pink. A model without any polarization and spin correlation is shown as a blue line. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty. Ratios to the predicted yields are provided in the lower panels.

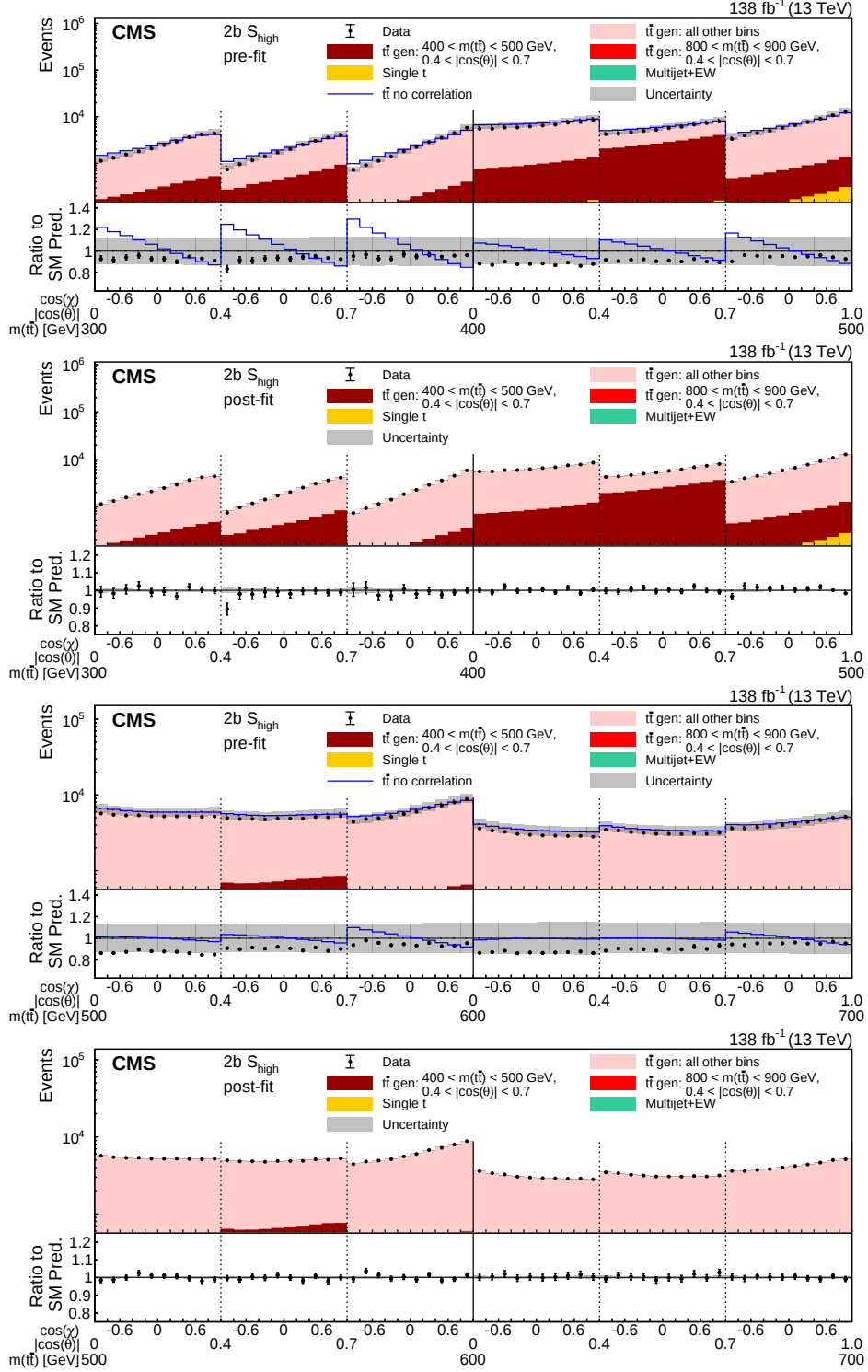


Figure 13: Pre- and post-fit distributions of $\cos(\chi)$ comparing the data (points) to the POWHEG+PYTHIA simulation (stacked histograms) for the D measurement in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ in the $2b S_{\text{high}}$ category. The boundaries of the $|\cos(\theta)|$ and $m(t\bar{t})$ bins are labeled and indicated by dashed and solid lines, respectively. For the illustration of resolution effects, $t\bar{t}$ events generated in two selected $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins are shown in different shades of red. All other $t\bar{t}$ contributions are shown in pink. A model without any polarization and spin correlation is shown as a blue line. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty. Ratios to the predicted yields are provided in the lower panels.

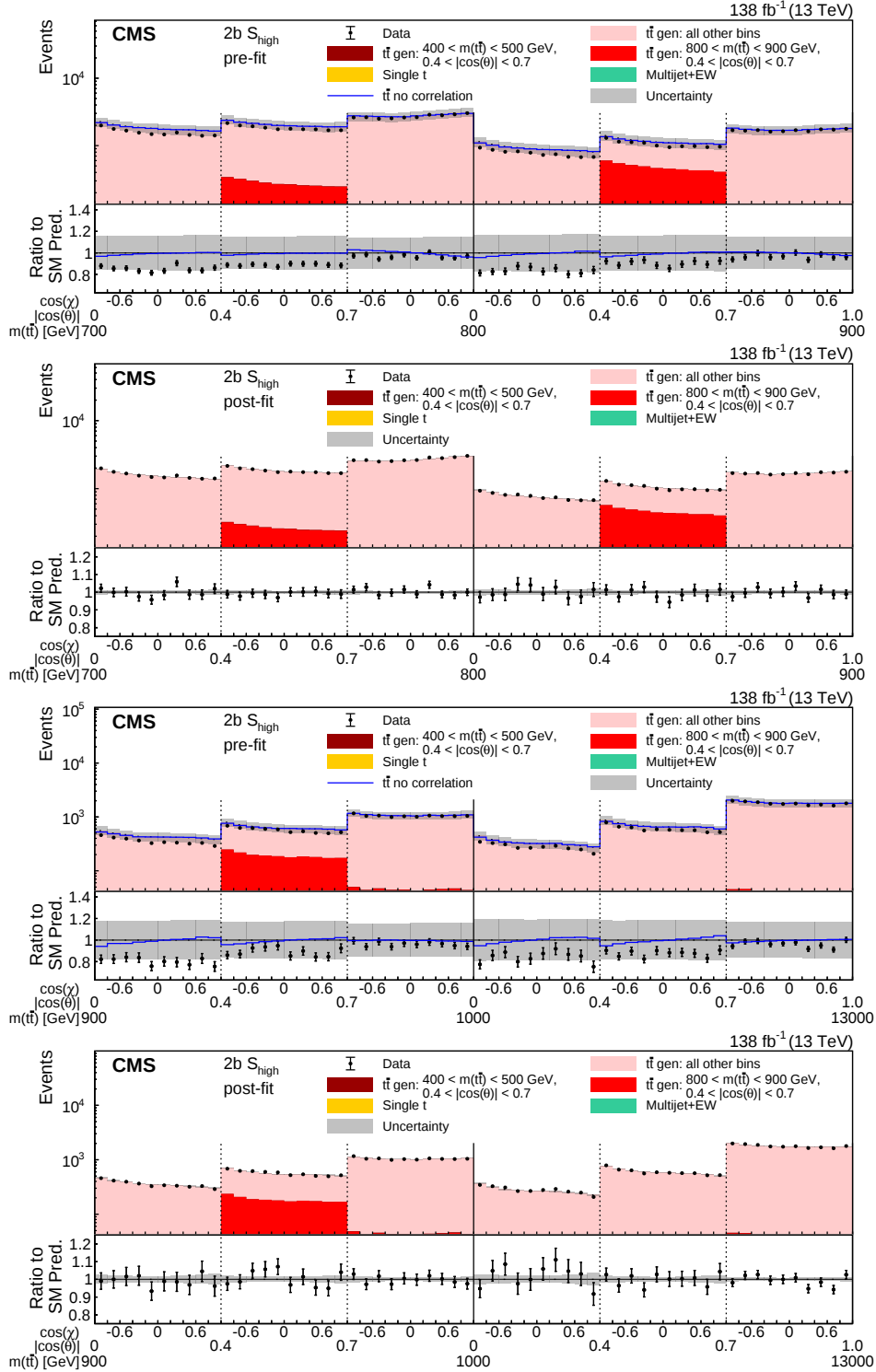


Figure 14: Pre- and post-fit distributions of $\cos(\chi)$ comparing the data (points) to the POWHEG+PYTHIA simulation (stacked histograms) for the D measurement in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ in the $2b S_{\text{high}}$ category. The boundaries of the $|\cos(\theta)|$ and $m(t\bar{t})$ bins are labeled and indicated by dashed and solid lines, respectively. For the illustration of resolution effects, $t\bar{t}$ events generated in two selected $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins are shown in different shades of red. All other $t\bar{t}$ contributions are shown in pink. A model without any polarization and spin correlation is shown as a blue line. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty. Ratios to the predicted yields are provided in the lower panels.

