

Search for Extremely-High-Energy Neutrinos and First Constraints on the Ultrahigh-Energy Cosmic-Ray Proton Fraction with IceCube

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We present a search for the diffuse extremely-high-energy neutrino flux using 12.6 years of IceCube data. The nonobservation of neutrinos with energies well above 10 PeV constrains the all-flavor neutrino flux at 10^{18} eV to a level of $E^2\Phi_{\nu_e+\nu_\mu+\nu_\tau} \simeq 10^{-8} \text{ GeV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$, the most stringent limit to date. Using these data, we constrain the proton fraction of ultrahigh-energy cosmic rays (UHECRs) above $\simeq 30 \text{ EeV}$ to be $\lesssim 70\%$ (at 90% CL) if the cosmological evolution of the sources is comparable to or stronger than the star formation rate. This is the first result to disfavor the “proton-only” hypothesis for UHECR in this evolution regime using neutrino data. This result complements direct air-shower measurements by being insensitive to uncertainties associated with hadronic interaction models. We also evaluate the tension between IceCube’s nonobservation and the $\sim 200 \text{ PeV}$ KM3NeT neutrino candidate (KM3-230213A), finding it to be $\sim 2.9\sigma$ based on a joint-lifetime fit between neutrino datasets.

Introduction—Extremely-high-energy neutrinos (EHE ν , $E_\nu \gtrsim 10^{16} \text{ eV} = 10 \text{ PeV}$) are unique messengers of the distant Universe. Unlike photons and ultrahigh-energy cosmic rays (UHECRs, $E_{\text{CR}} \geq 10^{18} \text{ eV} = 1 \text{ EeV}$), neutrinos are chargeless and only weakly interacting, allowing them to travel undeflected by magnetic fields and unattenuated by interactions with background photons. Their fluxes are closely linked to the properties of UHECR sources, which remain unidentified [1, 2]. Of particular interest is the chemical composition of UHECRs, which carries more information about the source environments than spectral measurements. Inside source environments, UHECRs can interact with ambient photon fields and matter, producing *astrophysical neutrinos* carrying up to $\sim 5\%$ of the parent cosmic ray energy. Additionally, after escaping their sources, UHECRs can interact with the cosmic microwave background (CMB) and extragalactic background light (EBL), creating a flux of *cosmogenic neutrinos* [3–20]. Interactions with the CMB are presumed responsible for the “Greisen-Zatsepin-Kuz’mín (GZK) cutoff” of extragalactic UHECRs [21, 22] above

$\sim 10^{19.6} \text{ eV}$. The production of cosmogenic neutrinos depends on a few key features of UHECR sources: their composition, spectrum, and distribution as a function of redshift. Thus, the measurement or even nonobservation of cosmogenic neutrinos can constrain some of these features.

In this Letter, we report a search for EHE ν using 12.6 years of data from the IceCube Neutrino Observatory. The data were taken between June 2010 and June 2023, corresponding to 4605 days of livetime. This is 50% more exposure than that of the previous IceCube search [23]. Additionally, the event selection has been reoptimized, improving the effective area by $\sim 15\%$ near 1 EeV. The null observation of cosmogenic neutrinos places significant constraints on the cosmological evolution of UHECR sources and, moreover, the composition of UHECRs. In this work, we investigate the specific hypothesis of a proton-only composition of UHECRs with the GZK cutoff generating the observed suppression of UHECRs at EeV energies. The method was proposed in [9], and in a similar fashion applied to the neutrino

measurement by the Pierre Auger Collaboration [24]. We find, at 90% CL, that the observed fraction of UHECRs that are protons at Earth above $\simeq 30$ EeV cannot exceed 70% if the source evolution is comparable to the star formation rate (SFR)—a general tracer of matter density in the Universe. These constraints are complementary to, and agree with, direct air-shower measurements [25, 26] by being insensitive to uncertainties associated with hadronic interaction models.

Data Sample—IceCube [27] is a neutrino detector at the South Pole. It consists of 5160 digital optical modules (DOMs), distributed on 86 strings, instrumenting a cubic kilometer of ice at depths between 1450 and 2450 m. Each DOM hosts a 10-inch photomultiplier tube [28] and readout electronics [29]. Charged particles produced in neutrino interactions give rise to Cherenkov light when propagating through the ice. Those Cherenkov photons are detected by DOMs and converted into photoelectrons (PE). On top of the IceCube strings, a surface array called IceTop [30] measures cosmic-ray air showers. EHE ν events in IceCube are observed as either tracks—light depositions along the trajectory of a long-range μ/τ produced in ν_μ/ν_τ charged-current interactions—or cascades—approximately spherical light depositions arising from all-flavor neutral-current interactions and charged-current interactions of ν_e .

This search aims to select cosmogenic neutrinos while rejecting backgrounds. Because $\gtrsim 100$ TeV neutrinos are absorbed by Earth [31], EHE ν s are expected to be downgoing or horizontal at IceCube. The dominant background is downgoing atmospheric muon bundles produced in cosmic-ray air showers. This flux is modeled using CORSIKA [32], with SIBYLL2.3c [33] as the hadronic interaction model and the cosmic-ray flux prediction from [34]. Further backgrounds arise from atmospheric and astrophysical neutrinos. Atmospheric neutrinos are produced by meson decays during cosmic-ray air showers. Their flux is divided into a conventional component [35] originating from pion and kaon decays, and a yet-unobserved prompt component [36] produced by heavier, short-lived mesons. All neutrinos—atmospheric, astrophysical, and cosmogenic—are simulated using the JULIET code [37].

