

# TopoX: A Suite of Python Packages for Machine Learning on Topological Domains

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## Abstract

We introduce TopoX, a Python software suite that provides reliable and user-friendly building blocks for computing and machine learning on topological domains that extend graphs: hypergraphs, simplicial, cellular, path and combinatorial complexes. TopoX consists of three packages: TopoNetX facilitates constructing and computing on these domains, including working with nodes, edges and higher-order cells; TopoEmbedX provides methods to embed

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topological domains into vector spaces, akin to popular graph-based embedding algorithms such as node2vec; `TopoModelX` is built on top of `PyTorch` and offers a comprehensive toolbox of higher-order message passing functions for neural networks on topological domains. The extensively documented and unit-tested source code of `TopoX` is available under MIT license at <https://pyt-team.github.io/>.

**Keywords:** topological deep learning, topological neural networks, graph neural networks, machine learning, Python packages.

## 1 Introduction

Deep learning traditionally operates within Euclidean domains, focusing on structured data like images (Krizhevsky et al., 2012) and sequences (Sutskever et al., 2014). However, to handle more diverse data types, geometric deep learning (GDL; Bronstein et al., 2021; Zhou et al., 2020; Cao et al., 2020) has emerged. GDL extends deep learning to non-Euclidean data by leveraging geometric regularities like symmetries and invariances. Recently, topological deep learning (TDL; Hajij et al., 2022) has gained attention, exploring models beyond traditional graph-based abstractions to process data with multi-way relations, such as simplicial complexes and hypergraphs. These extensions allow for the representation of diverse data domains encountered in scientific computations (Feng et al., 2019; Schaub et al., 2020; Hajij et al., 2020; Schaub et al., 2021; Roddenberry et al., 2021; Giusti et al., 2023; Yang and Isufi, 2023; Barbarossa and Sardellitti, 2020). Despite theoretical advancements, practical implementation faces challenges due to the lack of accessible software libraries supporting deep learning models with higher-order structures.

In this paper, we present `TopoX`, an open-source suite of Python packages designed for machine learning and deep learning operations in topological domains. `TopoX` is organized into three Python packages: `TopoNetX`, `TopoEmbedX`, and `TopoModelX` (see Figure 1). These packages enhance and generalize functionalities found in popular mainstream graph computations and learning tools, enabling them on topological domains. What sets `TopoX` apart is its abstract general design and the exploitation of the resulting modeling flexibility in the implementation of a broad spectrum of topological domains and TDL models (see Table 1). Further, every domain in `TopoNetX` offers utilities to work with various components such as nodes, edges, and higher-order cells. `TopoNetX` also supports computations using incidence matrices, (co)adjacency matrices, and up, down, and Hodge Laplacians. From a representation learning point of view, `TopoEmbedX` provides methods for embedding topological domains, or parts of these domains, into Euclidean domains. `TopoModelX` offers a wide range of TDL models based on a comprehensive implementation of higher-order message passing (Hajij et al., 2022), built on the `PyTorch` framework (Paszke et al., 2019).

The core objectives of `TopoX` are to: facilitate topological research through foundational code and algorithm dissemination; broaden access to the field with user-friendly topological learning tools for the ML community; serve as a resource for topological learning enriched with examples, notebooks, and visualizations; and provide a unified API for topological domains. This API supports the generalization of topological spaces across scientific computations, enhancing interoperability, productivity, learning, and collaboration, while reducing maintenance, promoting code portability, and enabling parallel computing.