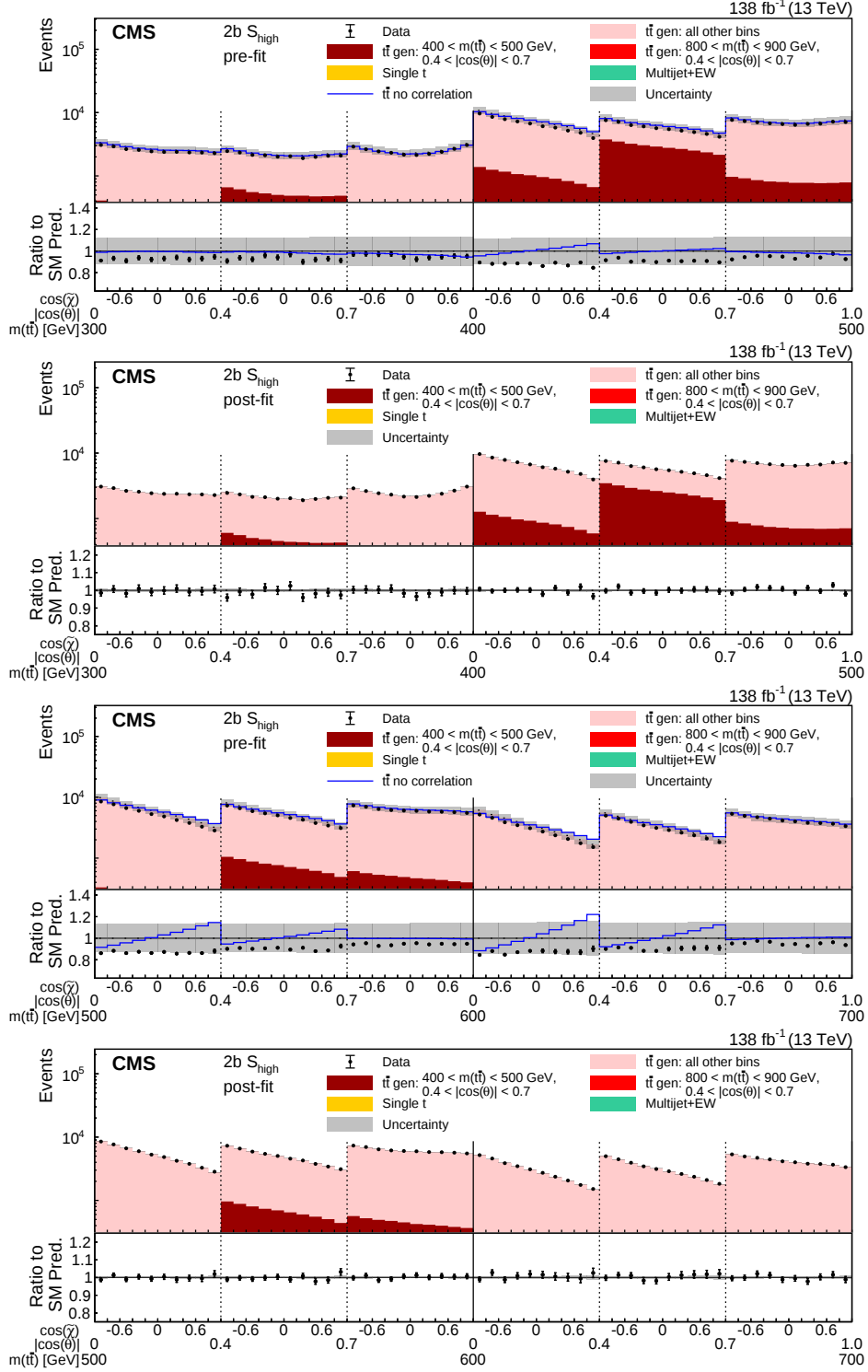


Figure 15: Pre- and post-fit distributions of $\cos(\tilde{\chi})$ comparing the data (points) to the POWHEG+PYTHIA simulation (stacked histograms) for the $\hat{D}$ measurement in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ in the $2b S_{\text{high}}$ category. The boundaries of the $|\cos(\theta)|$ and $m(t\bar{t})$ bins are labeled and indicated by dashed and solid lines, respectively. For the illustration of resolution effects, $t\bar{t}$ events generated in two selected $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins are shown in different shades of red. All other $t\bar{t}$ contributions are shown in pink. A model without any polarization and spin correlation is shown as a blue line. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty. Ratios to the predicted yields are provided in the lower panels.

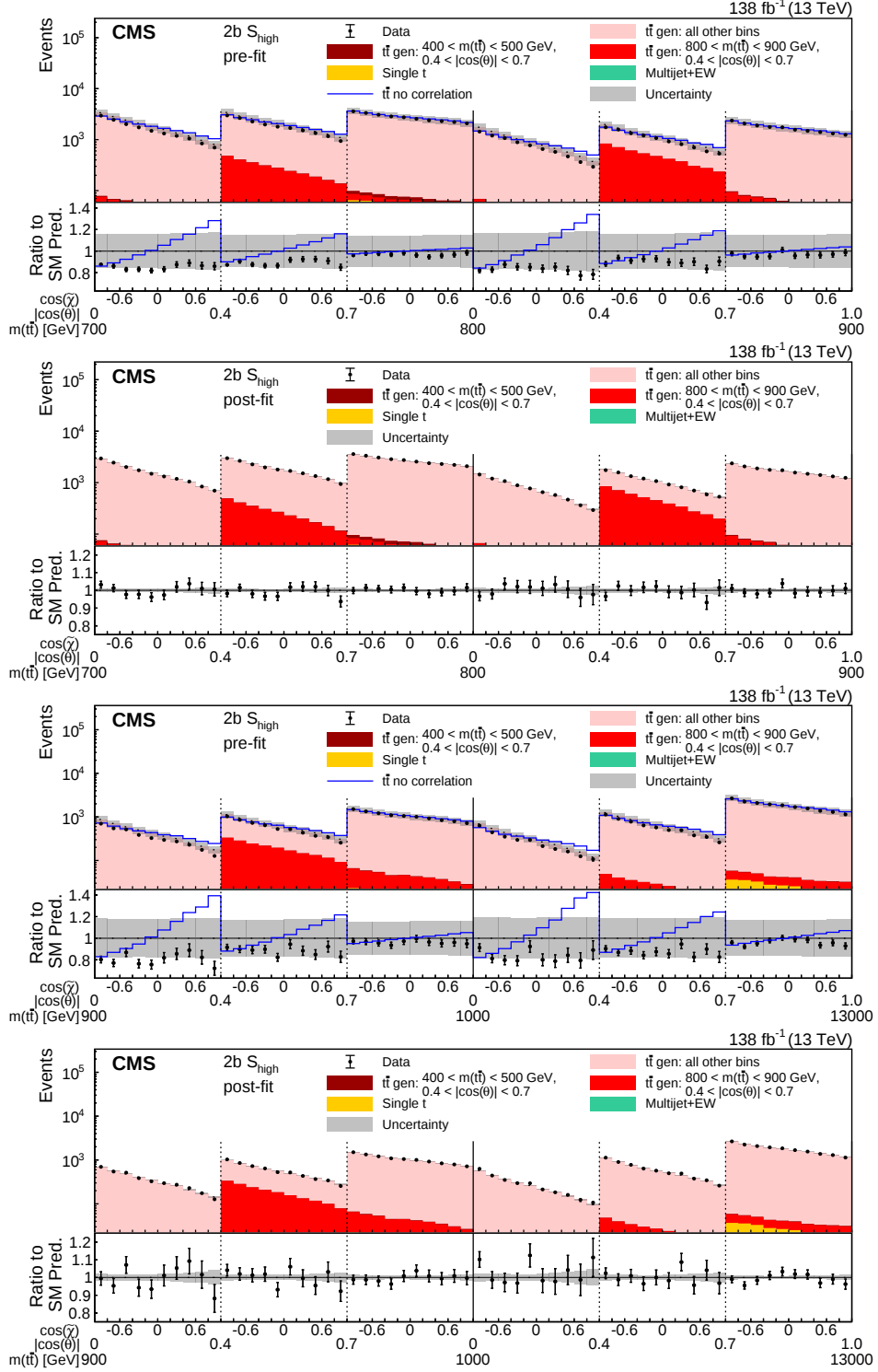


Figure 16: Pre- and post-fit distributions of $\cos(\tilde{\chi})$ comparing the data (points) to the POWHEG+PYTHIA simulation (stacked histograms) for the $\hat{D}$ measurement in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ in the $2b S_{\text{high}}$ category. The boundaries of the $|\cos(\theta)|$ and $m(t\bar{t})$ bins are labeled and indicated by dashed and solid lines, respectively. For the illustration of resolution effects, $t\bar{t}$ events generated in two selected $m(t\bar{t})$ vs. $|\cos(\theta)|$ bins are shown in different shades of red. All other $t\bar{t}$ contributions are shown in pink. A model without any polarization and spin correlation is shown as a blue line. The gray uncertainty band indicates the combined statistical and systematic uncertainties in the prediction. The vertical bars on the points show the statistical uncertainty. Ratios to the predicted yields are provided in the lower panels.

ing the scales for the different splittings $g \rightarrow q\bar{q}$, $g \rightarrow gg$, $q \rightarrow qg$, and $b \rightarrow bg$ by a factor of two, resulting in a total of eight independent variations. The corresponding distributions are obtained using event weights. The parton shower scale variations are correlated for $t\bar{t}$ and single top quark production.

- The scale that separates the phase space of the first QCD emission into soft and hard parts is controlled by the h_{damp} parameter for POWHEG simulations. The values used for the CP5 tune are $1.38^{+0.92}_{-0.51} m_t$. Separate samples produced with the different values of h_{damp} are used to obtain the corresponding distributions. To reduce the impact from statistical fluctuations we employ the NN based approach [67] to determine the weights applied to the central simulation based on the kinematic properties of top quarks determined at the generator level.
- To estimate the effect of the uncertainty in m_t , a variation of 0.5 GeV [48] is taken into account. For the evaluation of the expected event yields, we use the m_t -dependent $t\bar{t}$ production cross sections of 843 (820) pb for $m_t = 172.0$ (173.0) GeV [69].
- The uncertainties in the underlying event modeling are estimated using separate samples that represent an envelope of the uncertainties in the PYTHIA CP5 tune [40].
- The fraction of leptonically decaying b hadrons is changed according to the known uncertainty in the branching fraction using event-based reweighting [1].
- The uncertainty in the color reconnection is assessed using an alternative model where the reconnection of colored particles from resonant decays is activated in PYTHIA, while this is deactivated in the default tune. Other variations use the gluon move and the QCD-inspired models [70, 71]. The differences between these three and the default samples are added as symmetric uncertainties.
- At the $t\bar{t}$ production threshold, theoretical calculations based on nonrelativistic QCD [72] predict $t\bar{t}$ bound states and other effects not included in the POWHEG+PYTHIA simulation. To estimate their effects on the measurement, we mimic the theoretical calculation by adding a pseudoscalar particle η_t with a mass of 343 GeV and a width of twice the top quark width. It is produced in gg fusion and decays as $\eta_t \rightarrow WbW\bar{b}$. This is calculated using MADGRAPH5_aMC@NLO+PYTHIA and normalized using the cross section of 6.43 pb from Ref. [73]. The difference observed using this model is used to estimate the uncertainty due to bound-state effects.