The 3 kHz event trigger rate in IceCube is dominated by atmospheric muons, while the cosmogenic neutrino flux is already constrained to $\ll 1$ event per year [23]. The signal-to-noise ratio is improved by employing an event selection based on quality cuts of high-energy events in combination with an IceTop veto. Full details of the event selection are presented in End Matter. In brief, cosmogenic signal events have extremely high energies and, therefore, produce large amounts of charge (PE). As the atmospheric muon background is exclusively downgoing, we reject most backgrounds with a zenith-angle-dependent charge threshold. To do this, the event direction is reconstructed with a maximum-

likelihood reconstruction using an infinite-length track hypothesis [38].

Energy loss profiles for single muons show large stochastic variations as the muons propagate. In contrast, in high-multiplicity muon bundles, these single-muon fluctuations partly average out. To leverage this, the energy loss profile of events is reconstructed along the track direction, and stricter charge requirements are imposed upon less stochastic events. Using stochasticity information improved the effective area by 15% between 100 PeV and 1 EeV relative to the previous search. Lastly, IceTop is used to further reduce the background from atmospheric events, as described in [39]. The sample is divided into subsamples of tracks and cascades based on the reconstructed particle velocity, and their deposited energy and arrival direction are reconstructed with likelihood-based methods [40, 41] (cf. End Matter).

After the event selection, the expected atmospheric background is 0.40 ± 0.03 events, and up to ~ 5 cosmogenic neutrinos are expected for the most optimistic model [10], consisting of 73% tracks and 27% cascades. The flux beyond PeV energies is not well constrained, and the expectation strongly depends on the assumed model. The astrophysical expectation ranges from ~ 9 events for an unbroken power law with a hard spectral index ($\gamma = 2.37$) [42], down to ~ 0.5 events assuming a power law with a cutoff ($\gamma = 2.39$, $E_{\text{cutoff}} = 1.4$ PeV [43]). At the highest energies, $E_\nu > 100$ PeV, this expectation is reduced to 0.9 events and 3×10^{-30} events, respectively.

For both astrophysical and cosmogenic neutrinos, a flavor ratio of $\nu_e : \nu_\mu : \nu_\tau = 1 : 1 : 1$ at Earth is assumed [45], as well as equal fluxes of neutrinos and antineutrinos.

Three events with PeV energies survive the event selection: a through-going track [46], an uncontained cascade [47], and a starting track [48].

Analysis and Results—To infer physics parameters, the data are fit using a binned Poisson likelihood in the space of reconstructed direction and energy, following the method in [23]. Being in the regime of small statistics, all hypothesis tests and limits are based on ensembles of pseudoexperiments. Confidence intervals are determined using the likelihood ratio test statistic [49].

Systematic uncertainties are treated similarly to [45]: They are varied in pseudoexperiments based on estimated priors. The effect of incorporating systematics is modest, with the differential limit weakened by 4% at 100 PeV, reducing toward 1% at the highest energies. Details of the likelihood and systematics treatment are available in Supplemental Material [50].

Differential limit and model tests—The differential upper limit on the neutrino flux above 5×10^6 GeV is depicted in Fig. 1 as a red line. The sensitivity, i.e., the limit in case of a null observation, and previous limits are also shown. The limit is weakened with respect to the sensitivity below 100 PeV due to the observed events. At the

highest energies the improvement to the previous limit (IceCube 9yr [23]) is comparable to the increase in detector livetime as expected for a largely background-free analysis. At around 1 EeV, additionally, event selection enhancements make a sizable contribution. Notably, by a few hundred PeV, the previous limit deviates from the sensitivity due to observed PeV neutrinos. In this analysis, although a similar number of PeV neutrinos were observed, improved energy reconstructions mean they are incompatible with a flux centered at 100 PeV and above.

The differential limit is compared to a representative variety of cosmogenic neutrino models as gray lines. Qualitatively, larger normalizations, higher maximum accelerating energies, and stronger source evolutions generate larger cosmogenic neutrino fluxes [11, 12, 59]. In contrast, when the injected cosmic-ray primaries are heavy nuclei, photodisintegration becomes the dominant process over photopion production and the neutrino flux is suppressed [6, 13, 60]. All model predictions shown in Fig. 1 (except Van Vliet *et al.* 2019 [20], abbreviated “vV2019” hereafter) assume a pure-proton composition with moderate source redshift evolutions comparable to the SFR. The maximum acceleration energy varies between 10^{11} GeV and 10^{12} GeV.

For each aforementioned model, we performed a likelihood ratio test as described in Supplemental Material [50]; the results are in Table I. Although three events

were observed, the best-fit normalization for a cosmogenic flux component is zero for all tested models. This indicates the data can be sufficiently explained by astrophysical neutrinos. All tested cosmogenic models assuming a pure proton composition of UHECRs are rejected at 95% CL. This indicates that regardless of the differences between those models, if the SFR is driving the source evolution of UHECRs, a proton-only composition can be excluded.

TABLE I. A selection of cosmogenic neutrino models, the model rejection factor (MRF [64]) at 90% CL, and associated p value. The analysis strongly ($p < 0.05$) constrains several previously allowed models of the cosmogenic neutrino flux. Cosmogenic models assuming a proton-only composition are marked with a star.