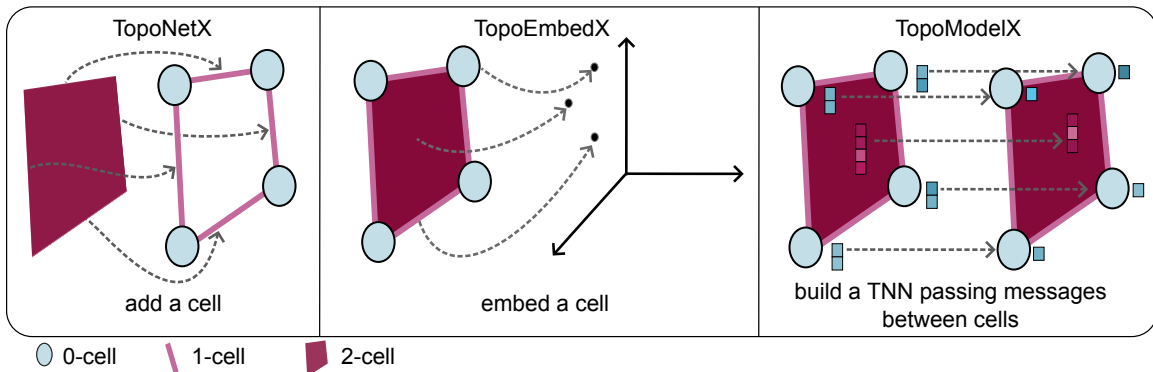


Figure 1: Building blocks from the three packages of the `TopoX` software suite. Left: `TopoNetX` enables building topological domains such as cell complexes. The figure demonstrates adding a 2-cell on a cell complex with `TopoNetX`. Middle: `TopoEmbedX` enables embedding of topological domains inside a Euclidean space. The figure illustrates embedding a 0-cell, a 1-cell and a 2-cell from a cell complex inside a Euclidean space with `TopoEmbedX`. Right: building a topological neural network (TNN) that processes data via higher-order message passing on a cell complex with `TopoModelX`.

## 2 Implementation Overview

The `TopoNetX` package is organized into three main modules: `classes`, `algorithms`, and `transform`. The `classes` module implements numerous common topological domains, such as `SimplicialComplex`, `CellComplex`, and more; inheriting from the abstract class `Complex`. The `algorithms` module implements spectral methods, distance computation, and connected component analysis in topological domains. The `transform` module facilitates conversions between different topological domains. `TopoNetX` uses `NumPy` and `SciPy` backends, and offers toy datasets and examples to facilitate learning and improve understanding.

The `TopoEmbedX` package supports the learning of representations for all topological domains available in `TopoNetX`. This package contains the module `classes`, which implements topological representation learning algorithms that generalize popular graph-based representation learning algorithms, including `DeepCell` and `Cell2Vec` (Hajij et al., 2020). The `TopoEmbedX` package has an API inspired by `scikit-learn` (Pedregosa et al., 2011) and utilizes the `KarateClub` (Rozemberczki et al., 2020) backend. While `TopoEmbedX` leverages methods from `KarateClub`, its functionalities are distinguished by a rigorous foundation in topological representation learning from Hajij et al. (2022). This foundation enables unique, theory-driven contributions, extending the package’s capabilities to embed all topological domains in `TopoNetX` with a single unifying API, not just graphs as in `KarateClub`.

`TopoModelX` is a Python package for topological deep learning, providing efficient tools to implement topological neural networks (TNNs). The package consists of two main modules: `base` and `nn`. The `base` module implements higher-order message passing methods, allowing the construction of general-purpose TNNs using the tensor diagram formalism introduced in Hajij et al. (2022) and surveyed in Papillon et al. (2023b). The `nn` module

implements various TNNs on popular topological domains, such as simplicial complexes, cell complexes, hypergraphs, and combinatorial complexes. Each implementation includes a corresponding Jupyter notebook tutorial for a user-friendly initiation into TDL. `TopoModelX` leverages `PyTorch` and `PyG` (`PyTorch Geometric`) backends (Fey and Lenssen, 2019). The `TopoModelX` package is the outcome of the unifying TDL framework introduced in Hajij et al. (2022) which lead to the coding challenge that crowd-sourced the implementations of TDL models (Papillon et al., 2023a).

### 3 Comparison and Interaction with Other Packages

The libraries most closely related to `TopoNetX` are `NetworkX` (Hagberg et al., 2008) and `HypernetX` (Liu et al., 2021). They facilitate computations on graphs and hypergraphs, respectively. `TopoNetX` utilizes a similar API to these two libraries to facilitate rapid adoption of topological domains, such as simplicial complexes, cell complexes, and colored hypergraphs. The `XGI` package (Landry et al., 2023) offers hypergraph functionalities similar to `HypernetX` with additional support for simplicial complexes and directed hypergraphs.