All theoretical uncertainties affect all data-taking periods in the same way and the corresponding nuisance parameters are fully correlated between them.

We take into account the following experimental uncertainties:

- The integrated luminosities for the 2016, 2017, and 2018 data-taking years have 1.2–2.5% individual uncertainties [74–76], while the overall uncertainty for the 2016–2018 period is 1.6%.
- The prediction of the number of pileup interactions in simulation is assuming a total inelastic proton-proton cross section of 69.2 mb [77]. Changes in the simulated pileup multiplicity are estimated by varying the total inelastic cross section by $\pm 4.6\%$. Templates with enhanced and reduced pileup are obtained by applying event weights. This uncertainty is treated as fully correlated between the data-taking periods.
- The jet energy scale uncertainties are split into 19 different sources [61]. The combined uncertainties are p_T - and η -dependent, with a magnitude that varies between

0.3 and 1.8% for the relevant jets. In addition, variations are applied depending on the true generated type to b jets, c jets, uds jets, and gluon jets. The correlations among the years are evaluated for each source. The differences in the distributions are obtained by rescaling the jet momenta in the simulation.

- Separate uncertainties for the jet energy resolution are taken into account for jets in the endcap and barrel regions by varying the resolution corrections within their uncertainties. These uncertainties are uncorrelated among the years.
- The dominant uncertainty in the p_T^{miss} is due to the jet energy calibration. Therefore, the p_T^{miss} is also recalculated whenever the jet momenta are rescaled. An additional contribution to the uncertainty due to particles that do not belong to the selected jets is estimated [64]. This uncertainty is uncorrelated among years.
- Uncertainties in the electron and muon reconstruction and trigger efficiencies are determined [58]. For each flavor a statistical and systematic uncertainty in the derived scale factors are taken into account, where the statistical component is uncorrelated and the systematic component is correlated among the years. In addition, an overall normalization uncertainty of 0.5% is used to account for the differences in DY and $t\bar{t}$ events.
- Since the analysis uses three b tagging categories as input to the NN, we allow for separate variations of the uncertainties in the scale factors for the tight, medium, and loose b tagging selections [62, 78]. The variations are performed by recalculating an event probability using all jets and their true type. The uncertainties in the correction factors for b and c jets are split into several sources such as statistical, jet energy correction, and pileup uncertainties. The statistical uncertainty is uncorrelated among the years, while the rest is treated as correlated. The uncertainties in the correction factors for the light jet flavors are split into a correlated and an uncorrelated component.
- During the data-taking, a gradual shift in the timing of the inputs of the ECAL L1 trigger in the region $|\eta| > 2.0$ and of the muon trigger caused a specific trigger inefficiency. Correction factors as functions of p_T , η , and time are computed from data and applied to the simulation. The statistical uncertainties in these correction factors are taken into account.
- The uncertainties in the background estimations are detailed in Section 7.

For each bin, an additional nuisance parameter is added [79] whose variation corresponds to the statistical uncertainty in the central templates. It is known that statistical fluctuations are also important for the systematic variations. In particular, if the variations are evaluated based on statistically independent simulations, the statistical effects can easily reach or even exceed the magnitude of the systematic effect. Therefore, it is often helpful to require a certain smoothness of the relative systematic effects. This reduces unphysical constraints of the related nuisance parameters. A 6(3)-dimensional smoothing [80] is applied for the full matrix (D and $\tilde{D}$) measurements.

10 Results

From the fits to the data we obtain the values of Q_{mn} (D_n , $\tilde{D}_n$) in bins of $m(t\bar{t})$ vs. $|\cos(\theta)|$ or $p_T(t)$ vs. $|\cos(\theta)|$. In the following, we concentrate on regions of the phase space that are of special interest, e.g., where a higher level of entanglement is expected. Most of the presented results are obtained from the combination of several $m(t\bar{t})$ vs. $|\cos(\theta)|$ or $p_T(t)$ vs. $|\cos(\theta)|$ bins.

With the $t\bar{t}$ event yields of the post-fit model at the generator level Y_n , and the normalization factors a_n , we obtain the total fitted event yields $K_n = Y_n a_n$. The result in a combined bin g is then obtained by averaging the measurements from bins $\{n\}$ using

$$\hat{Q}_{mg} = \frac{1}{\sum_{n \in g} K_n} \sum_{n \in g} K_n Q_{mn}. \quad (14)$$

The uncertainties in $\hat{Q}_{mg}$ are calculated using error propagation taking into account the uncertainties and their correlations in the event yields and the Q_{mn} as obtained from the fit. The combined normalization factors are obtained based on the K_n sum

$$c_g = \frac{1}{\sum_{n \in g} Y'_n} \sum_{n \in g} K_n, \quad (15)$$

where Y'_n are the $t\bar{t}$ yields of the pre-fit model at the generator level.

Following Refs. [9, 25], we use the new observables $C_{nr}^\pm = C_{nr} \pm C_{rm}$, $C_{rk}^\pm = C_{rk} \pm C_{kr}$, and $C_{nk}^\pm = C_{nk} \pm C_{kn}$, where for the calculation the covariances are taken into account. These are either even or odd under parity (P) and charge-parity (CP) transformations.

The inclusive full matrix measurements based on the $m(t\bar{t})$ vs. $|\cos(\theta)|$ and $p_T(t)$ vs. $|\cos(\theta)|$ fits are obtained from the combination of all bins in the additional observables, and are shown in Fig. 17. The displayed values of Δ_E are calculated following Eq. (5).

As expected, both binnings lead to consistent results, where the $p_T(t)$ vs. $|\cos(\theta)|$ binning has a higher expected and observed precision. For the inclusive coefficients, the values predicted by POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA, and MINNLO+PYTHIA are similar. The measured coefficients are in agreement with the predictions and consistent with the previous measurement in the $t\bar{t}$ dilepton channel [9]. The measured polarizations are all compatible with zero. Only the diagonal elements of C differ from zero with the exception of C_{rk}^+ , which is the only even coefficient under P and CP transformation. In Fig. 18 the results of the inclusive D and $\bar{D}$ measurements obtained with the $m(t\bar{t})$ vs. $|\cos(\theta)|$ and $p_T(t)$ vs. $|\cos(\theta)|$ binnings are shown.

Entangled quantum states are expected at the threshold of $t\bar{t}$ production and also at high $m(t\bar{t})$ and $p_T(t)$ in events with low $|\cos(\theta)|$ [21]. Therefore, taking advantage of the binning in the additional observables, we can obtain the spin correlation coefficients and thus test the entanglement criterion in several $m(t\bar{t})$ and $p_T(t)$ regions and its dependence on $|\cos(\theta)|$. Figures 19–22 provide the results of the full matrix measurements including the Δ_E values in bins of $m(t\bar{t})$ and $p_T(t)$, i.e., we combine the $|\cos(\theta)|$ bins in each of these regions. While POWHEG+HERWIG predicts a slightly smaller spin correlation than the other simulations, the measured coefficients are compatible with all predictions. With these measurements, the differences in the spin correlation for various kinematic regions become clearly visible. In particular, for the measurement in $p_T(t)$, we observe the signs of C_{rr} and C_{kk} changing from positive to negative with increasing $p_T(t)$, indicating the transition from the spin-singlet to the spin-triplet as the dominant state.

At the $t\bar{t}$ production threshold, the most significant results for entanglement using the full matrix measurement, based on the criterion $\Delta_E > 1$, are obtained for $m(t\bar{t}) < 400$ GeV and for $p_T(t) < 100$ GeV. We evaluate the significance of the deviation from the separable state hypothesis with $\Delta_E = 1$ based on the uncertainties in the measured values of Δ_E . However, the observed significance for entanglement does not exceed 2 standard deviations.