Model	MRF (90% CL)	p value
Ahlers 2010* [10] (1 EeV)	0.28	0.003
Ahlers 2012* [13]	0.65	0.043
Kotera SFR* [11]	0.49	0.027
van Vliet [20]	2.72	0.268
($f_p = 0.1, m = 3.4, \alpha = 2.5$)		
Murase AGN [63]	0.47	0.057
($\gamma = 2.0, \xi_{\text{CR}} = 3$)		
Murase AGN [63]	0.62	0.019
($\gamma = 2.3, \xi_{\text{CR}} = 100$)		

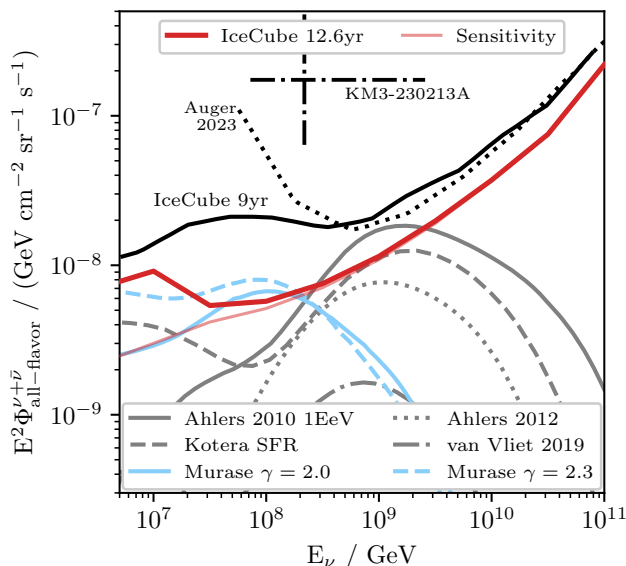


FIG. 1. Differential upper limit (90% CL) on the neutrino flux. The differential limit is compared to the IceCube 9 year result [23], the limit by Auger [61], the flux inferred from KM3-230213A [62], cosmogenic neutrino flux models [10, 11, 13, 20] and a UHE astrophysical model [63]. The model from vV2019 [20] assumes $\alpha = 2.5$, $E_{\text{max}} = 10^{20}$ eV, $m = 3.4$, and a 10% proton fraction. The Auger limit is rescaled to all-flavor, decade-wide bins for comparison.

Proton fraction constraints—Given the measured UHECR flux, the nonobservation of neutrinos imposes constraints on the sources. This approach is complementary to many existing models, which focus on accurately describing the cosmic-ray energy spectrum and composition and, thus, also obtain an estimation of the accompanying cosmogenic neutrino flux [15, 19, 65, 66].

The CRPropa package [67] is used to model cosmogenic fluxes (following vV2019 [20]). In the simulation, protons and secondary neutrinos are propagated to Earth including energy losses from photopion production and pair production on the CMB and EBL [68], neutron decay and cosmological adiabatic losses. Identical sources are distributed homogeneously and isotropically with a power-law injection spectrum $\Phi(E) \propto E^{-\alpha} \exp(-E/E_{\text{max}})$ with spectral index $\alpha \in [1.0, 3.0]$ and exponential cutoff at $E_{\text{max}} \in [4 \times 10^{10} \text{ GeV}, 10^{14} \text{ GeV}]$.

Two different models for cosmological source evolution are tested:

$$\text{SE}_1(z) = \begin{cases} (1+z)^m, & z \leq z' \\ (1+z')^m, & z > z' \end{cases} \quad (1)$$

with $z' = 1.5$ up to $z_{\text{max}} = 4$ [20], and a more conservative model of $\text{SE}_2(z) = (1+z)^m$ with $z_{\text{max}} = 2$, where m denotes the source evolution parameter. The simulation is normalized to the all-particle cosmic-ray flux measured by Auger at $10^{10.55}$ GeV. We normalize to the highest-energy data point below the observed GZK suppression, such that the cosmic-ray flux at the suppression energy

is saturated. This defines the flux corresponding to a proton fraction at Earth (f_p) of 100% above energies of $\simeq 30$ EeV. The reference energy impacts the resulting neutrino fluxes. A systematic shift to the reference energy on the order of the systematic energy scale of Auger of $\pm 14\%$ [25] results in a 5% shift of the overall neutrino flux.

Figure 2 shows the construction of the f_p constraints. The light-colored histograms show the simulated proton flux saturating the Auger measurement and the secondary neutrino flux. The source parameters α and $E_{\max}$ are chosen to minimize the integral neutrino energy flux to obtain a conservative prediction for a given value of m . The relatively wide range for α is motivated by both experimental and theoretical work, e.g., the Auger Collaboration [69] showing that α between 1 and 2 are allowed. Allowing this wider range gives a slightly more conservative result than bounding α at 2. The range for $E_{\max}$ is bracketed by the “GZK-cutoff” energy at the low end, and by a value much higher than the observed cosmic rays on the other. In practice, when marginalizing, the minimum value for $E_{\max}$ is always chosen. The flux shown in the figure is in tension with IceCube data, and, thus, f_p can be constrained based on the determined upper limit. As suggested in vV2019 [20], f_p can be determined by comparing the predicted neutrino flux with the experimental limit at 1 EeV. However, we instead perform a model test, which improves the sensitivity.