The closest package to `TopoEmbedX` is `KarateClub` (Rozemberczki et al., 2020), which is a Python package consisting of methods for unsupervised learning on graph-structured data. `TopoEmbedX` extends the functionality of `KarateClub` to topological domains supported in `TopoNetX`. `PyG` and `DGL` (Wang et al., 2019), which are two popular geometric deep learning packages that support deep learning models on graphs, are closely related to `TopoModelX`. The `DHG` (Deep HyperGraph) package (Feng et al., 2019) supports deep learning models defined on hypergraphs. All three of our packages feature a continuous integration pipeline and are well-tested with code coverage of  $\geq 95\%$  per package. This is comparable or better than many related graph-based learning libraries, such as `PyG`, `DGL`, `XGI`, `NetworkX`, and `HyperNetX`. Table 1 provides a comparison between `TopoX` and other Python packages.

### 4 Usage: Elementary Examples

`TopoNetX` provides a user-friendly interface which allows to create a complex in two main steps: first, instantiate the complex; second, add cells to that complex, as shown in the first three lines of the code snippet below. Furthermore, processing data on a complex requires matrices that describe the (co)adjacency of the incidence relations among cells.

```
import toponetx as tnx
cell_complex = tnx.CellComplex()
cell_complex.add_cell([1, 2, 3, 4], rank=2)
cell_complex.add_cell([1, 2, 5], rank=2)
L2 = cell_complex.hodge_laplacian_matrix(2)
```

The following code snippet shows how `TopoEmbedX` embeds edges of the Stanford bunny dataset using the `Cell2Vec` algorithm (Hajij et al., 2020):

```
import topoembedx as tex
cell_complex = tnx.datasets.stanford_bunny("cell")
model = tex.Cell2Vec()
model.fit(cell_complex, nbhd_type="adj", nbhd_dim={"adj": 1})
embeddings = model.get_embedding()
```

Comparison between TopoNetX and other Python packages		
Packages	Domains	Operations
TopoNetX	Graphs, colored hypergraphs, simplicial complexes, path complexes, cell complexes, combinatorial complexes	add_cell, add_node, add_simplex, adjacency_matrix, coadjacency_matrix, incidence_matrix, hodge_laplacian_matrix
NetworkX	Graphs	add_node, add_edge, adjacency_matrix, incidence_matrix, laplacian_matrix
HyperNetX	Hypergraphs	add_node, add_edge, adjacency_matrix, incidence_matrix
XGI	Simplicial complexes, hypergraphs, dihypergraph	add_node, add_edge, adjacency_matrix, boundary_matrix, hodge_laplacian
Comparison between TopoEmbedX and other Python packages		
Packages	Domains	Embedding algorithms
TopoEmbedX	Graphs, colored hypergraphs, simplicial complexes, path complexes, cell complexes, combinatorial complexes	Cell2Vec, DeepCell, CellDiff2Vec, HigherOrderLaplacianEigenMap, HOPE, HOGLEE,
Karateclub	Graphs	Node2Vec, Graph2Vec, Diff2Vec, GL2Vec, IGE, Role2Vec, GraRep
Comparison between TopoModelX and other Python packages		
Packages	Domains	Push-forward operators
TopoModelX	Graphs, (colored) hypergraphs, simplicial complexes, path complexes, cell complexes, combinatorial complexes	(Higher order) message passing, merge operator, split operator
DGL	Graphs	Message passing
DHG	Graphs, hypergraphs	Message passing, hypergraph message passing
PyG	Graphs	Message passing

Table 1: TopoX provides a user-friendly and comprehensive suite for building blocks and computing on topological domains. The table shows a comparison between TopoX and other Python packages.

The following code snippet shows how to instantiate, and run the forward-pass of an example of simplicial neural network (SAN; Battiloro et al., 2024) with TopoModelX:

```

from topomodelx.nn.simplicial.san import SAN
from topomodelx.utils.sparse import from_sparse
sc = tnx.datasets.karate_club("simplicial")
x = torch.tensor([*sc.get_simplex_attributes("edge_feat").values()])
L1_down = from_sparse(sc.down_laplacian_matrix(rank=1))
L1_up = from_sparse(sc.up_laplacian_matrix(rank=1))
san_model = SAN(in_channels=2, hidden_channels=16, n_layers=2)
san_model(x, L1_down, L1_up)

```

TopoNetX provides a high-level declarative interface. In TopoEmbedX, each embedding algorithm is compatible with all complexes available in TopoNetX. In TopoModelX, TNNs are classified according to the topological domain upon which they are defined. In each package, the directories that contain examples and notebooks offer an abundance of code snippets to assist users in starting their journey with TopoX.

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