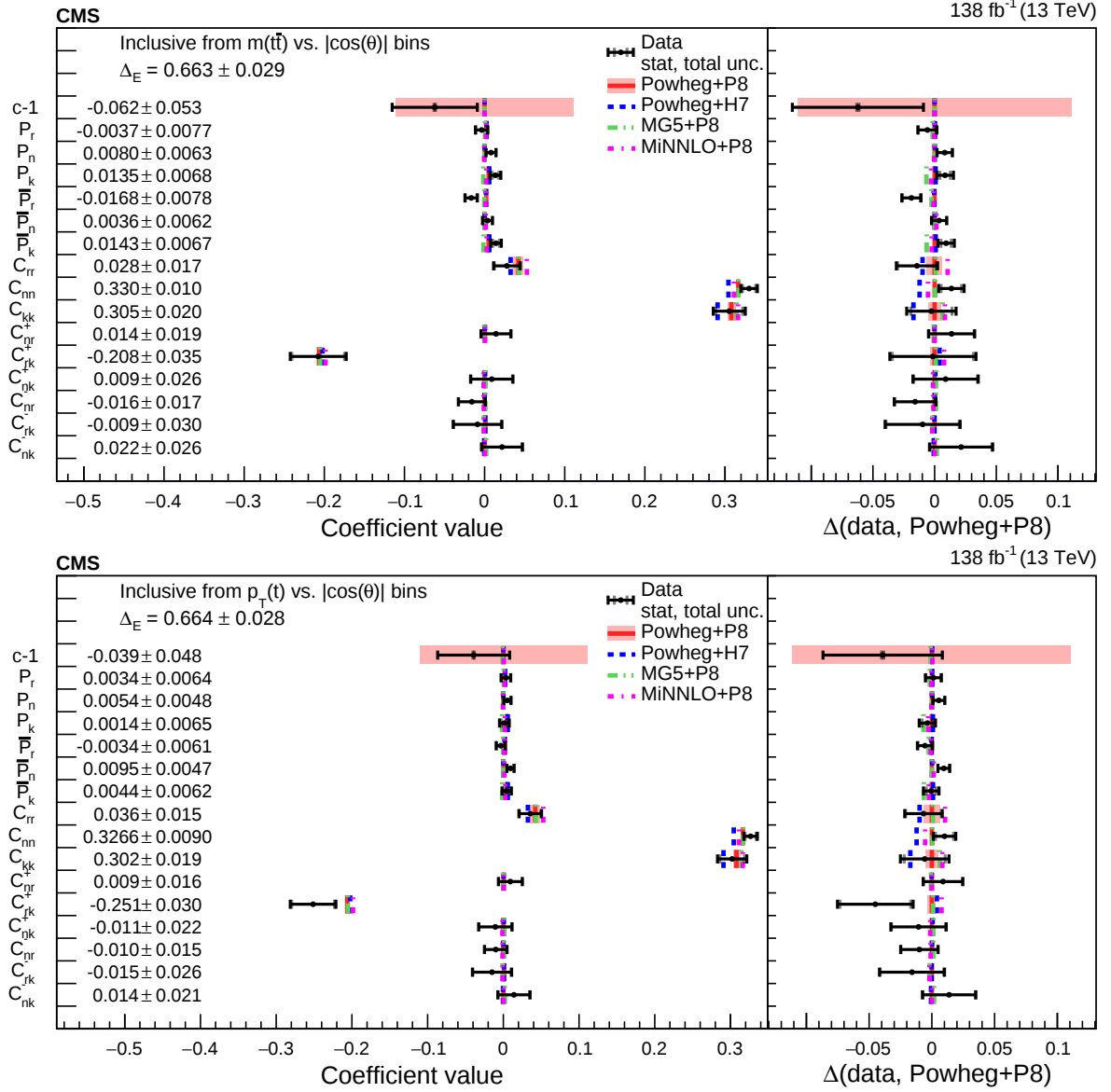


Figure 17: Results of the inclusive full matrix measurement obtained by combining the bins of the $m(t\bar{t})$ vs. $|\cos(\theta)|$ (upper) and $p_T(t)$ vs. $|\cos(\theta)|$ (lower) measurements. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

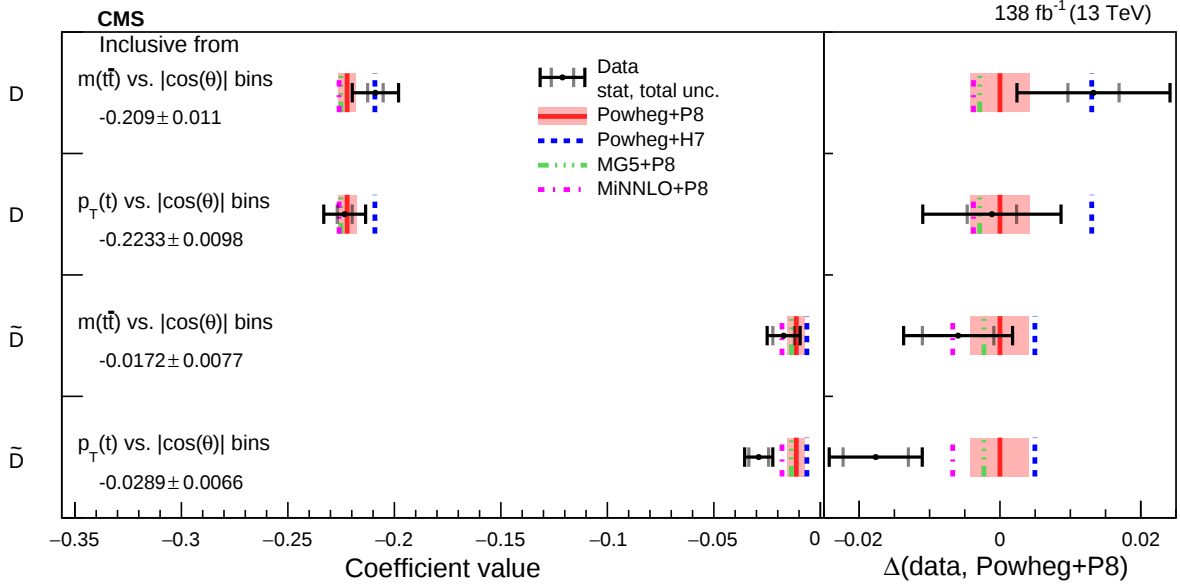


Figure 18: Results of the inclusive D and $\bar{D}$ measurement obtained by combining the bins of the $m(t\bar{t})$ vs. $|\cos(\theta)|$ and $p_T(t)$ vs. $|\cos(\theta)|$ measurements. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panel, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties.

The D and $\bar{D}$ measurements are presented in bins of $m(t\bar{t})$ and $p_T(t)$ in Fig. 23. The finer $p_T(t)$ binning in the D measurement allows studying events with $p_T(t) < 50$ GeV, where a significance for entanglement of 3.5 (4.4) standard deviations is observed (expected). A similar analysis performed in the dilepton channel [15] has higher sensitivity for entanglement at the $t\bar{t}$ production threshold. Overall POWHEG+HERWIG predicts slightly higher values of D in the threshold region, but the measured coefficients remain compatible with all predictions.

Figure 24 shows the contributions of various uncertainty sources to the uncertainties in the measured Δ_E , D , and $\bar{D}$ in bins of $m(t\bar{t})$. In general, the uncertainties in the results are dominated by the statistical contribution, with the exception of the D measurement, where systematic effects are more important at low $m(t\bar{t})$. The uncertainty in the b tagging calibration is the dominant source, but depending on the bin, theoretical uncertainties can be of similar sizes, in particular ME and PS scales.

We further study the results in the region $|\cos(\theta)| < 0.4$. These are shown in bins of $m(t\bar{t})$ in Figs. 25–26 for the full matrix and in Fig. 27 for the $\bar{D}$ measurement. The most significant observation (expectation) of entanglement is obtained for $m(t\bar{t}) > 800$ GeV and $|\cos(\theta)| < 0.4$, with 6.7 (5.6) standard deviations for the full matrix measurement and 6.1 (5.5) standard deviations for the $\bar{D}$ measurement. The D measurement does not have any sensitivity for entanglement in this region, since the diagonal elements of the C matrix do not all have the same sign.

Figure 28 summarizes the observed (expected) significance of the measured entanglement variables. In the upper panels of Fig. 28, the measured results for D (left) near the $t\bar{t}$ production threshold and for $\bar{D}$ (right) at high $m(t\bar{t})$ and low $|\cos(\theta)|$ are shown. For the full matrix measurement (lower), the Δ_E results with the highest expected significance are shown for the threshold and high- $m(t\bar{t})$ kinematic regions.

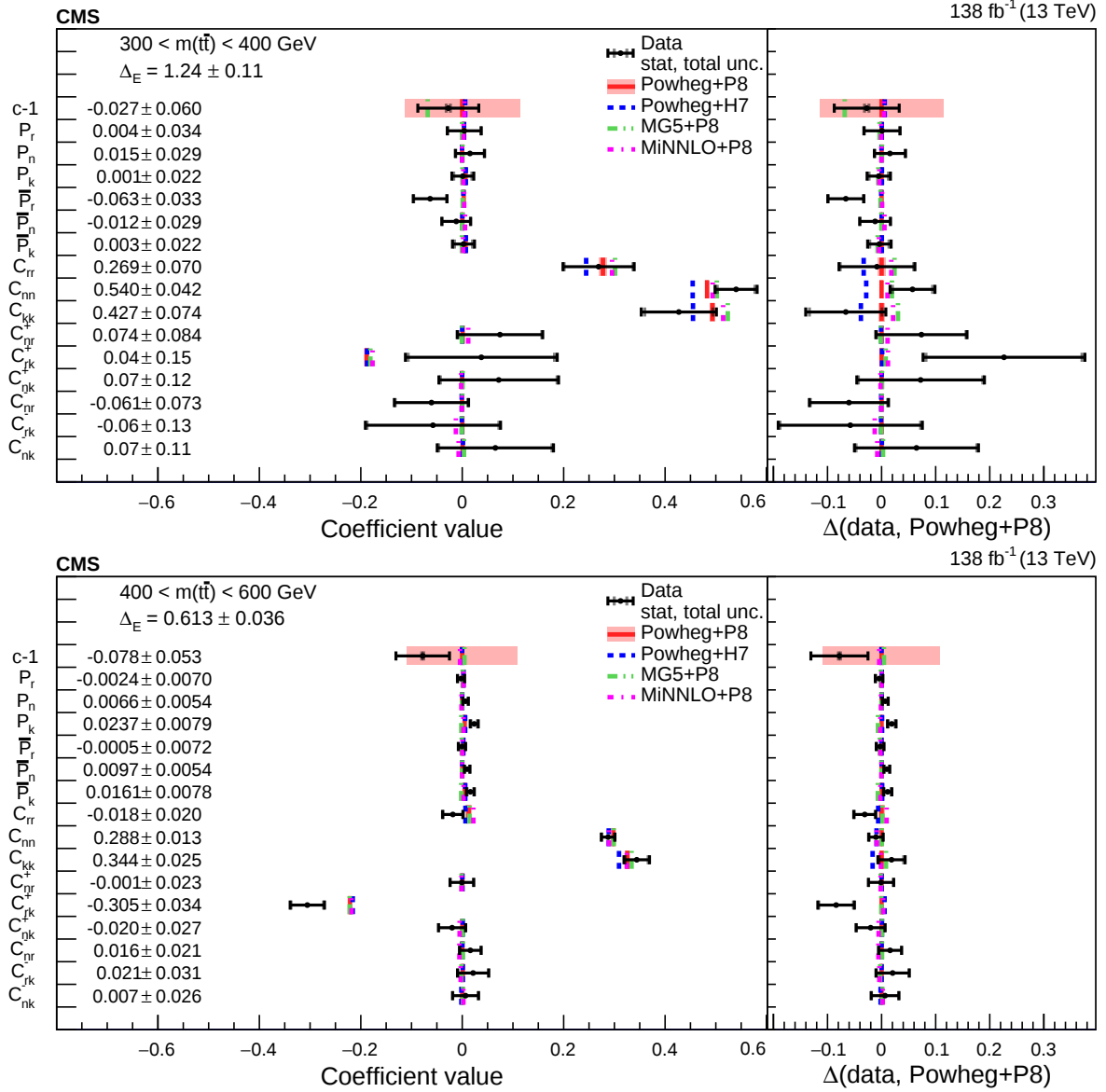


Figure 19: Results of the full matrix measurement in bins of $m(\text{t}\bar{\text{t}})$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