This procedure is repeated for different values of the source evolution parameter m , and the resulting constraints are shown in Fig. 3 for the source evolution models $SE_1(z)$ and $SE_2(z)$. The value of m for UHECR sources is unknown, but here we focus on the range in which f_p can be constrained by this analysis. For instance, given the source evolution is comparable to the SFR or stronger, f_p is constrained to be below about 70%. Alternatively, due to the degeneracy between f_p and m , the results can be interpreted as an upper bound on the source evolution of $m \lesssim 3$ for proton-dominated UHECRs, strengthening the claim of the previous analysis [39].

The predicted neutrino fluxes are dominated by distant cosmic-ray sources, from which high-energy cosmic rays are not expected to survive. The model presented here assumes that cosmic-ray sources are distributed homogeneously within the Universe. This is true at large distances, but due to Earth’s position within the Local Supercluster and Local Sheet, the local density of sources is enhanced. This leads to a relative reduction of distant sources and, thus, of the expected neutrino flux. Including a model of the local overdensity of sources based on the star formation rate of local galaxies [25, 71] weakens the neutrino fluxes, and the corresponding proton fraction constraints, by about 3% ($m = 6.0$) to 4% ($m = 2.0$). Additionally, a recent study by Auger shows that up to 5% of UHECRs above 40 EeV can be associated with

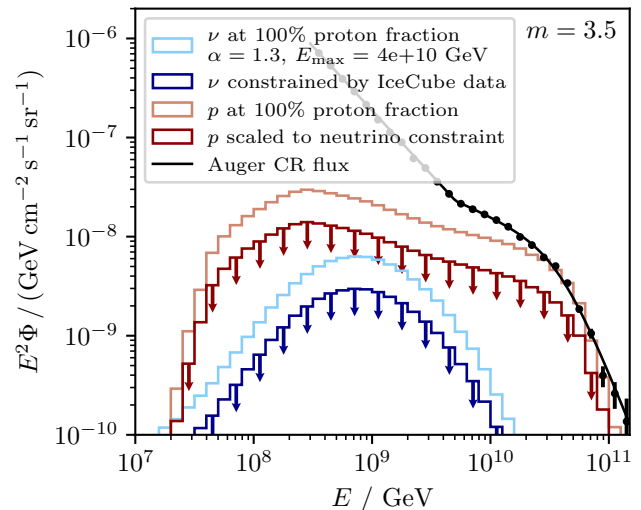


FIG. 2. Illustration of the construction of proton fraction constraints. The red and blue histograms are 90% CL upper limits on the flux of UHECR protons and cosmogenic neutrinos (per flavor), derived from the nonobservation of EHE ν , assuming $SE_1(z)$ with $m = 3.5$. Also plotted in black is the cosmic-ray flux measured by Auger [70]. The light-colored histograms represent the case where the proton flux (light red) is allowed to saturate the Auger measurement at $10^{10.55}$ GeV. The corresponding neutrino flux (light blue) is in tension with the nonobservation in IceCube data and is, therefore, excluded.

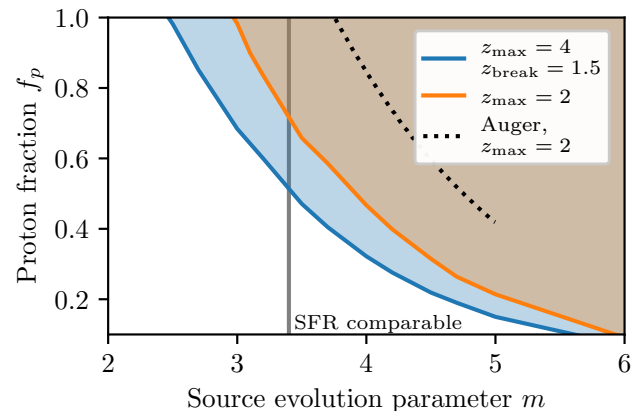


FIG. 3. Constraints on the proton fraction (f_p) of UHECRs as a function of source evolution parameter m at 90% CL based on the nonobservation of UHE neutrinos in this study. The excluded region is shown for the two source evolution models $SE_1(z)$ (blue) and $SE_2(z)$ (orange) and compared to constraints from Auger [24].

Centaurus A as the dominant local source [69]; in this case, the f_p constraint becomes weaker by the same fraction.

For context, constraints already exist from direct air-shower measurements. The Auger $X_{\max}$ data [25] and

the TA event isotropy [26] both favor small proton fractions. However, the data allow [24, 72], and some analyses find [65, 66, 73], a proton fraction as high as $\sim 10\%$. Air-shower-based composition measurements, while powerful, are dependent on hadronic interaction models and the associated uncertainties. As such, independent measurements that do not rely on air-shower observables directly are highly complementary and necessary. In particular, our result in this study does not rely on observables from air showers and is, therefore, insensitive to the uncertainties associated with hadronic interaction models. Although the estimation of the atmospheric muon or neutrino background has a dependence on hadronic interaction models, the influence on the derived constraints is negligible.