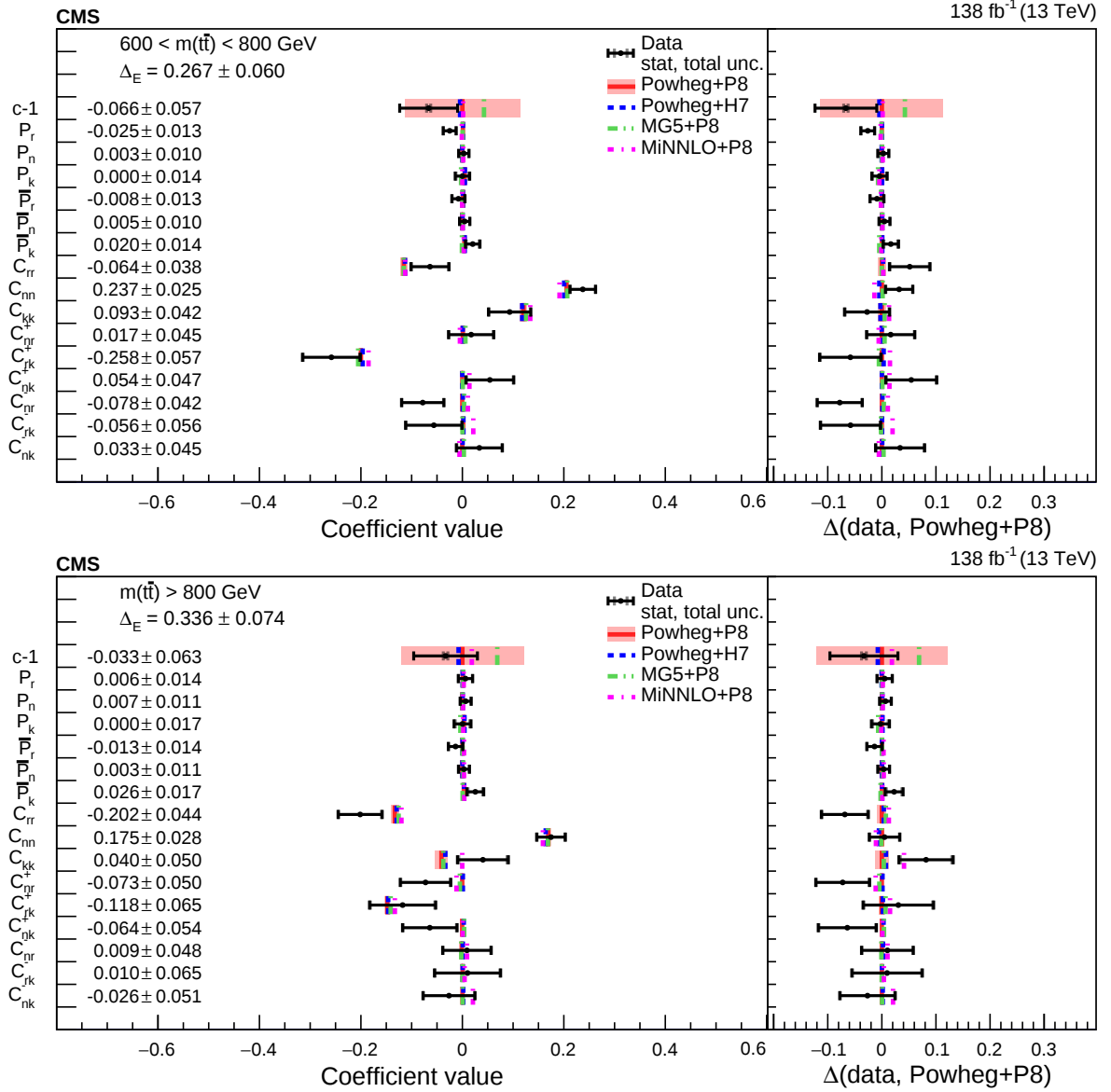


Figure 20: Results of the full matrix measurement in bins of $m(t\bar{t})$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

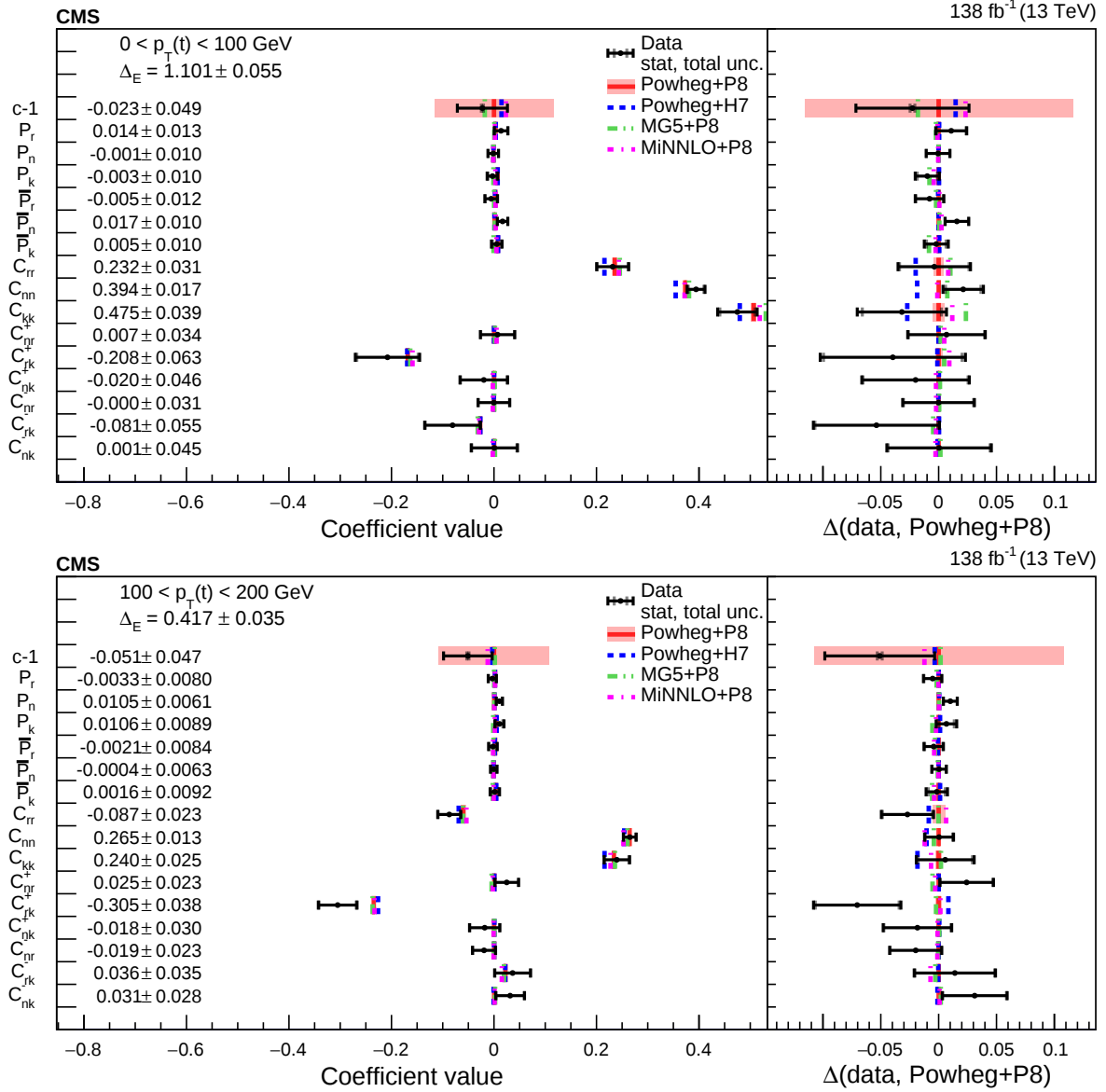


Figure 21: Results of the full matrix measurement in bins of $p_T(t)$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

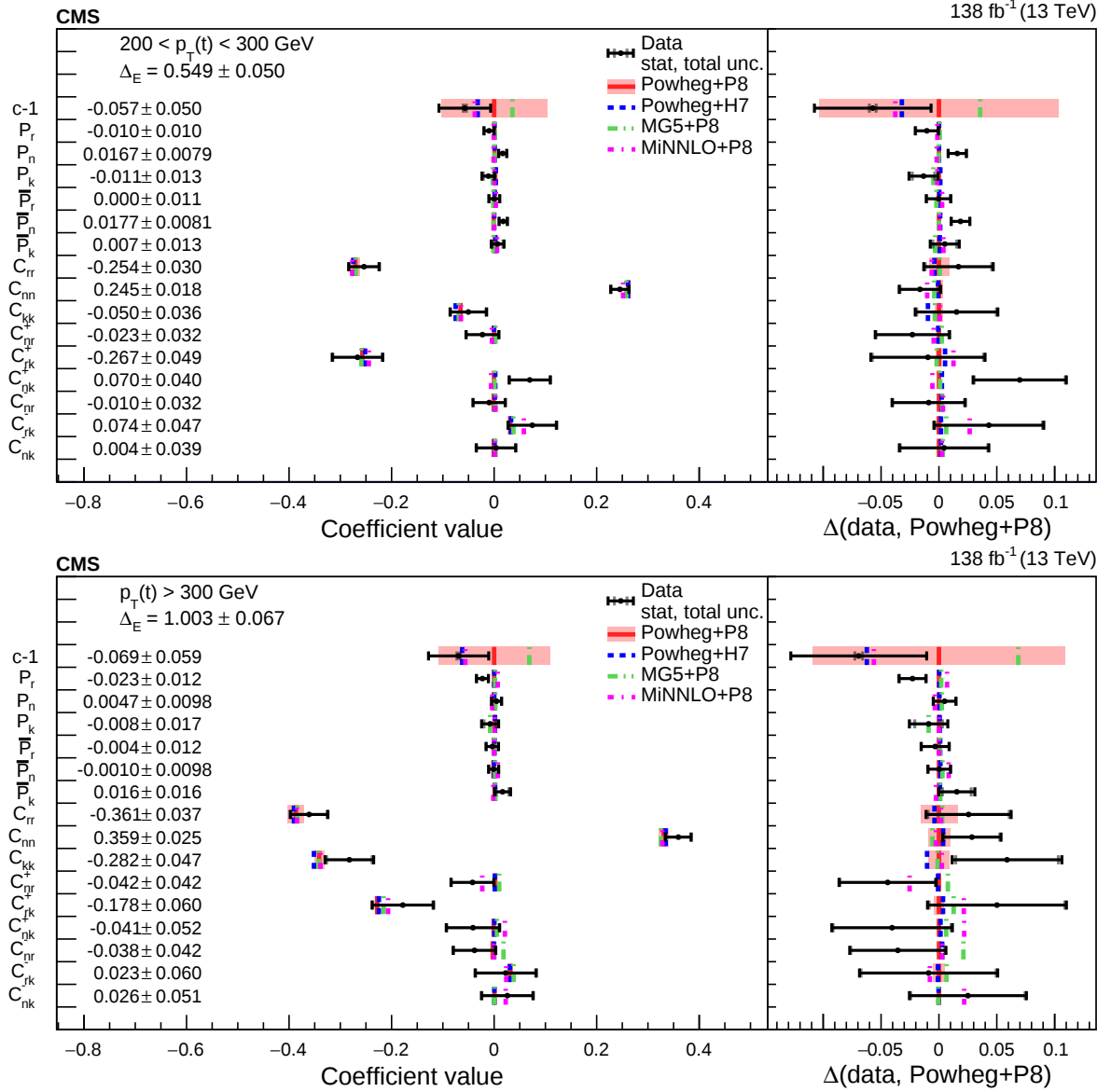


Figure 22: Results of the full matrix measurement in bins of $p_T(t)$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

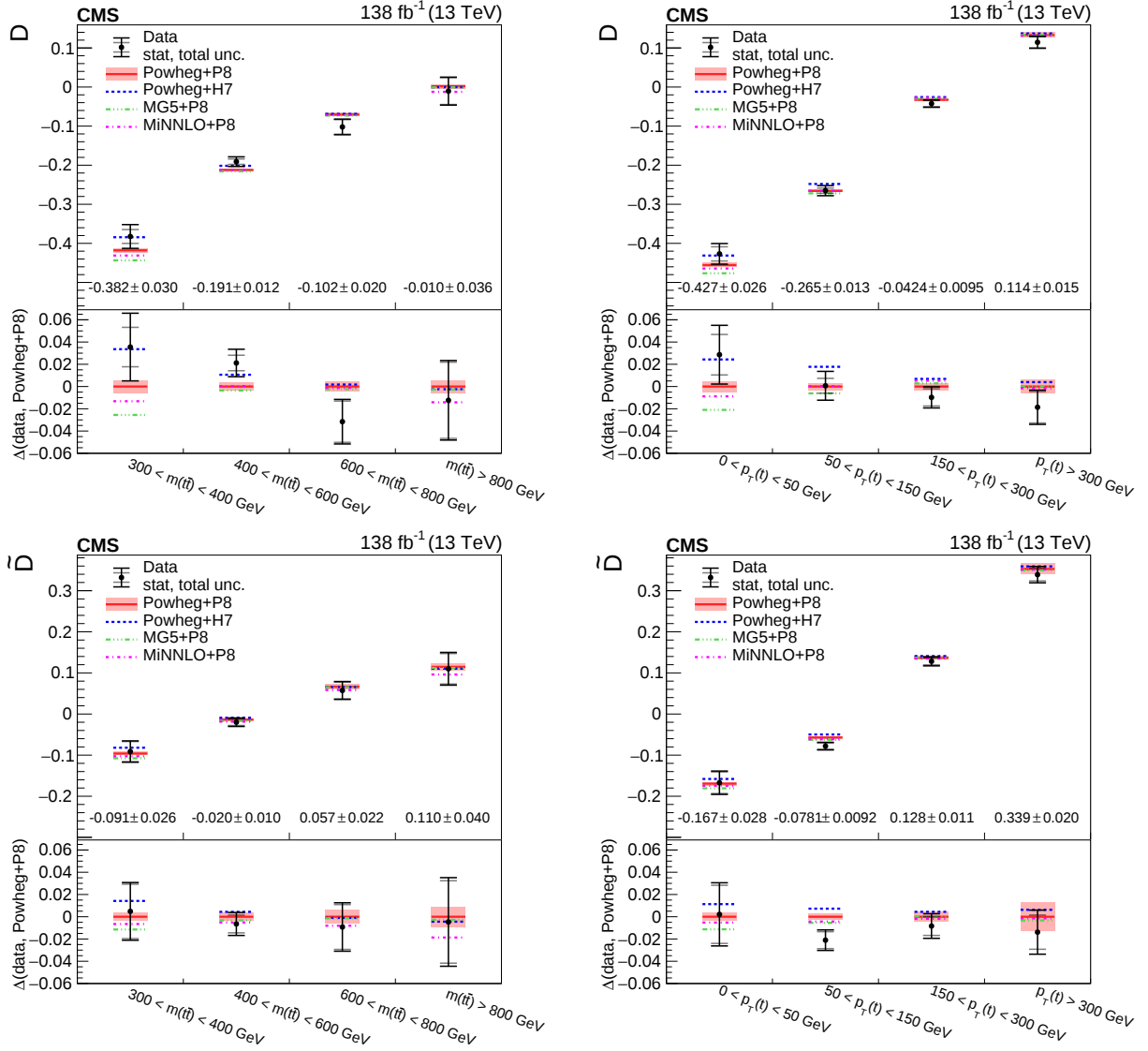


Figure 23: Results of the D and $\tilde{D}$ measurements in bins of $m(t\bar{t})$ and $p_T(t)$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the lower panel results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties.

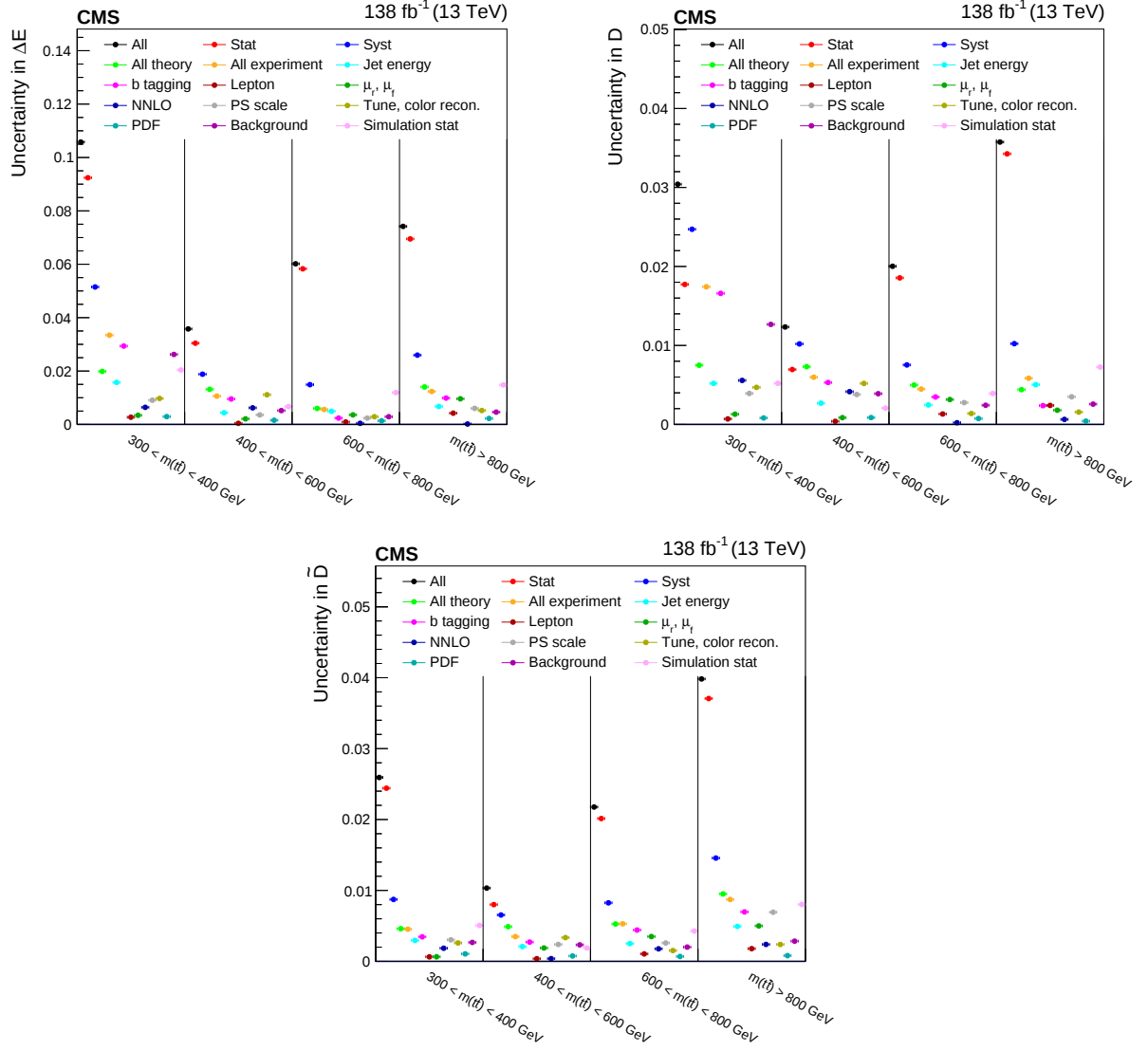


Figure 24: Contribution of individual uncertainty sources or groups of uncertainties in the measured ΔE , D , and $\bar{D}$ in bins of $m(t\bar{t})$.