Auger has also used their neutrino data to constrain f_p [24], similar to Fig. 3. Here, we substantially improve the constraints. In particular, a direct comparison with the SE₂ model with $z_{\text{max}} = 2$ can be made, where the resulting exclusion contour—the orange shaded region in Fig. 3—is shifted to smaller values of m relative to the Auger result (the black dotted line) by ~ 1 . For example, at $m \sim 3.4$, which is comparable to the SFR, we find $f_p \lesssim 70\%$ at 90%CL, where the Auger result is fully compatible with unity. We note that the IceCube result achieves this improvement despite making very conservative modeling choices, e.g., marginalizing over α and E_{max} .

AGN model constraints—In addition, we tested the active-galactic-nuclei (AGN) model from [63], instead of a cosmogenic flux model. The astrophysical neutrino flux described in this model cannot be explained by the observed sub-PeV astrophysical neutrinos (cf. Fig. 1). These UHE astrophysical neutrinos are indistinguishable from cosmogenic neutrinos event by event. The neutrino emission is based on observed photon fluxes, using phenomenological parameters like the cosmic-ray loading factor ξ_{CR} . The modeled flux scales linearly with ξ_{CR} , so the limit (cf. Table I) can be interpreted as an upper limit of $\xi_{\text{CR}} \leq 1.4$ and $\xi_{\text{CR}} \leq 62$ for assumed CR spectral indexes of $\gamma = 2.0$ and 2.3 , respectively. That the resulting MRFs are < 1 indicates that inner jets of AGN are unlikely to be a dominant source for UHECRs in this model scenario.

KM3-230213A — Recently, KM3NeT published a ~ 220 PeV neutrino candidate [62]. The inferred diffuse flux, also shown in Fig. 1, assumes an E^{-2} ranging from 72 PeV to 2.6 EeV and significantly exceeds the limits presented in this work. With the exposure of this analysis, this flux leads to an expectation of ~ 70 events, inconsistent with our nonobservation at $> 10\sigma$; a transient source hypothesis could reduce this tension [62, 74–76]. Considering a joint fit between IceCube, Auger, and KM3NeT, the tension in the diffuse hypothesis is significantly reduced [77]. After repeating the joint fit with the IceCube exposure presented here, the probability of

the joint fit resulting in one observed event in KM3NeT (with $\mu_{\text{KM3}} = 0.01$ expected events) and no events in both Auger ($\mu_{\text{A}} = 0.3$) and IceCube ($\mu_{\text{IC}} = 0.68$) is $\sim 0.35\%$. The corresponding goodness-of-fit p value determined by the saturated Poisson likelihood test [78] is 0.4% (2.9σ).

The impact on f_p constraints depends on the neutrino’s origin. If produced in a neutrino source environment, the constraints would be unaffected. If cosmogenic [79], a combined analysis will weaken the inferred limits.

Summary—The nonobservation of neutrinos with energies well above 10 PeV in 12.6 years of IceCube data places the most stringent limit on cosmogenic neutrino fluxes to date, reaching a neutrino flux of $E^2 \Phi_{\nu_e + \nu_\mu + \nu_\tau} \simeq 10^{-8} \text{ GeV cm}^{-2} \text{ s}^{-1} \text{ sr}^{-1}$. Additionally, we provide the strongest constraints on the composition of UHECRs obtained by neutrino astronomy, disfavoring proton-only UHECRs if their sources are evolving with the SFR or stronger.

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Data availability—The data that support the findings of this Letter are not publicly available upon publication because it is not technically feasible and/or the cost of preparing, depositing, and hosting the data would be prohibitive within the terms of this research project. The data are available from the authors upon reasonable request.

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END MATTER

Event Selection—The event selection approach is based on a previous IceCube study [39], where signal candidates are found by applying four consecutive steps that are designed to remove atmospheric and astrophysical backgrounds. Table II provides the expected number of background events passing each cut stage, along with the expectation for a cosmogenic neutrino flux [10].

TABLE II. For the four analysis cuts, the table describes the number of atmospheric muons, atmospheric neutrinos, and astrophysical neutrinos [44] passing the cuts. The final column provides a range of cosmogenic neutrino flux predictions between vV2019 [20] and [10].

Cut stage	Atm μ	Atm ν	Astro ν	Cosmo ν
(1) Charge and hit cut	5.5×10^4	4.8	37	2.6–11.5
(2) Track quality cut	8.2×10^3	0.4	1.3	1.4–8.5
(3) Muon bundle cut	0.6	0.2	0.5	0.8–5.6
(4) IceTop veto	0.2	0.2	0.5	0.8–5.4

In the first step of the event selection, only events with a total recorded charge of $Q_{\text{tot}} \geq 27\,500$ PE and a number of hit DOMs of $n_{\text{DOMs}} \geq 100$ are kept. This cut already rejects a majority of atmospheric neutrinos, reducing the expected background to < 10 events.