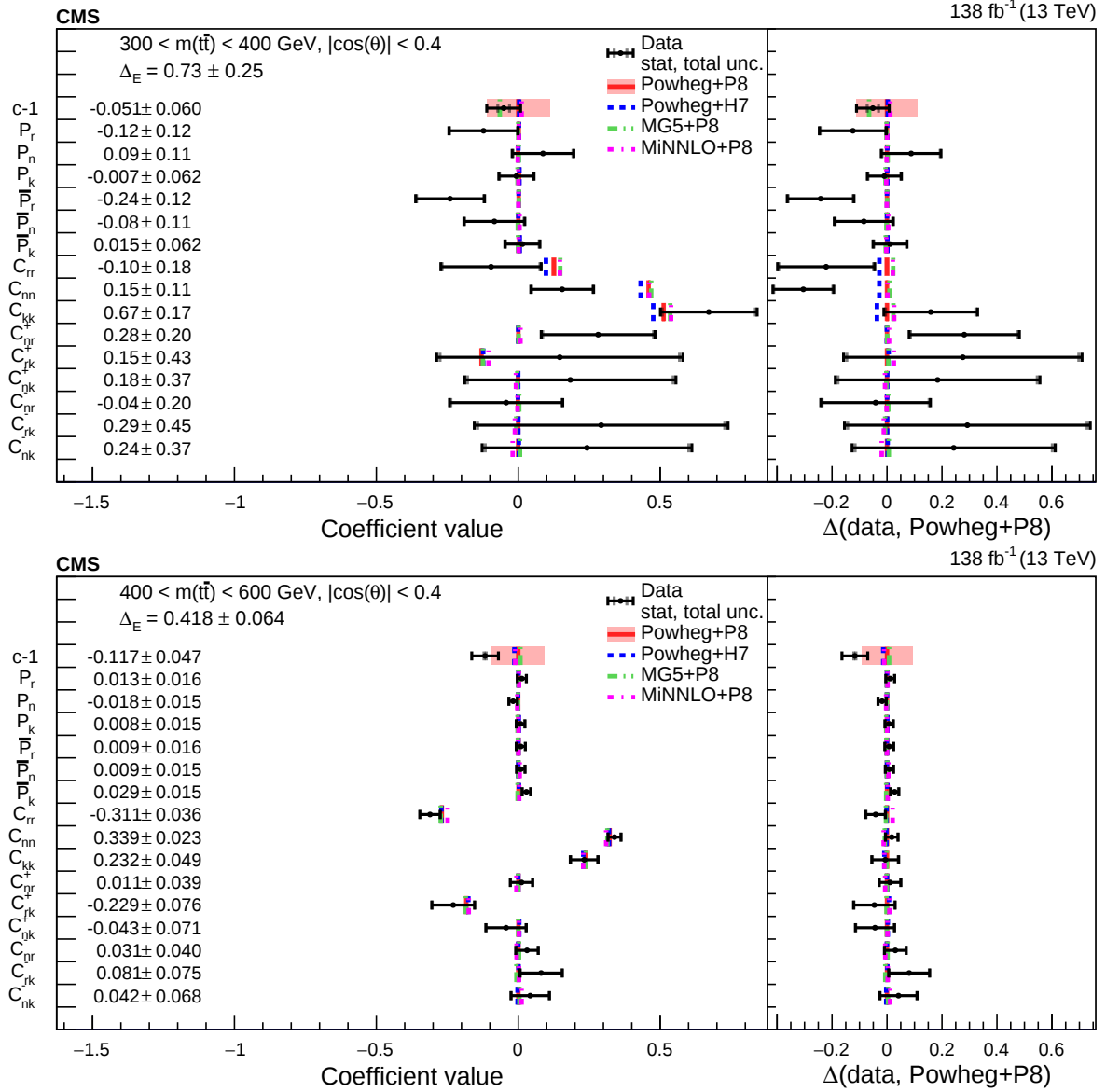


Figure 25: Results of the full matrix measurement in bins of $m(t\bar{t})$ for $|\cos(\theta)| < 0.4$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

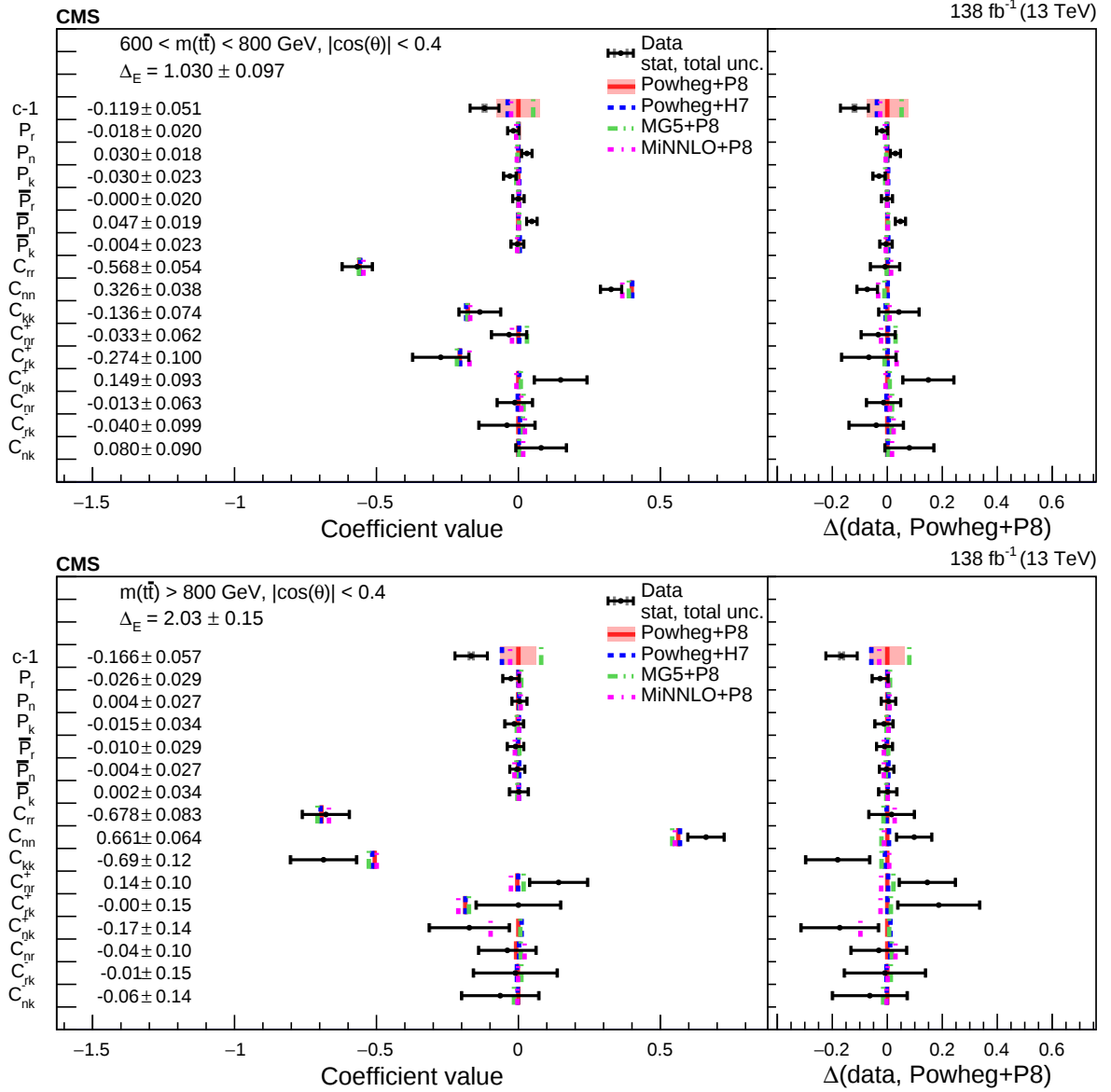


Figure 26: Results of the full matrix measurement in bins of $m(t\bar{t})$ for $|\cos(\theta)| < 0.4$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the right panels, results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties. The values of Δ_E are displayed for each measurement.

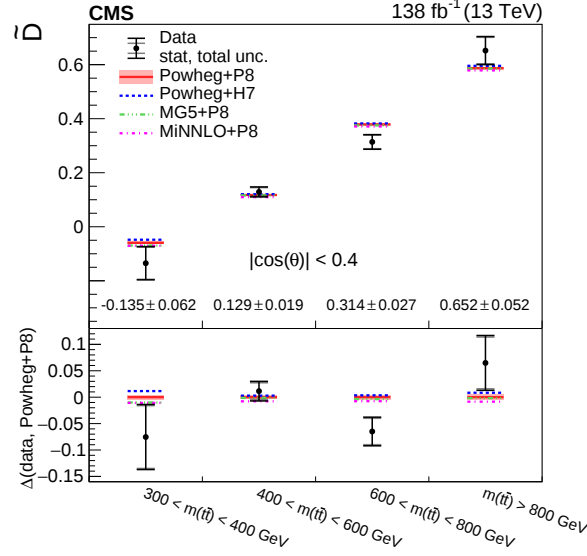


Figure 27: Results of the $\bar{D}$ measurements in bins of $m(t\bar{t})$ for $|\cos(\theta)| < 0.4$. The measurements (markers) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA and MINNLO+PYTHIA. In the lower panel results are presented with the POWHEG+PYTHIA predictions subtracted. The POWHEG+PYTHIA prediction is displayed with ME scale and PDF uncertainties.