The second step of the event selection is shown as the gray line in Fig. 4. The cut is a two-dimensional cut in the

plane of reconstructed relative particle velocity $\beta = |\vec{v}|/c$ and the total recorded charge Q_{tot} . Mathematically,

$$\log_{10} \left(\frac{Q_{\text{tot}}}{\text{PE}} \right) > \begin{cases} 5.33 & \beta \leq 0.867 \\ 5.33 - 30(\beta - 0.867) & 0.867 < \beta \leq 0.934 \\ 4.73 & \beta > 0.934. \end{cases} \quad (\text{EM-1})$$

The cut has multiple purposes. It rejects atmospheric neutrinos, and also rejects misreconstructed atmospheric muon events and neutrino events. The speed is reconstructed with the “LineFit” algorithm [80], which assumes a light source traveling with a velocity $\vec{v}$ along an infinite-length track. For a well-reconstructed track the speed will be distributed around the speed of light ($|\vec{v}| \simeq c \simeq 0.3 \text{ m ns}^{-1}$). (Apparently “superluminal” tracks are also possible due to uncertainty of the reconstruction.) At this stage, 65% of signal events are tracks well reconstructed with β within 10% of c , and the majority of outliers are cascades with $\beta < 0.9$. As a consequence, the speed can also be used to separate the final event sample into subsets of cascades and tracks, which is done at $|\vec{v}| = 0.27 \text{ m ns}^{-1}$, shown as a vertical dashed line in Fig. 4. The design of the event selection is mainly motivated by the distribution of the dominant tracklike events but is applied in the same fashion to all

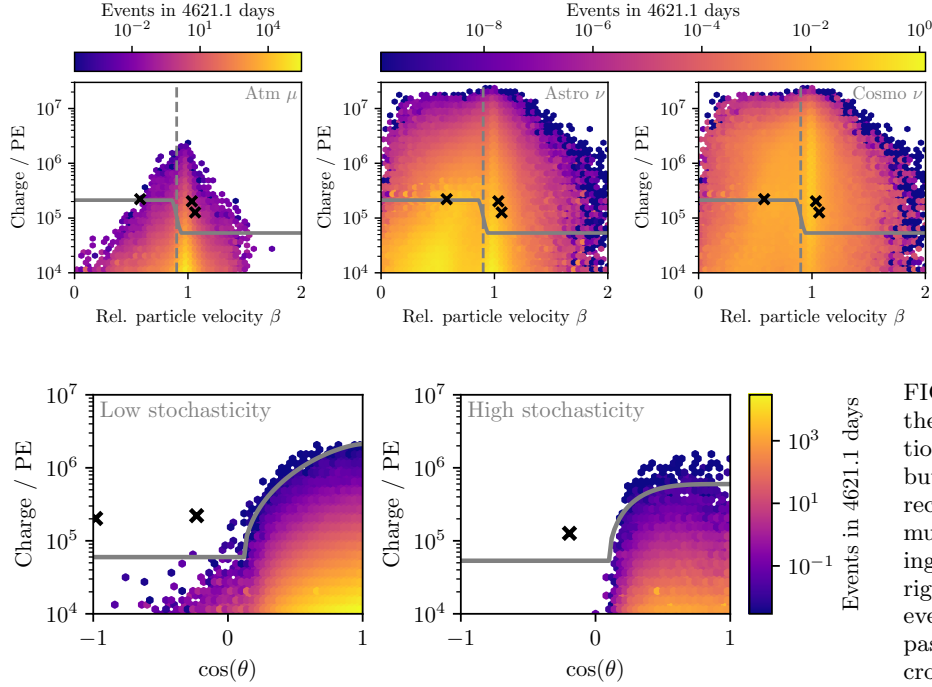


FIG. 4. 2D histograms of the second stage of the event selection. Distribution of charge vs reconstructed relative particle velocity β for atmospheric muons (left), astrophysical neutrinos (center [42]), and cosmogenic neutrinos (right [10]). The cut applied is shown as a gray dashed line. The three candidate events passing all cuts are shown as black crosses.

events, including cascades. After the track quality cut, the atmospheric neutrino expectation is < 1 . After this cut stage, the sample is dominated by downgoing atmospheric muon bundles. Therefore, at this stage in the analysis, we use a one-dimensional fit in observed charge between 5×10^4 – 10^6 PE to determine the overall normalization of the atmospheric muon flux.

The third step of the event selection is designed to remove the main background of downgoing muon bundles. The cut is made in the 2D plane of reconstructed particle zenith $\cos(\theta)$ and total recorded charge Q_{tot} and is visible in Fig. 5 for the atmospheric muon background. In this plane, the differences between signal (cosmogenic neutrinos) and dominant background (atmospheric muons) appear in both the zenith distribution and the energy loss profile of single muons or taus compared to muon bundles with large muon multiplicities. As the energy of a muon increases, its energy losses become more stochastic. In a muon bundle with the same total energy, the energy is distributed among many muons, resulting in a superposition of lower-energy muons losing their energy more continuously, even though their mean dE/dx is comparable. To obtain a measure of the “stochasticity” of an event, the energy loss profile is reconstructed using a segmented energy loss reconstruction [40] over a distance of 40 m. The reconstructed loss profile is then compared to a muon bundle probability density function obtained with PROPOSAL [81]. The probability density function is determined by simulating muon bundles for 40 m repeatedly and recording their total energy loss. Then, we define the reconstructed stochasticity: $\kappa = -\sum_i \log[P(\Delta E_i/E)]/\text{n.d.f.}$, where the sum runs

FIG. 5. A 2D histogram showing the third stage of the event selection. Both plots show the distribution of charge as a function of reconstructed zenith for atmospheric muons, with the left panel showing low-stochasticity events and the right panel showing high-stochasticity events. The three candidate events passing all cuts are shown as black crosses.