Previous measurements of the $t\bar{t}$ entanglement by ATLAS [14] and CMS [15] were performed only at the threshold of $t\bar{t}$ production, where the relative velocity of the top quarks is low. In this analysis, we additionally measure the entanglement at high $m(t\bar{t})$, where, in most of the selected events, the top quark and antiquark decays are space-like separated because of their high relative velocity. Using the decay products, the spin correlation is measured when the top quarks decay. From simulations we know that for $m(t\bar{t}) > 800$ GeV the fraction of space-like separated decays is about 90% [81]. An observation of entanglement could be explained by an unobserved exchange of classical information between the decaying top quarks. Therefore, we introduce a more stringent criterion for entanglement that cannot be explained by such an exchange of information at $v \leq c$ alone (“critical entanglement”). For this, the time-like separated decays are assumed to contribute with the maximum possible value for entanglement of $\Delta_{E\text{max}} = 3$, while the space-like separated decays should at least fulfill the condition $\Delta_{E\text{sep}} = 1$. Therefore, the lower boundary of critical entanglement $\Delta_{E\text{crit}}$ can be defined for a given fraction f of space-like separated decays as follows:

$$\Delta_{E\text{crit}} = f\Delta_{E\text{sep}} + (1 - f)\Delta_{E\text{max}}. \quad (16)$$

As was shown in Ref. [82], using top quark decays in the definition of f results in the most stringent criterion $\Delta_{E\text{crit}}$. The most sensitive measurements in the threshold and high- $m(t\bar{t})$ kinematic regions are summarized in Fig. 29 together with the value for $\Delta_{E\text{crit}}$ for each case, and the significance with respect to critical entanglement and separable states. The first bin $p_T(t) < 50$ GeV was obtained using the D measurement, and the second bin for $m(t\bar{t}) > 800$ GeV and $|\cos(\theta)| < 0.4$ was obtained using the full matrix measurement. In the second bin, the space-like fraction is $f = 90\%$, which corresponds to a $\Delta_{E\text{crit}} = 1.2$. The measured (expected) value exceeds this limit by 5.4 (4.1) standard deviations as shown by the blue vertical arrow.

To validate the Gaussian approximation used in calculating these significances, we perform profile likelihood fits for fixed values of Δ_E in the bin with $m(t\bar{t}) > 800$ GeV and $|\cos(\theta)| < 0.4$.

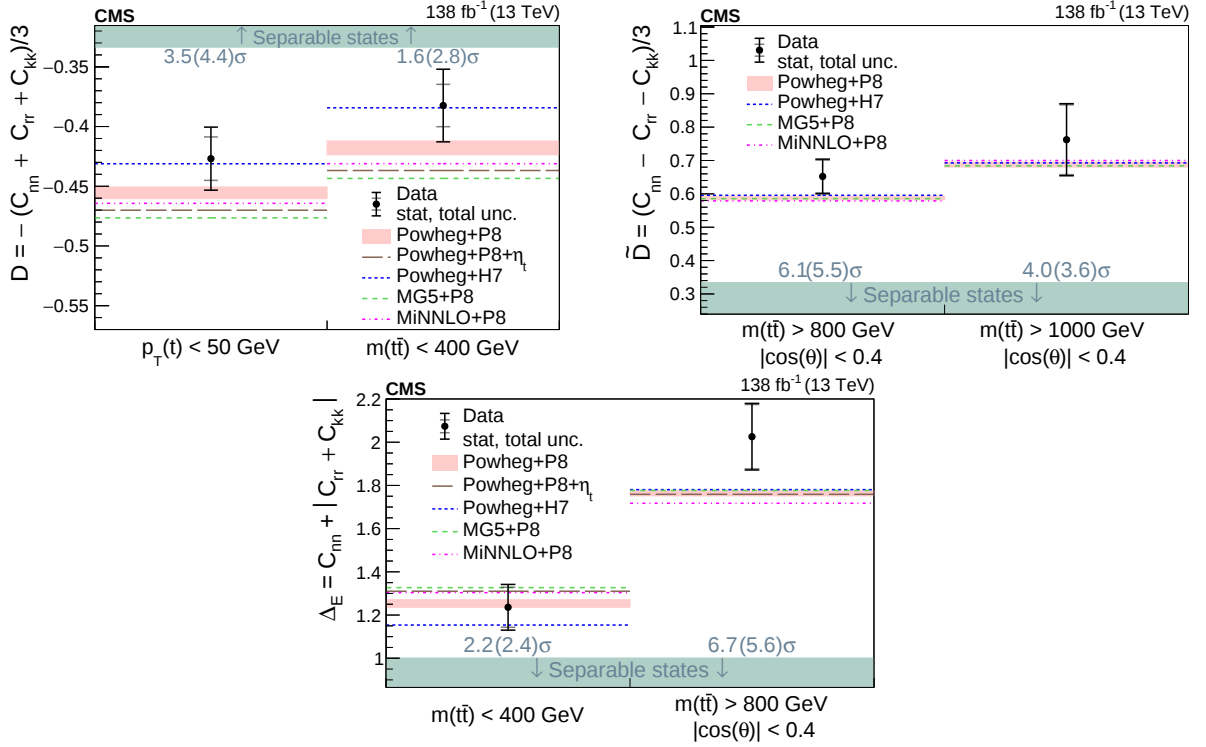


Figure 28: Entanglement results for the D measurement in the threshold region (upper left), $\bar{D}$ measurement in the high- $m(t\bar{t})$ region (upper right), and the full matrix measurement in different $m(t\bar{t})$ regions (lower). The measurements (points) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+PYTHIA+ η_t , POWHEG+HERWIG, MADGRAPH5_aMC@NLO+PYTHIA, and MINNLO+PYTHIA. The POWHEG+PYTHIA prediction is displayed with the ME scale and PDF uncertainties, while for all other predictions only the central values are indicated. The observed (expected) significance of the deviation from the boundary of separable states (green region) is quoted in standard deviations (σ).

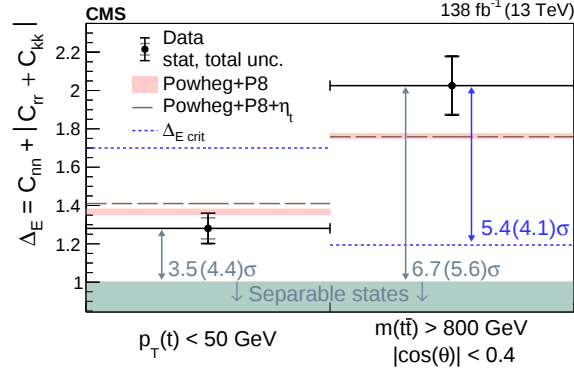


Figure 29: The observed levels of entanglement characterized by Δ_E are shown in the threshold region using the D measurement (first bin), and in the high- $m(t\bar{t})$ region using the full matrix measurement (second bin). The measurements (points) are shown with the statistical uncertainty (inner error bars) and total uncertainty (outer error bars) and compared to the predictions of POWHEG+PYTHIA, POWHEG+PYTHIA+ η_t . The POWHEG+PYTHIA prediction is displayed with the ME scale and PDF uncertainties. The horizontal blue lines correspond to the maximum level of entanglement $\Delta_{E \text{ crit}}$ that can be explained by the exchange of information between t and $\bar{t}$ at the speed of light. The significance in standard deviations (σ) by which the measurement exceeds $\Delta_{E \text{ crit}}$ and unity is quoted in blue and light green, respectively, and indicated by the corresponding arrows.

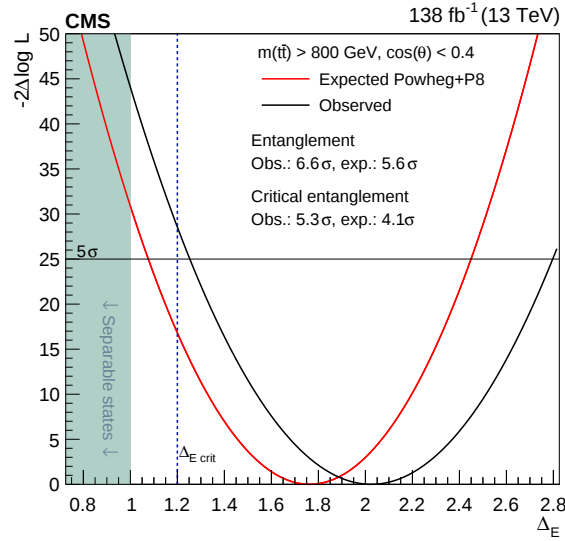


Figure 30: Results of the profile likelihood scans. The quantity $-2\Delta \log(L)$ is shown as function of Δ_E in the bin with $m(t\bar{t}) > 800$ GeV and $|\cos(\theta)| < 0.4$ for data (black line) and the POWHEG+PYTHIA simulation (red line). The observed and expected significances in standard deviations (σ) for Δ_E exceeding unity and $\Delta_{E \text{ crit}}$ are quoted.

For this test, the parameter transformation $C_{nn} = \Delta_E - |C_{rr} + C_{kk}|$ is applied to make Δ_E a parameter of L . The significances are calculated as $\sqrt{-2\Delta \log(L)}$, where $\Delta \log(L)$ is the difference between the profiled likelihood values for a fixed value of Δ_E and the global maximum. In Fig. 30, the scan of $-2\Delta \log(L)$ is shown as a function of Δ_E . The extracted significances for $\Delta_E = 1$ and 1.2 are in close agreement with those obtained with the approximate method.

11 Summary

The polarization and spin correlation in top quark pair ($t\bar{t}$) production are measured in events with an electron or a muon plus jets in the final state. The entanglement between the spins of the top quark and antiquark is determined from the measured spin correlation by applying the Peres–Horodecki criterion. The measurements are based on proton-proton collision data at $\sqrt{s} = 13$ TeV collected by the CMS experiment at the LHC, corresponding to an integrated luminosity of 138 fb^{-1} . The decay products of the top quarks are identified using an artificial neural network. The coefficients of the polarization vectors and the spin correlation matrix are extracted simultaneously from the angular distributions of $t\bar{t}$ decay products using a binned likelihood fit. This is done both inclusively and in various regions of the phase space. The observed polarization and spin correlation are in agreement with the standard model expectations. The standard model predicts entangled $t\bar{t}$ states at the production threshold and at high masses of the $t\bar{t}$ system. Entanglement is observed in events with high $t\bar{t}$ mass, with an observed (expected) significance of 6.7 (5.6) standard deviations, while in events with low transverse momentum of the top quark a significance of 3.5 (4.4) standard deviations is observed (expected). This is the first observation of entanglement at high $t\bar{t}$ mass where in about 90% of the observed $t\bar{t}$ events the decays of the top quark and antiquark are space-like separated.

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