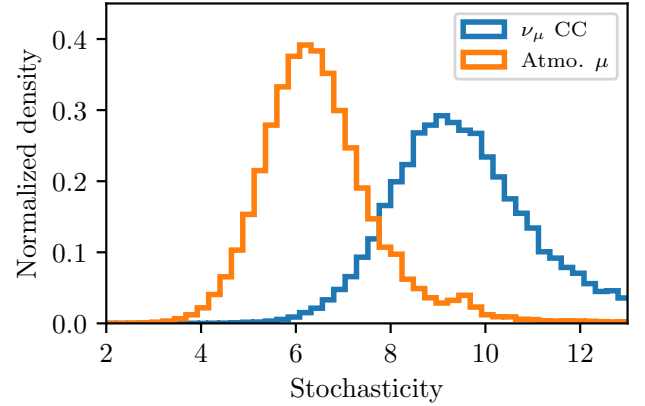


FIG. 6. Distribution of stochasticity for atmospheric muons (muon bundles) and ν_μ CC (single muons) events.

over all unfolded energy depositions ΔE_i in the reconstruction, and $\Delta E_i/E$ are the relative energy losses of the event. This produces a variable comparable to a reduced log-likelihood, the distribution of which is shown for atmospheric muon bundles and single high-energy muons in Fig. 6. Events with $\kappa > 8.37$ are regarded as “highly” stochastic.

With the goal of removing downgoing muon bundles, the cut imposes a stronger requirement on downgoing events than upgoing events. The cut is defined by two charge thresholds (a, b), a shape parameter c , and a tran-

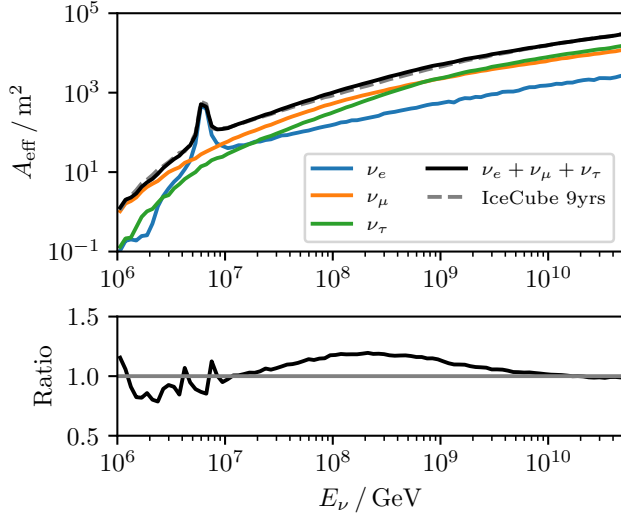


FIG. 7. The sky-averaged effective area of the analysis as a function of energy. The effective area from the previous iteration of this analysis [23] is plotted as a dashed line.

sition point from the upgoing to downgoing region d :

$$\log_{10} \left(\frac{Q_{\text{tot}}}{\text{PE}} \right) > \begin{cases} a & \cos(\theta) < d \\ a + b \sqrt{1 - \left(\frac{1 - \cos(\theta)}{1 - d} \right)^c} & \cos(\theta) \geq d \end{cases} \quad (\text{EM-2})$$

Parameter values are chosen to maximize the model rejection factor for the cosmogenic neutrino flux predic-

tion in [10]. The final parameter values are $a = 4.777$, $b = 1.55$, $c = 1.5$, and $d = 0.12$ for the low-stochasticity events, and $a = 4.727$, $b = 1.05$, $c = 4$, and $d = 0.10$ for high-stochasticity events. The result is a substantially looser selection for highly stochastic downgoing events, as seen in Fig. 5. This use of a stochasticity variable is new to this event selection and improves the MRF by more than 10% relative to the previous event selection.

The fourth and final stage in the event selection uses IceTop to reject atmospheric muons. IceTop hits correlated with an event in the in-ice detector can be found by extrapolating the reconstructed track to the surface and finding the time t_{CA} , where the track is at its closest approach to IceTop. Correlated IceTop hits are defined by the collections of hits that satisfy $-1 \mu\text{s} \leq t_{\text{CA}} \leq 1.5 \mu\text{s}$. Events are vetoed if they have two or more correlated hits in IceTop, reducing the remaining atmospheric muon background by $\sim 60\%$ but only reducing the all-sky neutrino rate by $< 5\%$.

The final zenith-averaged neutrino effective area for the event selection (before applying the IceTop veto) is shown in Fig. 7 and compared to the previous version of the event selection [39]. The effective area describes the neutrino-antineutrino average. The new event selection mostly improves the ν_μ effective area between 10 PeV and 1 EeV by about 30%, while reducing the ν_e and ν_τ effective area between 1 and 10 PeV to reduce the background of astrophysical neutrinos.

Data Release—A data release containing the main results of Figs. 1 and 7 is available online [82].

Supplemental Material for

“A search for extremely-high-energy neutrinos and first constraints on the ultra-high-energy cosmic-ray proton fraction with IceCube”

The IceCube Collaboration

Likelihood Construction: To infer physics parameters, the data is fit using a binned Poisson likelihood in the space of reconstructed direction and energy. The likelihood formulation is adopted directly from the previous search [23]. The observable binning is likewise adopted from [23], except here 10 directional cascade bins are used. The cascade angular binning is guided by the resolution of recent reconstruction algorithms [41].

The expectation in each observable bin i is the sum of cosmogenic ($\mu_{\text{GZK},i}$) and astrophysical ($\mu_{\text{astro},i}$) neutrinos, plus all other atmospheric backgrounds ($\mu_{\text{bkg},i}$), and is compared to the number of observed events n_i .

The overall normalizations of the cosmogenic and astrophysical models— λ_{GZK} and λ_{astro} —are allowed to float, with the latter a nuisance parameter.

$$\mathcal{L}(\lambda_{\text{GZK}}, \lambda_{\text{astro}}) = \prod_i \text{Pois}(n_i | \lambda_{\text{GZK}} \mu_{\text{GZK},i} + \lambda_{\text{astro}} \mu_{\text{astro},i} + \mu_{\text{bkg},i}). \quad (\text{S-1})$$

Being in the regime of small statistics, all hypothesis tests are based on ensembles of pseudo-experiments. Confidence intervals are determined using the likelihood ratio test statistic (TS) [49].

The compatibility of a cosmogenic neutrino model with

observed data is tested via the likelihood ratio test:

$$\Lambda = \log \left(\frac{\sup_{\lambda_{\text{GZK}}, \lambda_{\text{astro}}} \mathcal{L}(\lambda_{\text{GZK}}, \lambda_{\text{astro}})}{\sup_{\lambda_{\text{astro}}} \mathcal{L}(\lambda_{\text{GZK}} = 1, \lambda_{\text{astro}})} \right), \quad (\text{S-2})$$

where $\sup$ denotes the supremum.

To determine EHE ν flux constraints in a more model-independent manner, a differential upper limit is constructed. For this, a sliding E^{-1} neutrino spectrum extending half a decade to both sides around the central energy is injected in half-decade-wide steps [23]. For this flux, a spectral index of $\gamma = 1$ is chosen for comparability with previous results and results from other experiments.

Astrophysical Flux Treatment: To perform hypothesis tests and calculate upper limits, we must make assumptions about the TeV-PeV astrophysical neutrino flux. Such assumptions are also needed when constructing pseudo-experiments.

For model-specific hypothesis tests, we assume a power-law spectrum with spectral index $\gamma = 2.37 \pm 0.09$ observed in the energy range 15 TeV to 5 PeV [42], where the indicated range is considered as a systematic uncertainty. In building pseudo-experiments for these hypothesis tests, the value of λ_{astro} is the best fit obtained from data [51]. This balances model rejection power with the discovery potential for cosmogenic neutrinos, while giving good coverage. The effect of assuming a softer spectral index ($\gamma = 2.52$ [44]) ranges from -30% (Murase [63]) to 6% (van Vliet [20]), and is negligible at the 1% -level for Ahlers 2010 [10].

For construction of the differential neutrino limit and proton fraction constraints, we assume a single power law with exponential cutoff [44]. In building pseudo-experiments we assumed $\lambda_{\text{astro}} = 0$. The treatment is different in order to generate conservative upper-limits. This is because we are building upper-limits by construction. That is, even in case of an observation incompatible with background, only upper limits are reported. Of the commonly assumed models for the astrophysical neutrino flux—single-power laws, broken power laws, etc.—we found that assuming a single power-law model with exponential cutoff generated the most conservative results.

The assumptions made in this paper, and discussed above, differ from those made previously in [23]. Where

the previous work assumed a relatively hard spectrum of $\gamma = 2$, our assumptions here are in better agreement with recent measurements, and produce more conservative results. A full “joint-fit” with the TeV-PeV data will be helpful in further improving these constraints and is the topic of future work.

Systematic Uncertainties: The impact of systematic parameters is estimated by varying them in pseudo-experiments based on estimated priors. This procedure modifies n_i in Eq. S-1, widens the distribution of TS values, and thus the extracted confidence intervals. The parameters taken into account are: the optical efficiency of the DOMs ($\pm 10\%$) [28], the neutrino cross section ($^{+3}_{-20}\%$) [31, 52], the average neutrino inelasticity ($\pm 20\%$) [31, 52], the atmospheric muon flux ($^{+73}_{-46}\%$) and the conventional ($\pm 30\%$) [53] and prompt ($\pm 100\%$) [36] atmospheric neutrino flux. The uncertainty on the atmospheric muon flux is dominated by composition uncertainties of the cosmic-ray flux at Earth and the range is constructed by re-weighting the simulation to a primary cosmic-ray flux of protons or iron nuclei only [32, 34]. The baseline normalization of the atmospheric muon component is measured from a fit to sub-threshold data. The uncertainty on the cross section has two components – one from experimental uncertainties in extracting the parton distribution functions (PDFs) which are inputs to the calculation ($\pm 3\%$), and a second theoretical uncertainty in accounting for the effect of heavy quarks on the evolution of the PDFs at high energies according to perturbative QCD. The baseline cross section value from [31] shows that the value above $\sim 10^4$ GeV can be up to $\sim 20\%$ *smaller* depending the treatment of the bottom/top quark splitting. This leads to a conservative, asymmetric systematics uncertainty on the cross section of $+3\%$ and -20% .

Simulation of EHE ν s in IceCube: Simulation of EHE ν s using the conventional IceCube method of ray-tracing individual photons [54] is computationally infeasible. Instead, pre-calculated photon tables are used [55] to reduce the computational cost. The baseline simulation does not include the Landau-Pomeranchuk-Migdal (LPM) effect [56–58]. The scale of the effect was investigated by a special ν_e simulation including the LPM cascade elongation, and the effect was found to be a sub-percent effect on the total event rate of the EHE ν sample used in this work. The LPM effect on π^0 -production in hadronic showers was not tested here.